## Homework 3: Splay trees and KD trees

1. (12 points) The following questions concern splay trees.
a) Is it true that the worst case time performance of insert operation is $\mathrm{O}(\log n)$ ? Briefly explain your answer.
b) Draw the tree after deleting item $\mathbf{8}$ from the following splay tree.

c) Draw the tree after inserting item $\mathbf{8}$ back to the splay tree generated in b).
2. (8 points) Prove the following theorem:

If all nodes in a splay tree are accessed in sequential order (from small to large of the key values), the resulting tree consists of a chain of left children.
Hint: Use this example splay tree to prove to yourself this statement is true.

3. (5 points) Draw the 2-D tree after Inserting item ( 50,30 ) into the 2-D tree below:


