Chapter 3

Describing Syntax and Semantics

Introduction

We usually break down the problem of defining a programming language into two parts.

- Defining the PL's syntax
- Defining the PL's semantics

Syntax - the **form** or structure of the expressions, statements, and program units

Semantics - the **meaning** of the expressions, statements, and program units.

Note: There is not always a clear boundary between the two.

Why and How

Why? We want specifications for several communities:

- -Other language designers
- Implementors

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• Programmers (the users of the language)

How? One ways is via natural language descriptions (e.g., user's manuals, text books) but there are a number of techniques for specifying the syntax and semantics that are more formal.

Syntax Overview

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- Language preliminaries
- Context-free grammars and BNF
- Syntax diagrams

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Introduction

A *sentence* is a string of characters over some alphabet.

A *language* is a set of sentences.

A *lexeme* is the lowest level syntactic unit of a language (e.g., *, sum, begin).

A token is a category of lexemes (e.g., identifier).

Formal approaches to describing syntax:

1. Recognizers - used in compilers

2. Generators - what we'll study

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Lexical Structure of Programming Languages • The structure of its lexemes (words or tokens) • token is a category of lexeme • The scanning phase (lexical analyser) collects characters into tokens • Parsing phase(syntactic analyser)determines syntactic structure • Stream of characters

Syntactic

analyser

lexical

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analyser

BNF (continued)

A *metalanguage* is a language used to describe another language.

In BNF, *abstractions* are used to represent classes of syntactic structures--they act like syntactic variables (also called *nonterminal symbols*), e.g.

<while_stmt> ::= while <logic_expr> do <stmt>

This is a *rule*; it describes the structure of a while statement

Grammars

Context-Free Grammars

- Developed by Noam Chomsky in the mid-1950s.
- Language generators, meant to describe the syntax of natural languages.
- Define a class of languages called *context-free languages*.

Backus Normal/Naur Form (1959)

- Invented by John Backus to describe Algol 58 and refined by Peter Naur for Algol 60.
- BNF is equivalent to context-free grammars

BNF

- A rule has a left-hand side (LHS) which is a single non-terminal symbol and a right-hand side (RHS), one or more *terminal* or *nonterminal* symbols.
- A grammar is a finite nonempty set of rules
- A non-terminal symbol is "defined" by one or more rules.
- Multiple rules can be combined with the | symbol so that

```
<stmts> ::= <stmt>
<stmts> ::= <stmnt> ; <stmnts>
And this rule are equivalent
```

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<stmts> ::= <stmt> | <stmnt> ; <stmnts>

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BNF

Syntactic lists are described in BNF using recursion

<ident_list> -> ident

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| ident, <ident_list>

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A *derivation* is a repeated application of rules, starting with the start symbol and ending with a sentence (all terminal symbols)

Derivation using BNF

<sentence> -> <noun-phrase><verb-phrase>.
 <article><noun><verb_phrase>.
 the<noun><verb_phrase>.
 the man <verb_phrase>.
 the man <verb><noun-phrase>.
 the man eats <noun-phrase>.
 the man eats <article> < noun>.
 the man eats the <noun>.
 the man eats the apple.

Another BNF Example

```
Note: There is some
<program> -> <stmts>
                                            variation in notation
<stmts> -> <stmt>
                                            for BNF grammars.
           <stmt> ; <stmts>
                                            Here we are using ->
                                            in the rules instead
<stmt> -> <var> = <expr>
                                            of ::=.
<var> -> a | b | c | d
<expr> -> <term> + <term> | <term> - <term>
<term> -> <var> | const
Here is a derivation:
   <program> => <stmts> => <stmt></proceedings
                 => <var> = <expr> => a = <expr>
                    a = \langle term \rangle + \langle term \rangle
                 =>
                       = \langle var \rangle + \langle term \rangle
                       = b + < term >
                    a = b + const
```

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Derivation

Every string of symbols in the derivation is a *sentential form*.

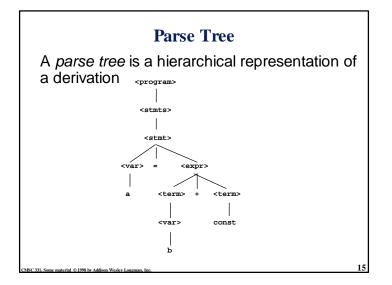
A *sentence* is a sentential form that has only terminal symbols.

