Description Logics

What is **Description Logic**?

- A family of logic based KR formalisms
 - Descendants of <u>semantic networks</u> and <u>KL-ONE</u>
 - Describe domain in terms of concepts (classes), roles (relationships) and individuals
- Distinguished by:
 - Formal semantics (typically <u>model theoretic</u>) based on a <u>decidable</u> fragments of FOL
 - Provision of inference services
 - Sound and complete decision procedures for key problems
 - Implemented systems (highly optimized)
- Formal basis for OWL (DL profile)

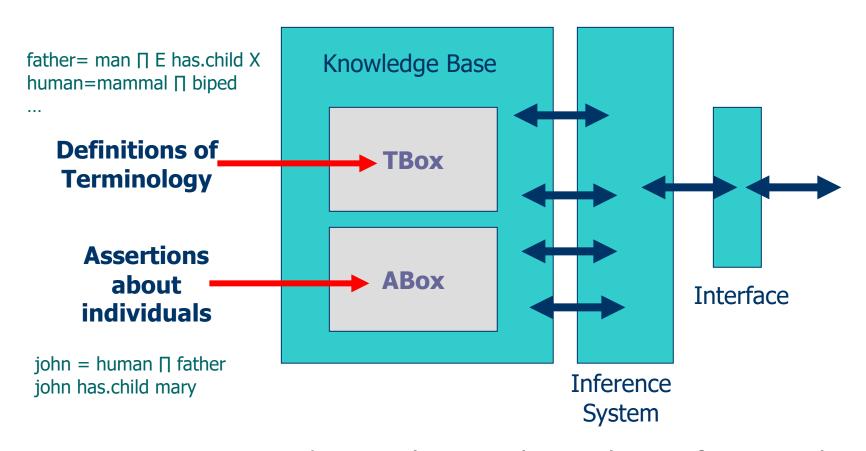
Informally, What is **Description Logic**?

- We define a concept using a simple noun phrase in a human language like English
 - A red car
 - A tall person who works for IBM
 - A tall person who works for a Bay-area Technology company
- E.g., we don't do this, using a set of rules
- Natural languages have multiple ways of attaching modifiers to a simple concept
 - E.g. adjectives, propositional phrases, clausal modifiers, connectives (and, or, not)
- Description logics, like OWL-DL, designed to define concepts in a similar way

DL Paradigm

- <u>Description Logic</u> characterized by a set of constructors that allow one to build complex descriptions or terms out of concepts and roles from atomic ones
 - Concepts: classes interpreted as sets of objects,
 - Roles: relations interpreted as binary relations on objects
- Set of axioms for asserting facts about concepts, roles and individuals

Typical Architecture



Division into TBox and ABox has no logical significance, but is made for conceptual and implementation convenience

DL defines a family of languages

- The expressiveness of a description logic is determined by the operators that it uses
 - Adding or removing operators (e.g., \neg , \cup) increases or decreases the kinds of statements expressible
 - Higher expressiveness usually means higher reasoning complexity
- AL or Attributive Language is the base and includes just a few operators
- Other DLs are described by the additional operators they include

AL: Attributive Language

Constructor	Syntax	Example
atomic concept	С	Human
atomic negation	~ C	~ Human
atomic role	R	hasChild
conjunction	$C \wedge D$	Human ∧ Male
value restriction	R.C	Human ∃ hasChild.Blond
existential rest. (lim)	∃ R	Human ∃ hasChild
Top (univ. conc.)	T	T
bottom (null conc)	上	上

for concepts C and D and role R

ALC

ALC is the smallest DL that is *propositionally closed* (i.e., includes full negation and disjunction) and include booleans (and, or, not) and restrictions on role values

constructor	Syntax	Example
atomic concept	C	Human
negation	~ C	~ (Human V Ape)
atomic role	R	hasChild
conjunction	C ^ D	Human ^ Male
disjunction	CVD	Nice V Rich
value restrict.	∃ R.C	Human ∃ hasChild.Blond
existential restrict.	∃ R.C	Human ∃ hasChild.Male
Top (univ. conc.)	Т	Т
bottom (null conc)	\perp	上

