Filter Coefficient Design

- Many algorithms to find the coefficients for a digital (or analog) filter
  - Butterworth
  - Chebyshev
  - Bilinear transformation
  - Elliptic
- Some specify no ripple in the pass band or the stop band

Parks-McClellan Method

- Parks-McClellan method is a popular method
  - Published in the early 70s
  - Iterative
  - Computationally efficient
  - Works by specifying length of filter and frequency/magnitude pairs
  - See Oppenheim & Schafer for a thorough discussion
Filter Specification

- Filter specifications are frequently given in dB as min/max attenuation/ripple over frequency regions
- Ex:
  - Low-pass filter
  - Maximum +/- 4dB ripple in passband
  - Sampling frequency is 100 MHz
  - Passband from DC to 12.5 MHz
  - Minimum attenuation 22dB from 19 MHz to 25 MHz

Example Filter

- Example filter
  - Low-pass
  - frequencies specified as fractions of $\pi$:
    - $[0 \ 0.25 \ 0.30 \ 1]$;
    - corresponding amplitudes: $[1 \ 1 \ 0 \ 0]$;
  - Don’t care about transition band between 0.25 pi and 0.30 pi
  - Use `remez()` function in matlab
Example Filter

- 7 coeffs.

Example Filter

- 11 coeffs.
Example Filter

- 21 coeffs.

Example Filter

- 51 coeffs.
Example 21-tap Filter

- \( \text{coeffs} = \text{remez}(20, [0 \ 0.25 \ 0.30 \ 1], [1 \ 1 \ 0 \ 0]) \);
- Notice \text{remez} function’s first argument is the number of desired taps minus 1
- \text{remez()} for filter design.
  `>> \text{help remez}`
  to get more information on a matlab function
- To plot the coefficients, use
  `stem(-10:10, \text{coeffs});`

Example Filter Coefficients

- Coefficients of 21-tap filter
- Note \text{sinc()} shape in time domain
- Remember this is a low-pass which is a \text{rect()} in the frequency domain