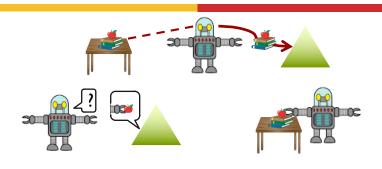
# Knowledge-Based Agents and Propositional Logic (Ch. 7)



Some material adopted from notes by Andreas Geyer-Schulz and Chuck Dyer

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#### Bookkeeping

- HW3 due Friday at 11:59 PM
  - Reminder: if Blackboard says it's late, it will be marked late
  - Please feel free to submit early!
- · If you missed class Tuesday, please collect your exam

#### Today's Class

- · Knowledge Based Agents
  - · Knowledge Bases
  - Inference
- The Wumpus
  - · A simple case that we can do a lot with using logic
- Inferential Logics
  - Propositional (Boolean) Logic: a Refresher
  - · Logic in general models and entailment
  - Equivalence, validity, satisfiability
  - · Inference rules and theorem proving

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#### **Logical Agents**

- Knowledge-based agents agents that have an explicit representation of knowledge that can be reasoned with
  - We refer to the set of represented knowledge as a "knowledge base"
    - · For historical reasons, KBs are always shown as triangles
- These agents can manipulate this knowledge to infer new things at the "knowledge level"



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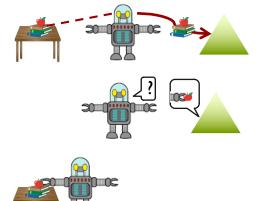
#### A Knowledge-Based Agent

- A knowledge-based agent includes (at least):
  - A knowledge base
  - An inference system
- A knowledge base (KB) is a set of representations of facts about the world
- Each individual representation is a sentence or assertion
- Expressed in a knowledge representation language
  - Usually starts with some background knowledge
    - Can be general (world knowledge) or specific (domain language)

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#### A Knowledge-Based Agent

- Operates as follows:
  - 1. TELLs the knowledge base what it perceives.
    - ("asserts" knowledge into the KB)
  - **2. ASKs** the knowledge base what action to perform.
    - (performs "inference")
  - 3. **PERFORMs** the chosen action.



#### A simple knowledge-based agent must...

- Represent states, actions, etc.
- Incorporate new percepts
- Update internal representations of the world
- Deduce hidden properties of the world
- Deduce appropriate actions

```
function KB-AGENT( percept) returns an action
static: KB, a knowledge base
t, a counter, initially 0, indicating time

Tell(KB, Make-Percept-Sentence( percept, t))
action ← ASK(KB, Make-ACTION-QUERY(t))

Tell(KB, Make-ACTION-Sentence(action, t))
t←t+1
return action
```

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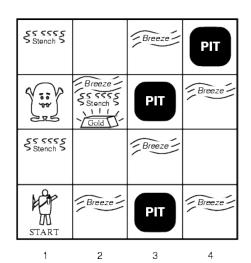
#### Architecture of a Knowledge-Based Agent

- Knowledge Level
  - · The most abstract level
  - Describe agent by saying what it knows
    - Example: A taxi agent might know that the Golden Gate Bridge connects San Francisco with the Marin County.
- Logical Level
  - Level at which knowledge is encoded into sentences.
    - Example: Links(GoldenGateBridge, SanFrancisco, MarinCounty)
- Implementation Level
  - The physical representation of the sentences in the logical level.
    - Example:

```
'(links goldengatebridge sanfrancisco marincounty)'
```

#### The Wumpus World Environment

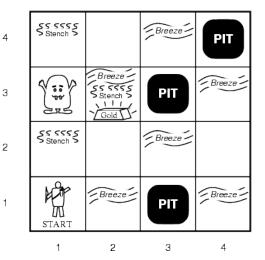
- The Wumpus computer game
  - Agent explores a dark cave consisting of rooms connected by passageways.
  - Lurking somewhere in the cave is the Wumpus, a beast that eats any agent that enters its room.
  - Some rooms contain bottomless pits that trap any agent that wanders into the room.
  - Occasionally, there is a heap of gold in a room.
  - The goal is to collect the gold and exit the world without being eaten (or trapped).