Examples of ALC concepts

- Person ∧ ∀hasChild.Male (everybody whose children are all male)
- Person ∧ ∀hasChild.Male ∧∃hasChild.T (everybody who has a child and whose children are all male)
- Living_being ∧ ¬Human_being (all living beings that are not human beings)
- Student ∧ ¬∃interestedIn.Mathematics (all students not interested in mathematics)
- Student ∧ ∀drinks.tea (all students who only drink tea)
- ∃hasChild.Male V ∀hasChild.⊥ (everybody who has a son or no child)

Other Constructors

The general DL model has additional constructors...

Constructor	Syntax	Example
Number restriction	>= n R	>= 7 hasChild
	<= n R	<= 1 hasmother
Inverse role	R-	haschild-
Transitive role	R*	hasChild*
Role composition	$R \circ R$	hasParent o hasBrother
Qualified # restric.	>= n R.C	>= 2 hasChild.Female
Singleton concepts	{ <name>}</name>	{Italy}

Special names and combinations

See http://en.wikipedia.org/wiki/Description_logic

- S = ALC + transitive properties
- H = role hierarchy, e.g., rdfs:subPropertyOf
- O = nominals, e.g., values constrained by enumerated classes (e.g., days of week), as in owl:oneOf and owl:hasValue
- I = inverse properties
- N = cardinality restrictions (owl:cardinality, maxCardonality)
- (D) = use of datatypes properties
- R = complex role axioms (e.g. (ir)reflexivity, disjointedness)
- Q = Qualified cardinality (e.g., at least two female children)
- → OWL-DL is SHOIN(D)
- → OWL 2 is SROIQ^(D)

Note: R->H and Q->N

Notes:

Complexity of reasoning in Description Logics Note: the information here is (always) incomplete and updated often

Base description logic: Attributive Language with Complements $\mathcal{ALC} := \bot \mid \mathsf{T} \mid \mathsf{A} \mid \neg \mathsf{C} \mid \mathsf{C} \cap \mathsf{D} \mid \mathsf{C} \cup \mathsf{D} \mid \exists \mathsf{R.C} \mid \forall \mathsf{R.C}$



Concept const	tructors:		Role constructors:	trans reg		
𝔻 - functionality ² : (≤1 R) 𝔻 - (unqualified) number restrictions: (≥n R), (≤n R) ā		R.C), (≤n R.C) e-of")	 ✓ - role inverse: R⁻ ○ ∩ - role intersection³: R ∩ S ○ ∪ - role union: R ∪ S ○ ¬ - role complement: ¬R full ÷ ○ o - role chain (composition): R o S ○ * - reflexive-transitive closure⁴: R* 			
Forbid ‡ complex roles ⁵ in number restrictions ⁶		uons=	□ id – concept identity: id(C)	12		
TBox (concept axioms): • empty TBox • acyclic TBox ($A \equiv C$, A is a concept name; no cycles) • general TBox ($C \subseteq D$, for arbitrary concepts C and D)			RBox (role axioms): $S - \text{role transitivity: } Tr(R)$ $H - \text{role hierarchy: } R \subseteq S$ $R - \text{complex role inclusions: } R \circ S \subseteq R, R \circ S \subseteq S$ $S - \text{some additional features (check it to see)}$	OWL-Lite OWL-DL OWL 1.1		
Reset	You	have selected a Description Log	ic: ACC			
	Complexity of reasoning problems ⁷					
Reasoning problem	Complexity ⁸	Comments and references				
Concept satisfiability	PSpace-complete	Hardness for ALC: see [80]. Upper bound for ALCQ: see [12, Theorem 4.6].				
ABox consistency	PSpace-complete	Hardness follows from that for concept satisfiability. Upper bound for ALCQO: see [17, Appendix A].				
		Important propertie	es of the description logic			
Finite model property	Yes	\mathcal{ALC} is a notational variant of the multi-modal logic \mathbf{K}_{m} (cf. [77]), for which the finite model property can be found in [4, Sect. 2.3].				
Tree model property	Yes	\mathcal{ALC} is a notational variant of the multi-modal logic $\mathbf{K_m}$ (cf. [77]), for which the tree model property can be found in [4, Proposition 2.15].				
Maintained by: E			Any comments are we	elcome:		