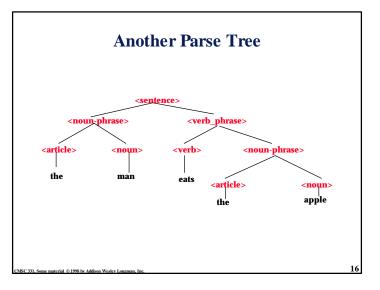
A *leftmost derivation* is one in which the leftmost nonterminal in each sentential form is the one that is expanded.

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A derivation may be neither leftmost nor rightmost (or something else)

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Grammar

A grammar is *ambiguous* iff it generates a sentential form that has two or more distinct parse trees.

Ambiguous grammars are, in general, very undesirable in formal languages.

We can eliminate ambiguity by revising the grammar.

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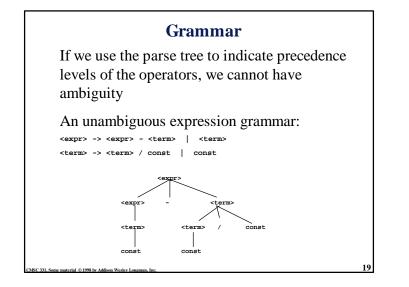
Grammar

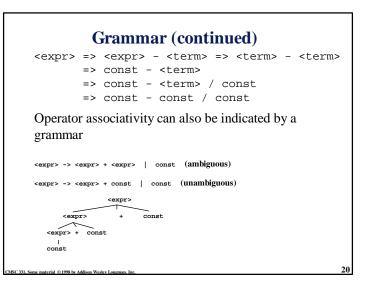
Here is a simple grammar for expressions that is ambiguous

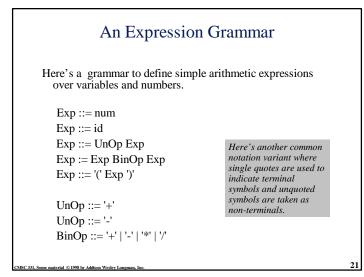
<expr> -> <expr> <op> <expr>
<expr> -> int
<op> -> +|-|*|/

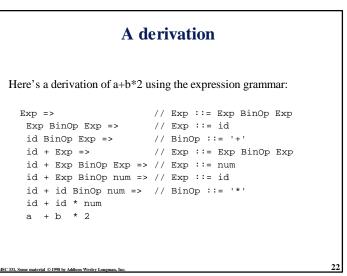
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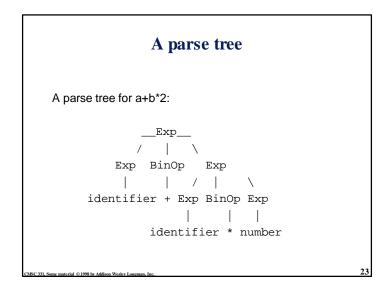
The sentence 1+2*3 can lead to two different parse trees corresponding to 1+(2*3) and (1+2)*3

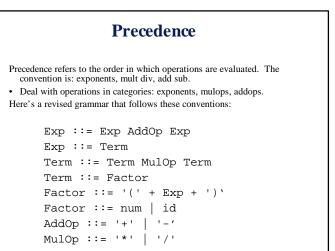




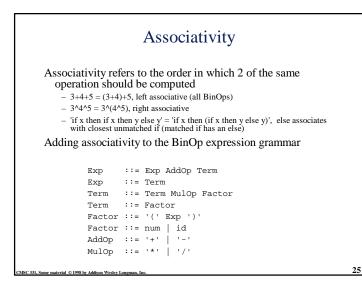


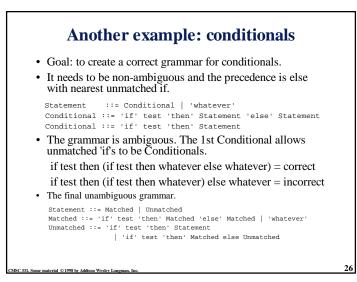






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Extended BNF

Syntactic sugar: doesn't extend the expressive power of the formalism, but does make it easier to use.

Optional parts are placed in brackets ([])

<proc_call> -> ident [(<expr_list>)]

Put alternative parts of RHSs in parentheses and separate them with vertical bars

```
<term> -> <term> (+ | -) const
```

```
Put repetitions (0 or more) in braces ({})
```

<ident> -> letter { letter | digit }

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BNF

<expr> -> <expr> + <term>

<expr> - <term>

<term>

<term> -> <term> * <factor>

<term> / <factor>

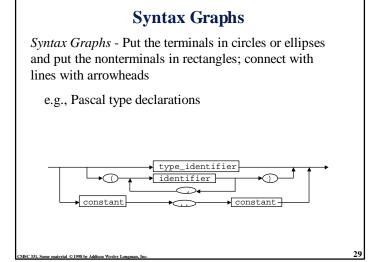
<factor>

EBNF:

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BNF:

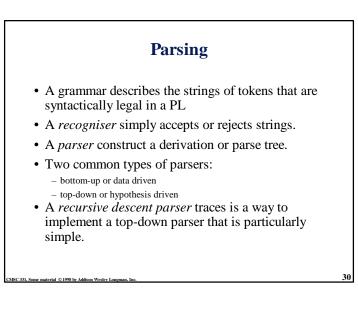
```
<expr> -> <term> {(+ | -) <term>}
<term> -> <factor> {(* | /) <factor>}
```



Recursive Decent Parsing

- Each nonterminal in the grammar has a subprogram associated with it; the subprogram parses all sentential forms that the nonterminal can generate
- The recursive descent parsing subprograms are built directly from the grammar rules
- Recursive descent parsers, like other topdown parsers, cannot be built from leftrecursive grammars (why not?)

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Recursive Decent Parsing Example Example: For the grammar:

<term> -> <factor> {(*|/)<factor>}

We could use the following recursive descent parsing subprogram (this one is written in C)

```
void term() {
  factor(); /* parse first factor*/
  while (next_token == ast_code ||
        next_token == slash_code) {
      lexical(); /* get next token */
      factor(); /* parse next factor */
  }
}
```

Semantics

Static Semantics

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Static semantics covers some language features that are difficult or impossible to handle in a BNF/CFG.

It is also a mechanism for building a parser which produces a "abstract syntax tree" of it's input.

Categories attribute grammars can handle:

- Context-free but cumbersome (e.g. type checking)
- Noncontext-free (e.g. variables must be declared before they are used)

Semantics Overview

- Syntax is about "form" and semantics about "meaning".
- The boundary between syntax and semantics is not always clear.
- First we'll look at issues close to the syntax end, what Sebesta calls "static semantics", and the technique of attribute grammars.
- Then we'll sketch three approaches to defining "deeper" semantics
 - Operational semantics
 - Axiomatic semantics

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- Denotational semantics

Attribute Grammars

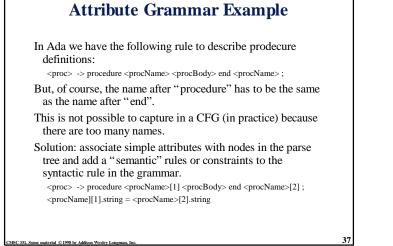
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Attribute Grammars (AGs) (Knuth, 1968)

- CFGs cannot describe all of the syntax of programming languages
- Additions to CFGs to carry some "semantic" info along through parse trees

Primary value of AGs:

- Static semantics specification
- Compiler design (static semantics checking)



Attribute Grammars

Def: An *attribute grammar* is a CFG G=(S,N,T,P)

with the following additions:

- For each grammar symbol x there is a set A(x) of attribute values.
- Each rule has a set of functions that define certain attributes of the nonterminals in the rule.
- Each rule has a (possibly empty) set of predicates to check for attribute consistency

Attribute Grammars

Let $X_0 \rightarrow X_1 \dots X_n$ be a rule.

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Functions of the form $S(X_0) = f(A(X_1), ..., A(X_n))$ define *synthesized attributes*

Functions of the form $I(X_j) = f(A(X_0), ..., A(X_n))$ for i <= j <= n define *inherited attributes*

Initially, there are *intrinsic attributes* on the leaves

Attribute Grammars

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Example: expressions of the form id + id

• id's can be either int_type or real_type

• types of the two id's must be the same

• type of the expression must match it's expected type

BNF: <expr> -> <var> + <var> <var> -> id

Attributes:

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actual_type - synthesized for <var> and <expr>
expected_type - inherited for <expr>

Attribute Grammars

Attribute Grammar:

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2. Syntax rule: <var> -> id Semantic rule: <var>.actual_type ← lookup (id, <var>)

Attribute Grammars (continued)

<expr>.expcted_type \leftarrow inherited from parent

<var>[1].actual_type cokup (A, <var>[1])
<var>[2].actual_type cokup (B, <var>[2])
<var>[1].actual_type =? <var>[2].actual_type

<expr>.actual_type <- <var>[1].actual_type <expr>.actual_type =? <expr>.expected_type

Attribute Grammars (continued)

How are attribute values computed?

•If all attributes were inherited, the tree could be decorated in top-down order.

•If all attributes were synthesized, the tree could be decorated in bottom-up order.

•In many cases, both kinds of attributes are used, and it is some combination of topdown and bottom-up that must be used.