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#### A Typical Wumpus World

- The agent always starts in the field [1,1].
- The task of the agent is to find the gold, return to the field [1,1] and climb out of the cave.



#### **Wumpus Goal**

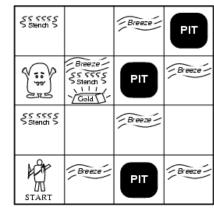
- Agent's goal is to:
  - Find the gold
  - Bring it back to the start square as quickly as possible
  - · Don't get killed
- Scoring
  - 1000 points reward for climbing out with the gold
  - 1 point deducted for every action taken
  - 1000 points penalty for getting killed
- Principle Difficulty: agent is initially ignorant of the configuration of the environment – going to have to reason to figure out where the gold is without getting killed!

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#### Wumpus World PEAS description

- · Performance measure
  - gold +1000, death -1000
  - -1 per step, -10 for using the arrow
- Environment: 4 x 4 grid of rooms
  - Squares adjacent to wumpus are smelly
  - Squares adjacent to pit are breezy
  - Glitter iff gold is in the same square
  - Shooting kills wumpus if you are facing it
  - · Shooting uses up the only arrow
  - Grabbing picks up gold if in same square
  - Releasing drops the gold in same square



1 2 3 4

- Sensors: Stench, Breeze, Glitter, Bump, Scream (shot Wumpus)
- Actuators: Left turn, Right turn, Forward, Grab, Release, Shoot

#### Wumpus world characterization

- Fully Observable?
- Deterministic?
- · Episodic?
  - In an episodic environment, only the current percept is required
  - In a sequential environment, an agent requires memory of past actions to determine the next best actions
- Static?
- Discrete?
- Single-agent?

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#### Wumpus world characterization

- Fully Observable? No only local perception
- Deterministic? Yes outcomes exactly specified
- Episodic? No sequential at the level of actions
  - In an episodic environment, only the current percept is required
  - In a sequential environment, an agent requires memory of past actions to determine the next best actions
- Static? Yes Wumpus and Pits do not move
- Discrete? Yes
- Single-agent? Yes Wumpus is essentially a natural feature

#### Agent in a Wumpus World: Percepts

- · Agent perceives
  - Stench in the square containing the wumpus and in adjacent squares (not diagonally)
  - Breeze in the squares adjacent to a pit
  - · Glitter in the square where the gold is
  - **Bump**, if it walks into a wall
  - Woeful scream everywhere in the cave, if the wumpus is killed
- The percepts are given as a five-symbol list.
- If there is a stench and a breeze, but no glitter, no bump, and no scream, the percept is:

```
[Stench, Breeze, None, None, None]
```

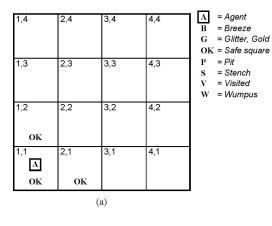
• The agent cannot perceive its own location (have to remember over time)

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#### **Wumpus Agent Actions**

- go forward
- turn right 90 degrees
- turn left 90 degrees
- grab: Pick up an object that is in the same square as the agent
- shoot: Fire an arrow in a straight line in the direction the agent is facing.
  - The arrow continues until it either hits and kills the wumpus or hits the outer wall.
  - The agent has only one arrow, so only the first Shoot action has any effect
- climb: leave the cave. This action is only effective in the start square
- **die**: This action automatically happens if the agent enters a square with a pit or a live wumpus

#### **Exploring the Wumpus World**



**Initial situation:** A = Agent B = Breeze

= Glitter, Gold

= Pit

= Stench

= Visited

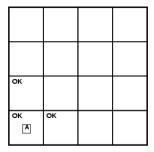
Agent in 1,1 and percept is [None, None, None, None, None]

From this the agent can infer the neighboring squares are safe (otherwise there would be a breeze or a stench)

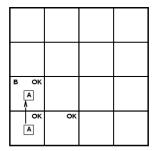
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#### Exploring a wumpus world



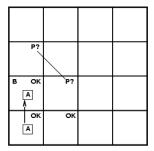
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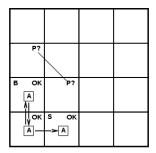
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## Exploring a wumpus world



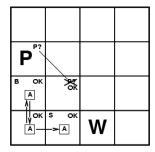
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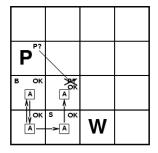
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## Exploring a wumpus world



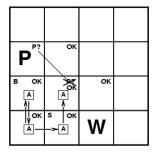
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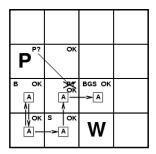
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## Exploring a wumpus world



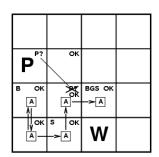
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#### Exploring a wumpus world



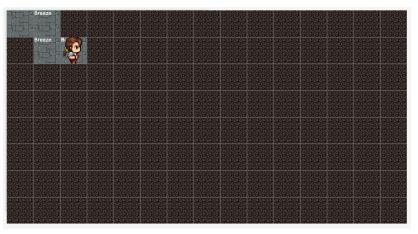
In each case where the agent draws a conclusion from the available information, that conclusion is guaranteed to be correct if the available information is correct...

This is a fundamental property of logical reasoning

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#### **Wumpuses Online**

- Google "Hunt the Wumpus" and you will find many playable versions
- There are many variations (multiple gold, bats, multiple arrows, ...)

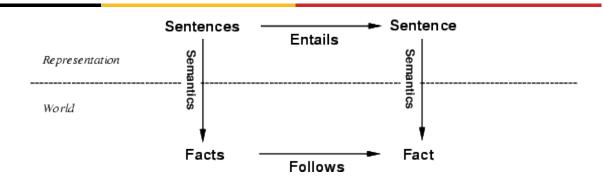


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#### Representation, Reasoning, and Logic

- Point of knowledge representation is to express knowledge in a computer usable form
  - Needed for agents to act on it!
- Logics are formal languages for representing information such that conclusions can be drawn
- **Syntax** defines how symbols can be put together to form the sentences in the language
- Semantics define the "meaning" of sentences;
  - i.e., define truth of a sentence in a world (given an interpretation)
- Knowledge is stored in a Knowledge Base, or KB

#### The Connection Between Sentences and Facts



Semantics maps sentences in logic to facts in the world. The property of one fact following from another is mirrored by the property of one sentence **being entailed** by another.

"Dr M is sick with the flu" ⊨ "Dr M is sick"

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#### Entailment

- Entailment means that one thing follows logically from another:
  - KB ⊨ α
  - Knowledge base KB entails sentence  $\alpha$  if and only if  $\alpha$  is true in all worlds where KB is true
  - E.g., the KB containing "the Phillies won and the Astros won" entails "The Phillies won"
- Inference is a procedure that allows new sentences to be derived from a knowledge base.
  - KB ⊢ α
  - E.g., from the KB containing "the Phillies won" and "Dr. M will be happy if the Phillies win," we can infer "Dr. M is happy"

Some slide material: www.eecis.udel.edu/~mccoy/courses/cisc4-681.10f/lec-materials/Chapt7-7.4+Logical-Agents.pp

#### **Entailment and Derivation**

#### • Entailment: KB ⊨ Q

- Q is entailed by KB (a set of premises or assumptions) if and only if there is no logically possible world in which Q is false while all the premises in KB are true.
- Or, stated positively, Q is entailed by KB if and only if the conclusion is true in every logically possible world in which all the premises in KB are true.

