

#### **Problems with Recursion**

- Recursion is generally favored over iteration in Scheme and many other languages
  - It's elegant, minimal, can be implemented with regular functions and easier to analyze formally
  - Some languages don't have iteration (Prolog)
- It can also be less efficient more functional calls and stack operations (context saving and restoration)
- Running out of stack space leads to failure deep recursion

#### Tail recursion is iteration

- <u>Tail recursion</u> is a pattern of use that can be compiled or interpreted as iteration, avoiding the inefficiencies
- A tail recursive function is one where every recursive call is the last thing done by the function before returning and thus produces the function's value
- More generally, we identify some procedure calls as <u>tail calls</u>

#### Tail Call

A *tail call* is a procedure call inside another procedure that returns a value which is then immediately returned by the calling procedure

def foo(data): bar1(data) return bar2(data) def foo(data): if test(data): return bar2(data) else:

return bar3(data)

A tail call need not come at the textual end of the procedure, but at one of its logical ends

#### Tail call optimization

- When a function is called, we must remember the place it was called from so we can return to it with the result when the call is complete
- This is typically stored on the call stack
- There is no need to do this for tail calls
- Instead, we leave the stack alone, so the newly called function will return its result directly to the original caller

#### Scheme's top level loop

- Consider a simplified version of the REPL
  - (define (repl)
    - (printf ">")
    - (print (eval (read)))
    - (repl))
- This is an easy case: with no parameters there is not much context

#### Scheme's top level loop 2

Consider a fancier REPL

(define (repl) (repl1 0))

(define (repl1 n) (printf "~s> " n) (print (eval (read))) (repl1 (add1 n)))

• This is only slightly harder: just modify the local variable n and start at the top

#### Scheme's top level loop 3

- There might be more than one tail recursive call (define (repl1 n) (printf "~s> " n) (print (eval (read)))) (if (= n 9) (repl1 0) (repl1 (add1 n))))
- What's important is that there's nothing more to do in the function after the recursive calls







Trace shows what's going on > (requireracket/trace) > (load "fact.ss") > (trace fact1) > (fact1 6)	(fact1 6)   (fact1 5)    (fact1 4)     (fact1 3)      (fact1 2)       (fact1 1)       (fact1 0)       1
	2   6
	24   120
	720 720

> (trace fact2 fact2.1)
> (fact2 6)
|(fact2 6)
|(fact2.1 6 1)
|(fact2.1 5 6)
|(fact2.1 3 120)
|(fact2.1 2 360)
|(fact2.1 1 720)
|(fact2.1 0 720)
|720
720

# fact2

- Interpreter & compiler note the last expression to be evaled & returned in fact2.1 is a recursive call
- Instead of pushing state on the sack, it reassigns the local variables and jumps to beginning of the procedure
- Thus, the recursion is automatically transformed into iteration

### **Reverse a list**

 This version works, but has two problems (define (rev1 list) ; returns the reverse a list (if (null? list)

empty

- (append (rev1 (rest list)) (list (first list))))))
- It is not tail recursive
- It creates needless temporary lists

#### A better reverse

(define (rev2 list) (rev2.1 list empty))

(define (rev2.1 list reversed) (if (null? list) reversed (rev2.1 (rest list) (cons (first list) reversed))))

#### > (load "reverse.ss") rev1 and rev2 > (trace rev1 rev2 rev2.1) > (rev1 '(a b c)) (rev1 (a b c)) > (rev2 '(a b c)) | (rev1 (b c)) (rev2 (a b c)) | |(rev1 (c)) (rev2.1 (a b c) ()) | | (rev1 ()) (rev2.1 (b c) (a)) |||()|(rev2.1 (c) (b a)) | |(c) (rev2.1 () (c b a)) | (c b) (c b a) |(c b a) (c b a) (c b a) >

## The other problem

- Append copies the top level list structure of it's first argument.
- (append '(1 2 3) '(4 5 6)) creates a copy of the list (1 2 3) and changes the last cdr pointer to point to the list (4 5 6)
- In reverse, each time we add a new element to the end of the list, we are (re-)copying the list.

# Append (two args only)

(define (append list1 list2) (if (null? list1) list2 (cons (first list1) (append (rest list1) list2))))

# Why does this matter?

- The repeated rebuilding of the reversed list is needless work
- It uses up memory and adds to the cost of garbage collection (GC)
- GC adds a significant overhead to the cost of any system that uses it
- Experienced programmers avoid algorithms that needlessly consume memory that must be garbage collected











#### Compare to an iterative version

- The tail recursive version passes the "loop variables" as arguments to the recursive calls
- It's just a way to do iteration using recursive functions without the need for special iteration operators



#### No tail call elimination in many PLs

- Many languages don't optimize tail calls, including C, Java and Python
- Recursion depth is constrained by the space allocated for the call stack
- This is a design decision that might be justified by the worse is better principle
- See Guido van Rossum's comments on TRE



#### Conclusion

- Recursion is an elegant and powerful control mechanism
- We don't need to use iteration
- We can eliminate any inefficiency if we Recognize and optimize tail-recursive calls, turning recursion into iteration
- Some languages (e.g., Python) choose not to do this, and advocate using iteration when appropriate
- But side-effect free programming remains easier to analyze and parallelize