

Logical Inference 1 introduction

Chapter 9

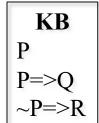
Overview

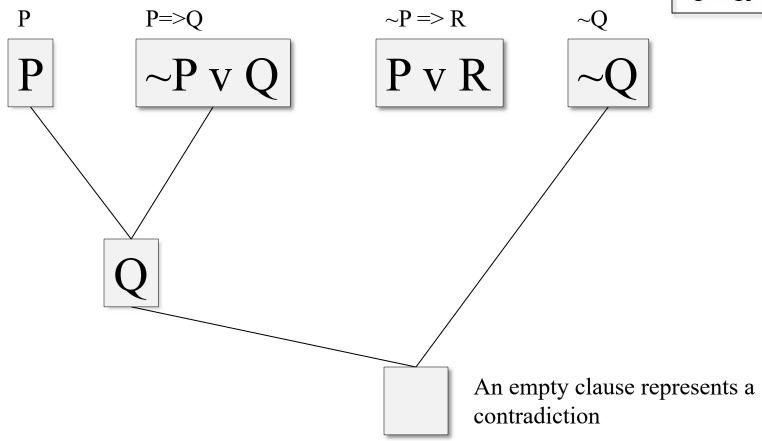
- A: Model checking for propositional logic
- Rule based reasoning in first-order logic
 - Inference rules and generalized modes ponens
 - Forward chaining
 - Backward chaining
- Resolution-based reasoning in first-order logic
 - Clausal form
 - Unification
 - Resolution as search
- Inference wrap up

From Satisfiability to Proof

- To see if a satisfiable KB entails sentence S, see if $\overline{KB} \wedge \overline{-S}$ is satisfiable
 - If it is not, then the KB entails S
 - If it is, then the KB does not entail S
 - -This is a refutation proof
- Consider the KB with (P, P=>Q, ~P=>R)
 - -Does the KB it entail Q? R?

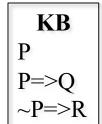
Does the KB entail Q?

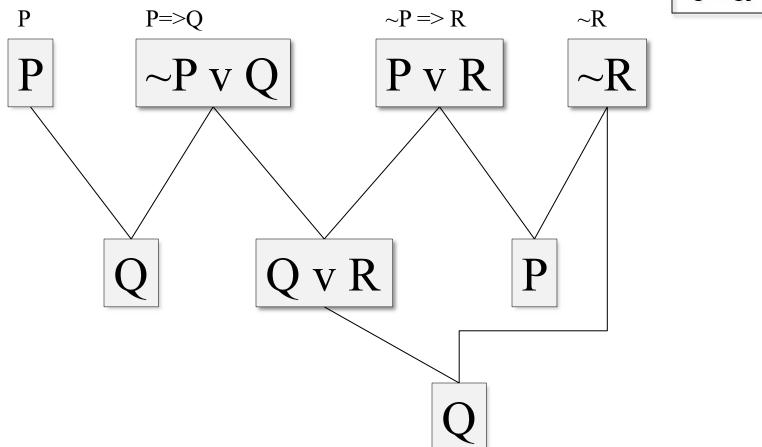




We assume that every sentence in the KB is true. Adding ~Q to the KB yields a contradiction, so ~Q must be false, so Q must be true.

Does the KB entail R?





Adding ~R to KB does not produce a contradiction after drawing all possible conclusions, so it could be False, so KB doesn't entail R.

Propositional logic model checking

- Given KB, does a sentence S hold?
 - -All the variables in S must be in the KB
 - A candidate model is just an assignment of T|F to every variable in the KB
- Basically it is generate and test:
 - Consider candidate models M for the KB
 - -If \forall M S is true, then S is provably true
 - -If \forall M \neg S, then S is provably false
 - -Otherwise (∃M1 S ∧ ∃M2 ¬S): S is **satisfiable** but neither provably true or provably false

Efficient PL model checking (1)

<u>Davis-Putnam algorithm</u> (DPLL) is <u>generate-and-test</u> model checking with several optimizations:

- Early termination: short-circuiting of disjunction or conjunction sentences
- Pure symbol heuristic: symbols appearing only negated or un-negated must be FALSE/TRUE respectively
 e.g., in [(A∨¬B), (¬B∨¬C), (C∨A)] A & B are pure, C impure. Make pure symbol literal true: if there's a model for S, making pure symbol true is also a model
- Unit clause heuristic: Symbols in a clause by itself can immediately be set to TRUE or FALSE

Using the AIMA Code

expr parses a string, and returns a logical expression

```
python> python
Python ...
                                          dpll satisfiable returns a
                                          model if satisfiable else False
>>> from logic import *
>>> expr('P & P==>Q & ~P==>R')
((P \& (P >> Q)) \& (\sim P >> R))
>>> dpll_satisfiable(expr('P & P==>Q & ~P==>R'))
{R: True, P: True, Q: True}
>>> dpll satisfiable(expr('P & P==>Q & \sim P==>R & \sim R'))
{R: False, P: True, Q: True}
>>> dpll satisfiable(expr('P & P==>Q & \sim P==>R & \sim Q'))
False
```

>>>

The KB entails Q but does not entail R

Efficient PL model checking (2)

- WalkSAT: a local search for satisfiability: Pick a symbol to flip (toggle TRUE/FALSE), either using min-conflicts or choosing randomly
- ...or use any local or global search algorithm
- Many model checking algorithms & systems:
- –E.g.: MiniSat: minimalistic, open-source SAT solver developed to help researchers & developers use SAT"
- -E.g.: <u>International SAT Competition</u> (2002...2020): identify new challenging **benchmarks** to promote new **solvers** for Boolean SAT"

```
>>> kb1 = PropKB()
>>> kb1.clauses
[]
>>> kb1.tell(expr('P==>Q & ~P==>R'))
>>> kbl.clauses
[(Q \mid \sim P), (R \mid P)]
>>> kb1.ask(expr('Q'))
False
>>> kb1.tell(expr('P'))
>>> kbl.clauses
[(Q \mid \sim P), (R \mid P), P]
>>> kb1.ask(expr('Q'))
{}
>>> kb1.retract(expr('P'))
>>> kbl.clauses
[(Q \mid \sim P), (R \mid P)]
>>> kb1.ask(expr('Q'))
False
```

AIMA KB Class

PropKB is a subclass

A sentence is converted to CNF and the clauses added

The KB does not entail Q

After adding P the KB does entail Q

Retracting P removes it and the KB no longer entails Q