#### Derivation: KB ⊢ Q

 We can derive Q from KB if there is a proof consisting of a sequence of valid inference steps starting from the premises in KB and resulting in Q  $x \models y$ : x semantically entails y

 $x \vdash y$ : y is provable from x

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# Logic as a KR Language Multi-valued Logic Probabilistic Logic First Order Fuzzy Logic Propositional Logic Propositional Logic

#### Ontology and Epistemology

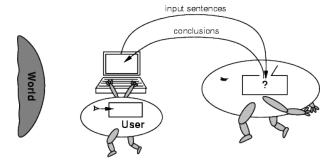
- Ontology is the study of what there is—an inventory of what exists. An ontological commitment is a commitment to an existence claim.
  - Knowledge bases with certain characteristics are called **ontologies**.
- Epistemology is a major branch of philosophy that concerns the forms, nature, and preconditions of knowledge.

Language	Ontological Commitment (What exists in the world)	Epistemological Commitment (What an agent believes about facts)
Propositional logic	facts	true/false/unknown
First-order logic	facts, objects, relations	true/false/unknown
Temporal logic	facts, objects, relations, times	true/false/unknown
Probability theory	facts	degree of belief 0 1
Fuzzy logic	degree of truth	degree of belief 0 1

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#### No Independent World Access

- The reasoning agent often gets its knowledge about the facts of the world as a sequence of logical sentences.
- Must draw conclusions from them without (other) access to the world.
- Thus it is very important that the agent's reasoning is sound!



#### KBs allow reasoning about actions

- Agents have a knowledge base that contains everything they know about the world
  - Including goals and possible actions
  - · Updated when new percepts arrive from sensors
  - Stored as logical sentences: (haveColor redColor apples)
- Inference can be used to work out new facts about the world
  - · When new facts come in, can conclude new things
  - Based on that knowledge, make decisions about what to do
- Knowledge underpins decisions about what actions to take

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#### **KB Agents - Summary**

- Intelligent agents need knowledge about the world for making good decisions
- The knowledge of an agent is stored in a knowledge base in the form of sentences in a knowledge representation language
- A knowledge-based agent needs a knowledge base and an inference mechanism
  - It operates by storing sentences in its knowledge base, inferring new sentences with the inference mechanism, and using them to deduce which actions to take
- A representation language is defined by its syntax and semantics, which specify structure of sentences and how they relate to world facts
- The **interpretation** of a sentence is the fact to which it refers. If this fact is part of the actual world, then the sentence is true

## **Propositional Logic**

Chapter 7.4-7.8

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#### **Propositional Logic**

- Logical constants: true, false
- Propositional symbols: P, Q, S, ... (atomic sentences)
- Wrapping parentheses: ( ... )
- Sentences are atoms combined by connectives:
  - \( \Lambda \) ...and [conjunction] \( \V \) ...or [disjunction]
  - ⇒ ...implies [implication / conditional]
  - ⇔ ...is equivalent [biconditional] ¬ ...not [negation]
- Literal: atomic sentence or negated atomic sentence

#### Propositional Logic (PL)

- · A simple language useful for showing key ideas and definitions
- User defines a set of propositional symbols, like P and Q.
- User defines the semantics of each propositional symbol:
  - Ho means "It is hot"
  - Hu means "It is humid"
  - R means "It is raining"
- · Combinations of propositional symbols yield logical expressions

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#### Propositional logic: Syntax

- Propositional logic is the simplest logic illustrates basic ideas
  - If S is a sentence,  $\neg$ (S) is a sentence (negation)
  - If S1 and S2 are sentences, (S1 ∧ S2) is a sentence (conjunction)
  - If S1 and S2 are sentences, (S1 ∨ S2) is a sentence (disjunction)
  - If S1 and S2 are sentences, (S1  $\Rightarrow$  S2) is a sentence (implication)
  - If S1 and S2 are sentences, (S1 ⇔ S2) is a sentence (biconditional)