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Dynamic Semantics

No single widely acceptable notation or formalism for describing semantics.

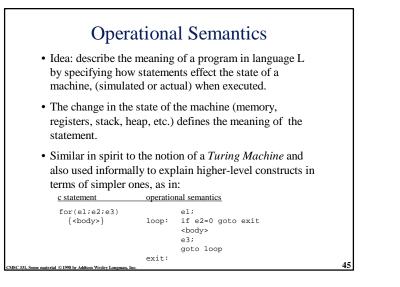
The general approach to defining the semantics of any language L is to specify a general mechanism to translate any sentence in L into a set of sentences in another language or system that we take to be well defined.

Here are three approaches we'll briefly look at:

- Operational semantics
- Axiomatic semantics

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- Denotational semantics



Operational Semantics

- To use operational semantics for a high-level language, a virtual machine in needed
- A *hardware* pure interpreter would be too expensive
- A *software* pure interpreter also has problems:
 - The detailed characteristics of the particular
 - computer would make actions difficult to understand
 - Such a semantic definition would be machine-dependent

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Operational Semantics A better alternative: A complete computer simulation Build a translator (translates source code to the machine code of an idealized computer) Build a simulator for the idealized computer Evaluation of operational semantics: Good if used informally Extremely complex if used formally (e.g. VDL)

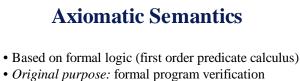
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Vienna Definition Language

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- VDL was a language developed at IBM Vienna Labs as a language for formal, algebraic definition via operational semantics.
- It was used to specify the semantics of PL/I.
- See: *The Vienna Definition Language*, P. Wegner, ACM Comp Surveys 4(1):5-63 (Mar 1972)
- The VDL specification of PL/I was very large, very complicated, a remarkable technical accomplishment, and of little practical use.

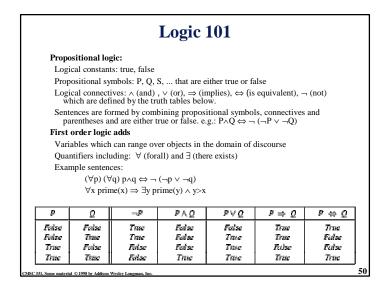


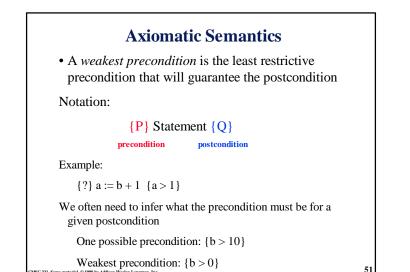
- *Approach:* Define axioms and inference rules in logic for each statement type in the language (to allow transformations of expressions to other expressions)
- The expressions are called *assertions* and are either
 - **Preconditions:** An assertion before a statement states the relationships and constraints among variables that are true at that point in execution

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• **Postconditions:** An assertion following a statement

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Axiomatic Semantics Program proof process: • The postcondition for the whole program is the desired results.

- Work back through the program to the first statement.
- If the precondition on the first statement is the same as the program spec, the program is correct.



Here's how we might define a simple assignment statement of the form x := e in a programming language.

•
$$\{Q_{x\to E}\} x := E \{Q\}$$

• Where Q_{x->E} means the result of replacing all occurrences of *x* with *E* in *Q*

So from

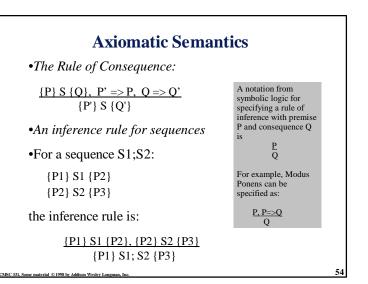
 $\{Q\}$ a := b/2-1 $\{a < 10\}$

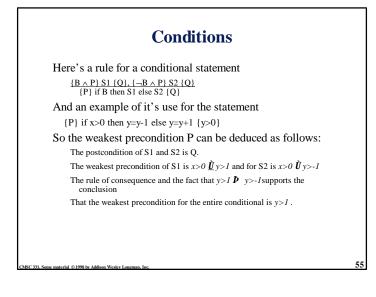
We can infer that the weakest precondition Q

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is

b/2-1<10 or b<22



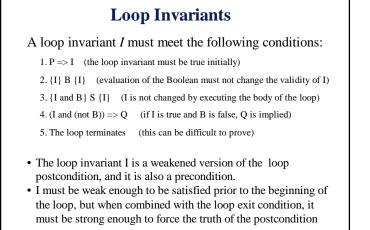


Loops

For the loop construct {P} while B do S end {Q} the inference rule is:

 ${I \land B} S {I}$ ${I} while B do S {I \land \neg B}$

where I is the *loop invariant*, a proposition necessarily true throughout the loop's execution.