http://www.cs.man.ac.uk/~ezolin/dl/

OWL as a DL

- OWL-DL is SHOIN^(D)
- We can think of OWL as having three kinds of statements
- Ways to specify classes
 - the intersection of humans and males
- Ways to state axioms about those classes
 - Humans are a subclass of apes
- Ways to talk about individuals
 - John is a human, a male, and has a child Mary

Subsumption: $D \subseteq C$?

- Concept C subsumes D iff on every <u>interpretation</u> I
 I(D) ⊆ I(C)
- This means the same as $\forall (x)(D(x) \rightarrow C(x))$ for complex statements D & C
- Determining whether one concept logically contains another is called the subsumption problem.
- Subsumption is undecidable for reasonably expressive languages
 - e.g.; for FOL, subsumption means "does one FOL sentence imply another"
- and non-polynomial for fairly restricted ones

Other reasoning problems

These problems can be reduced to subsumption (for languages with negation) and to the satisfiability problem

- Concept satisfiability is C (necessarily) empty?
- Instance Checking Father(john)?
- **Equivalence** CreatureWithHeart ≡ CreatureWithKidney
- Disjointness
 C □ D
- **Retrieval** Father(X)? X = {john, robert}
- **Realization** X(john)? X = {Father}

Definitions

- A definition is a description of a concept or a relationship
- It is used to assign a meaning to a term
- In description logics, definitions use a specialized logical language
- Description logics are able to do limited reasoning about concepts defined in their logic
- One important inference is classification (computation of subsumption)

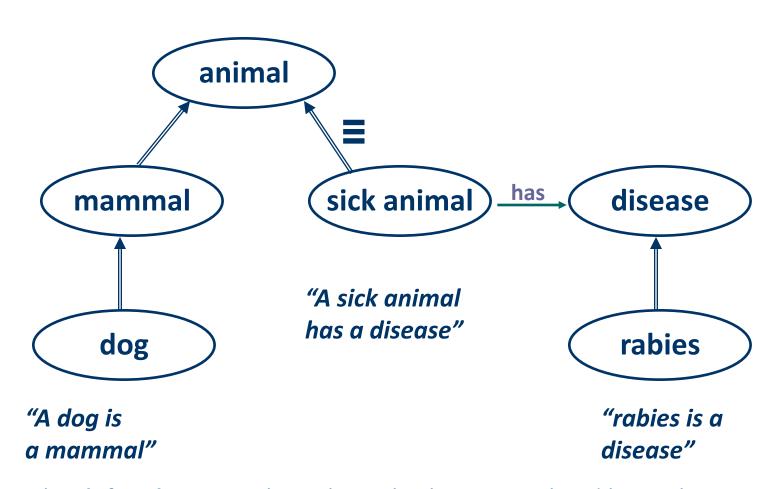
Necessary vs. Sufficient

- Necessary properties of an object are common to all objects of that type
 - Being a man is a necessary condition for being a father
- Sufficient properties allow one to identify an object as belonging to a type and need not be common to all members of the type
 - Speeding is a sufficient reason for being stopped by the police (but there are others!)
- Definitions typically specify both necessary and sufficient properties

