
Binary Search Tree
A Binary Search Tree is a Binary Tree in which, at every
node v , the values stored in the left subtree of v are less
than the value at v and the values stored in the right subtree
are greater.
The elements in the BST must be comparable.
Duplicates are not allowed in our discussion.
Note that each subtree of a BST is also a BST.

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A BST of integers

Describe the values which might appear in the subtrees
labeled A, B, C, and D
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BST Implementation
ADT
stores
tree which
duplicates.

- It is dynamic.
- The elements are ordered in the following ways
- inorder -- as dictated by operator $<$
- preorder, postorder, levelorder - - as dictated by the structure of
the tree

BST Implementation template <typename Comparable>
class BinarySearchTree
$\{$
const Comparable \& findMin( ) const;
const Comparable \& findMax ( ) const;
bool contains ( const Comparable \& x ) const;
bool isEmpty ( ) const;
void printTree ( ) const;
void makeEmpty ( ) ;
void insert (const Comparable \& x )i
void remove( const Comparable \& x )i
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BST Implementation (2)
const BinarySearchTree \&
operator=( const BinarySearchTree \& rhs );
private:
struct BinaryNode
\{
Comparable element;
BinaryNode *left;
BinaryNode *right;


$$
\begin{aligned}
& \ddot{\sim} \\
& 0 \\
& 0 \\
& \tilde{0} \\
& 0 \\
& u
\end{aligned}
$$

$$
\sim
$$

BST Implementation (3)

$$
\begin{gathered}
\text { // private data } \\
\text { BinaryNode *ro }
\end{gathered}
$$

$$
\begin{aligned}
& \text { BST }{ }^{66} \text { contains }{ }^{99} \text { method } \\
& \text { // Returns true if } x \text { is found (contained) in the } \\
& \text { bool contains ( const comparable \& } x \text { ) const } \\
& \left\{\begin{array}{l}
\text { \{eturn contains }(x, \text { root }) ;
\end{array}\right. \\
& \text { \} rement }
\end{aligned}
$$



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The insert Operation

Predecessor in BST
Predecessor of a node v in a BST is the node that holds the
data value that immediately precedes the data at v in order.

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template <typename Comparable>
void BinarySearchTree<Comparable>: :

| makeEmpty ( ) |
| :--- | :--- |
| \{ makeEmpty ( root ); | | // public makeEmpty ( ) |
| :--- |

makeEmpty(




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Tree Iterators As we know there are several ways to traverse through
a BST. For the user to do so, we must supply
different kind of iterators. The iterator type defines
how the elements are traversed.

- InOrderIterator<T> *InOrderBegin ( );
- PerOrderIterator<T> *PreOrderBegin ( );
- PostOrderIterator<T> *PostOrderBegin ( );
- LevelOrderIterator<T> *LevelOrderBegin ( );
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Using Tree Iterator

BST begin( ) and end( )
// BST InOrderBegin( ) to create an InOrderIterator
template <typename T$\rangle$
InOrderIterator<T> BST<T>: : InOrderBegin( ) const
\{ return InOrderIterator( m_root );
\}
// BST InOrderEnd( ) to signal "end" of the tree
template <typename $\mathrm{T}>$
InOrderIterator<T> BST<T>: :InOrderBegin( ) const
\{ return InOrderIterator ( NULL );
Iterator Class with a List
The InOrderIterator is a disguised List Iterator
$/ /$ An InOrderIterator that uses a list to store
$/ /$ the complete in-order traversal
template $<$ typename $T>$
class InOrderIterator

:otctand
10/4/2006
// InOrderIterator constructor
// InOrderIterator constructor
// if root == NULL, an empty list is created
template <typename T>
InOrderIterator<T>: :InOrderIterator ( BinaryNode<T> * root )
\{
$\quad$ FillListInorder( m_theList, root );
$\quad$ m_listIter $=m$ theList.begin( );

$$
\begin{gathered}
\text { List-based InOrderIterator Operators } \\
\text { Call List Iterator operators }
\end{gathered}
$$

$$
\begin{aligned}
& \text { template <typename } \mathrm{T}> \\
& \mathrm{T} \text { InOrderIterator<T>: operator++ ( ) } \\
& \text { \{ } \\
& \text { \} } \quad \text { +m_listIter; } \\
& \text { template <typename } \mathrm{T}> \\
& \mathrm{T} \text { InOrderIterator<T>: operator* ( ) const } \\
& \text { \{ } \\
& \text { return *m_listIter; } \\
& \text { \} template <typename } \mathrm{T}> \\
& \text { bool InOrderIterator<T>: : } \\
& \text { operator!= (const InorderIterator\& rhs ) const } \\
& \text { \{ return m_listIter != rhs.m_listIter; }
\end{aligned}
$$

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$$
\begin{aligned}
& \text { BinaryNode *v }=\left(m_{-}\right. \text {theStack.Top( ))->right; } \\
& \text { m_theStack.Pop(); } \\
& \text { while (v ! = NULI ) } \\
& \text { \{ m_theStack.Push( v ); // push right child } \\
& \text { v = v->left; } \\
& \text { \} // and all left descendants } \\
& \text { return *this; }
\end{aligned}
$$


More Recursive Binary (Search) Tree Functions

- const $T \&$ findMin ( BinaryNode $<T>* t$ )
returns the minimum value in a BST
- int CountFullNodes ( BinaryNode<T> *t )
returns the number of full nodes (those with 2 children) in
a binary tree
- int CountLeaves ( BinaryNode $<T>* t$ )
counts the number of leaves in a Binary Tree
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