Evaluation of Axiomatic Semantics

- Developing axioms or inference rules for all of the statements in a language is difficult
- It is a good tool for correctness proofs, and an excellent framework for reasoning about programs
- It is much less useful for language users and compiler writers

Denotational Semantics

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- A technique for describing the meaning of programs in terms of mathematical functions on programs and program components.
- Programs are translated into functions about which properties can be proved using the standard mathematical theory of functions, and especially domain theory.
- Originally developed by Scott and Strachey (1970) and based on recursive function theory
- The most abstract semantics description method

Denotational Semantics

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• The process of building a denotational specification for a language:

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- 1. Define a mathematical object for each language entity
- 2. Define a function that maps instances of the language entities onto instances of the corresponding mathematical objects
- The meaning of language constructs are defined by only the values of the program's variables

Denotational Semantics (continued)

- The difference between denotational and operational semantics: In operational semantics, the state changes are defined by coded algorithms; in denotational semantics, they are defined by rigorous mathematical functions
- The *state* of a program is the values of all its current variables

$$s = \{ <\!\!i_1, v_1\!\!>\!\!, <\!\!i_2, v_2\!\!>\!\!, \ldots, <\!\!i_n, v_n\!\!> \}$$

• Let VARMAP be a function that, when given a variable name and a state, returns the current value of the variable

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 $VARMAP(i_j, s) = v_j$

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Expressions $M_e(\langle expr \rangle, s) \Delta =$ case <expr> of <dec_num $> => M_{dec}(<$ dec_num>, s)<var> => if VARMAP(<var>, s) = undef then error else VARMAP(<var>, s)
 dinary_expr> => if (M_o(<binary_expr>.<left_expr>, s) = undef OR M_e(<binary_expr>.<right_expr>, s) = undef) then error else if (<binary_expr>.<operator> = '+' then M_e(<binary_expr>.<left_expr>, s) + M_e(<binary_expr>.<right_expr>, s) else Me(<binary_expr>.<left_expr>, s) * M_e(<binary_expr>.<right_expr>, s) aterial © 1998 by Addison Wesley I

Example: Decimal Numbers

 $\begin{array}{l} M_{dec}('0') = 0, \ M_{dec} \ ('1') = 1, \ \ldots, \ M_{dec} \ ('9') = 9 \\ M_{dec} \ (<\!dec_num\!>'0') = 10 \ ^* M_{dec} \ (<\!dec_num\!>) \\ M_{dec} \ (<\!dec_num\!>'1') = 10 \ ^* M_{dec} \ (<\!dec_num\!>) + 1 \end{array}$

 $M_{dec} (\langle dec_num \rangle '9') = 10 * M_{dec} (\langle dec_num \rangle) + 9$

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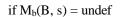
Assignment Statements

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$$\begin{split} M_a(x := E, s) \, \Delta = & \\ & \text{if } M_e(E, s) = \text{error} \\ & \text{then error} \\ & \text{else } s' = \{ <\!\!i_1, '\!\!, \!\!v_1'\!\!>, <\!\!i_2', \!\!v_2'\!\!>, ..., <\!\!i_n', \!\!v_n'\!\!> \}, \\ & \text{where for } j = 1, \, 2, \, ..., \, n, \\ & v_j' = VARMAP(i_j, s) \text{ if } i_j <\!\!> x \\ & = M_e(E, s) \text{ if } i_j = x \end{split}$$





then error

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else if $M_b(B, s) = false$

then s

else if $M_{sl}(L, s) = error$

then error

else M_l(while B do L, M_{sl}(L, s))

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Logical Pretest Loops

- The meaning of the loop is the value of the program variables after the statements in the loop have been executed the prescribed number of times, assuming there have been no errors
- In essence, the loop has been converted from iteration to recursion, where the recursive control is mathematically defined by other recursive state mapping functions
- Recursion, when compared to iteration, is easier to describe with mathematical rigor

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Denotational Semantics

Evaluation of denotational semantics:

- Can be used to prove the correctness of programs
- Provides a rigorous way to think about programs
- Can be an aid to language design
- Has been used in compiler generation systems

Summary

This chapter covered the following

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- Backus-Naur Form and Context Free Grammars
- Syntax Graphs and Attribute Grammars
- Semantic Descriptions: Operational, Axiomatic and Denotational