Subsumption

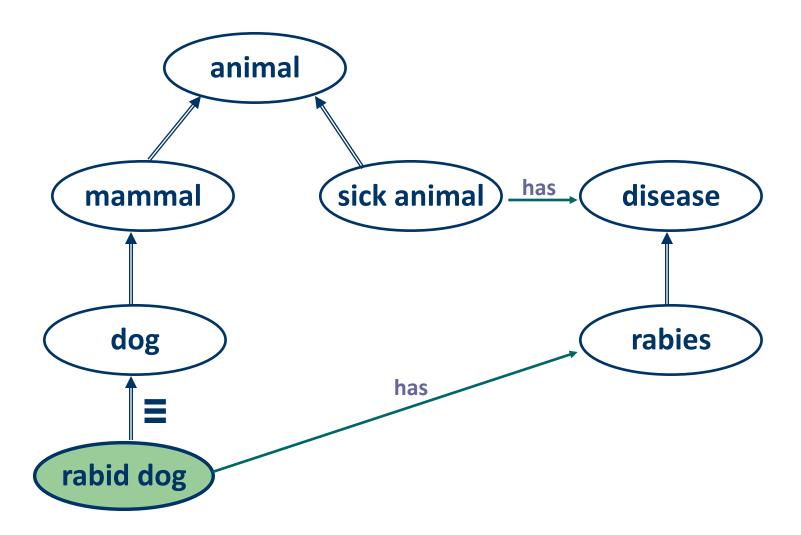
- Meaning of Subsumption
 - A more general concept/description **subsumes** a more specific one. Members of a subsumed concept are necessarily members of a subsuming concept
- Example: Animal subsumes Person; (aka IS-A, rdfs:subClassOf)
- Two ways to formalize meaning of subsumption
 - Using logic: satisfying a subsumed concept implies that the subsuming concept is satisfied also
 - E.g., if john is a person, he is also an animal
 - Using set theory: instances of subsumed concept are necessarily a subset of subsuming concept's instances
 - E.g., the set of all persons is a subset of all animals

How Does Classification Work?



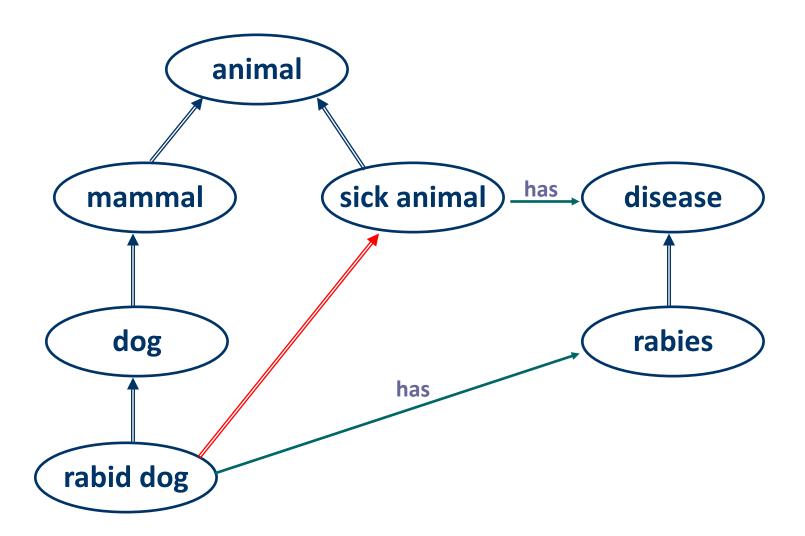
A sick animal is **defined** as something that is both an animal and has at least one thing that is a kind of a disease

Defining a "rabid dog"



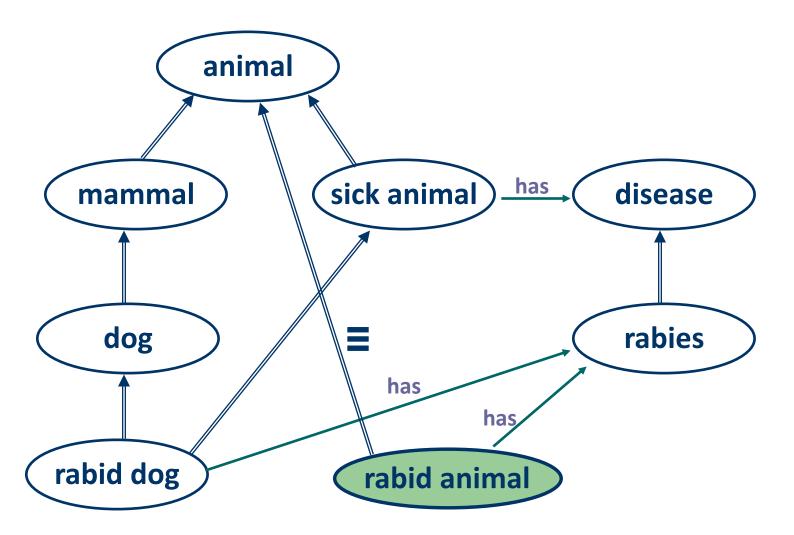
The **rabid dog** cocept is **defined** as something that is both a dog and has rabies

Classification as a "sick animal"



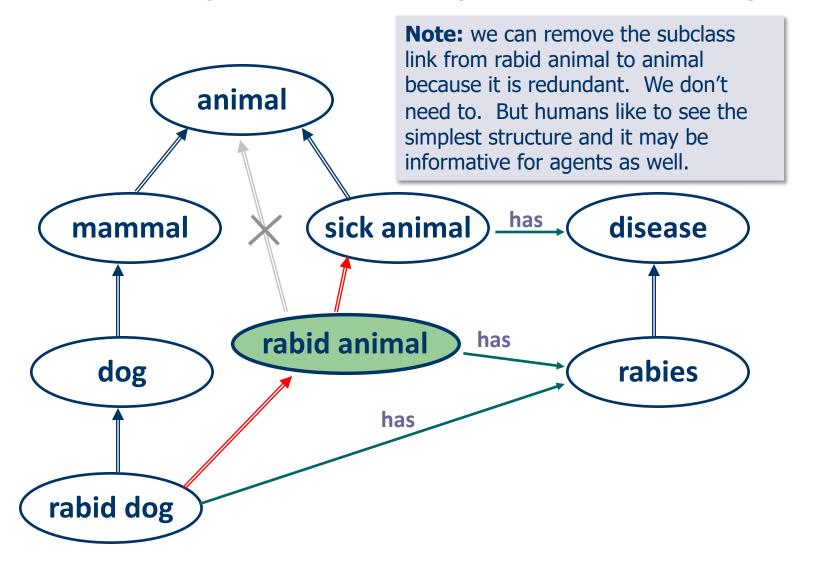
We can easily prove that s rabid dog is a kind of sick animal

Defining "rabid animal"



the **rabid animal** concept is **defined** as something that is both an animal and has rabies

DL reasoners places concepts in hierarchy



We can easily prove that s rabid dog is a kind of rabid animal

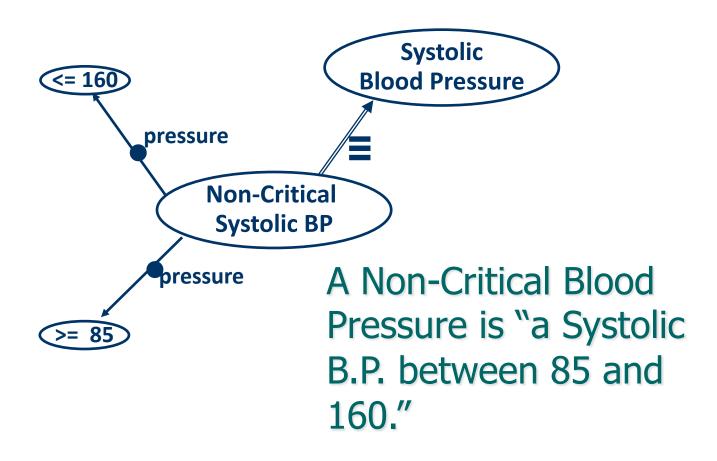
Primitive versus Structured (Defined)

- Description logics reason with definitions
 - They prefer to have complete descriptions
 - A complete definition includes both necessary conditions and sufficient conditions
- Often impractical or impossible, especially with natural kinds
- A "primitive" definition is an incomplete one
 - Limits amount of classification that can be done automatically
- Example:
 - Primitive: a Person
 - Defined: Parent = Person with at least one child

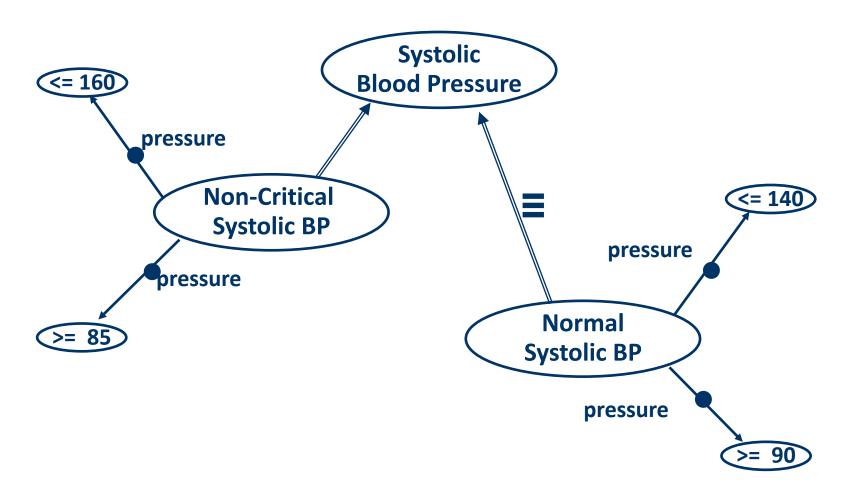
Classification is very useful

- Classification is a powerful kind of reasoning that is very useful
- Many expert systems can be usefully thought of as doing "heuristic classification"
- Logical classification over structured descriptions and individuals is also quite useful
- But... can classification ever deduce something about an individual other than what classes it belongs to?
- And what does *that* tell us?

Example: Blood Pressure

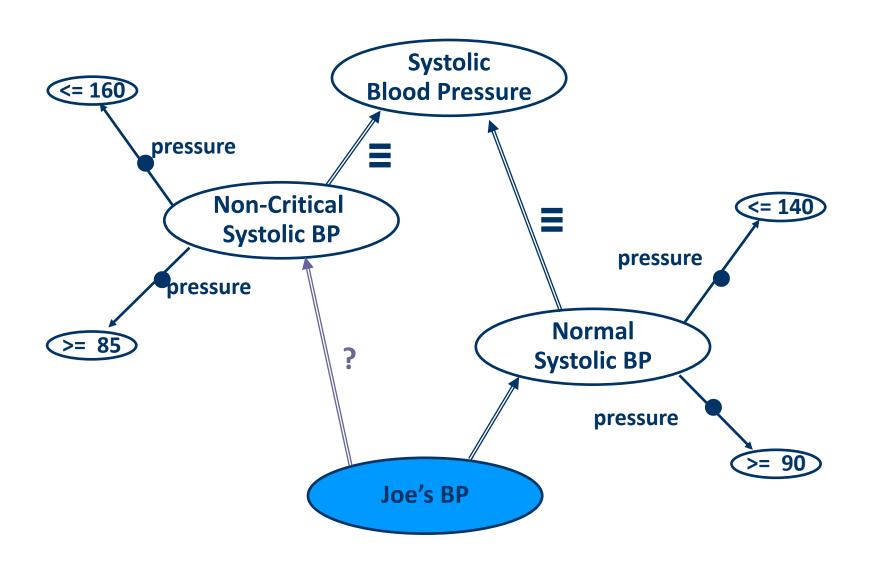


Example: Blood Pressure

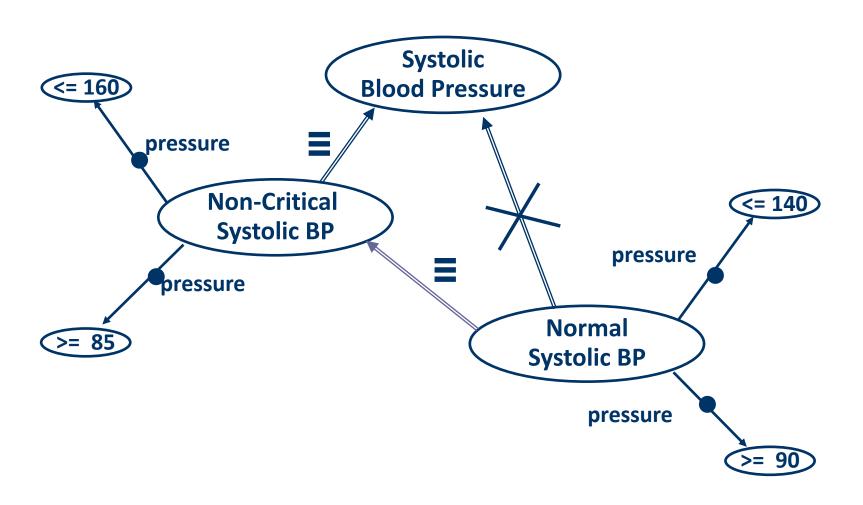


Normal Systolic B.P. is "a Systolic B.P. between 90 and 140.

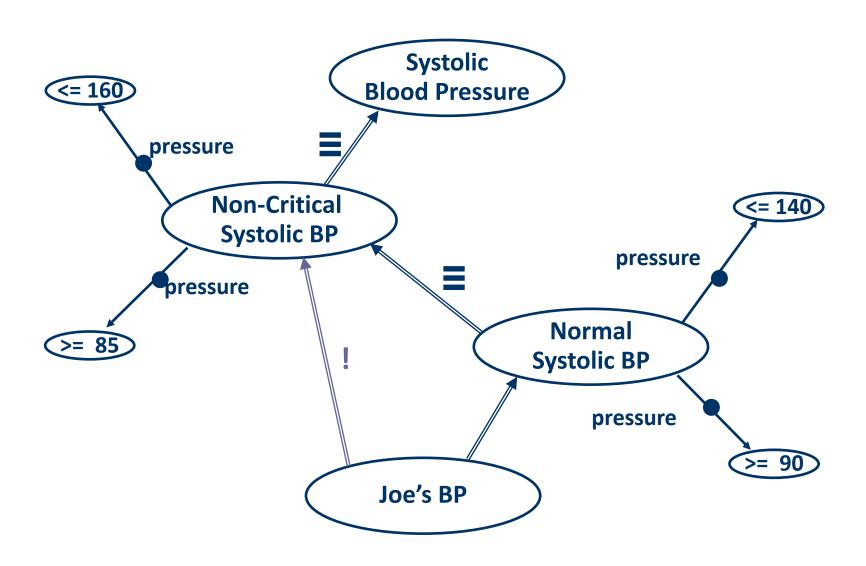
If Joe's BP is Normal is it also Non-Critical?



Concept Classification Infers Normal BP is Subsumed by Non-Critical BP



With Classified Concepts the Answer is Easy to Compute



Incidental properties

- We can consider properties that are not part of any definition to be incidental
- Classification based on non-incidental properties allow the inference of incidental properties
- Examples:
 - E.g., red cars have been observed to have a high accident rate by insurance companies
 - Birds weighing more than 25kg can not fly
 - People with non-critical blood pressure require no medication

DL Conclusion

- Description logic was the model for OWL reasoning
- More expressive than rule-based systems without being undecidable or intractable
- It can reason over general statements (e.g., a dog with rabies is a sick animal), unlike most rule-based systems
- It still has limitations tho...