#### Propositional logic: Semantics

- Each model specifies true/false for each proposition symbol
- Rules for evaluating truth with respect to a set of t/f values for sentences:

```
\neg \mathsf{S}
                 is true iff S is false
S1 ∧ S2
                is true iff S1 is true
                                                            S2 is true
                                                   and
S1 ∨ S2
                is true iff S1 is true
                                                   or
                                                            S2 is true
                is true iff S1 is false
S1 \Rightarrow S2
                                                            S2 is true
                                                   or
                is true iff S1⇒S2 is true
S1 ⇔ S2
                                                   and
                                                           S2⇒S1 is true
```

- Simple recursive process evaluates an arbitrary sentence, e.g.,
  - $\neg P_{1,2} \wedge (P_{2,2} \vee P_{3,1}) = \text{true} \wedge (\text{true} \vee \text{false}) = \text{true} \wedge \text{true} = \text{true}$

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#### **Examples of PL Sentences**

- $(P \land Q) \Rightarrow R$ : "If it is hot and humid, then it is raining"
- $Q \Rightarrow P$  : "If it is humid, then it is hot"
- Q : "It is humid."
- A better way:
  - Ho = "It is hot"
  - Hu = "It is humid"
  - R = "It is raining"
- (Ho  $\wedge$  Hu)  $\Rightarrow$  R; Hu  $\Rightarrow$  Ho; Hu

#### Validity and Satisfiability

- A sentence is valid if it is true in all models
  - Ex: True, AV $\neg$ A, A  $\Rightarrow$  A, (A $\land$ (A  $\Rightarrow$  B))  $\Rightarrow$  B
- A sentence is satisfiable if it is true in some model
  - Ex: A V B, C
- A sentence is unsatisfiable if it is true in no models
  - Ex: A ∧ ¬A

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#### Some Terms

- The meaning or **semantics** of a sentence determines its **interpretation**.
- Given the **truth values** of all symbols in a sentence, it can be "evaluated" to determine its truth value (True or False).
- A **model** for a KB is a "possible world" (assignment of truth values to propositional symbols) in which each sentence in the KB is True.
  - E.g.: it is both hot and humid.

#### More Terms

- A valid sentence or tautology is a sentence that is True under all interpretations, no matter what the world is actually like or what the semantics is.
  - Example: "It's raining or it's not raining."
- An **inconsistent sentence** or **contradiction** is a sentence that is False under all interpretations. The world is never like what it describes.
  - · Example: "It's raining and it's not raining."
- P semantically entails Q, written P ⊨ Q, means that whenever P is True, so is Q. In other words, all models of P are also models of Q.

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#### Wumpus world sentences

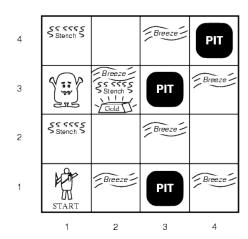
Let P<sub>i,j</sub> be true if there is a pit in [i, j];
 Let B<sub>i,j</sub> be true if there is a breeze in [i, j].

$$\neg P_{1,1}$$
  $\neg B_{1,1}$ 

 $B_{2,1}$ 

"Pits cause breezes in adjacent squares"

$$\begin{split} B_{1,1} & \Leftrightarrow & (P_{1,2} \vee P_{2,1}) \\ B_{2,1} & \Leftrightarrow & (P_{1,1} \vee P_{2,2} \vee P_{3,1}) \end{split}$$



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#### Inference Rules

- Logical inference is used to create new sentences that logically follow from a given set of predicate calculus sentences (KB).
- An inference rule is sound if every sentence X produced by an inference rule operating on a KB logically follows from the KB.
  - (That is, the inference rule does not create any contradictions)
- An inference rule is **complete** if it is able to produce every expression that logically follows from (is entailed by) the KB.
  - (Note the analogy to complete search algorithms.)

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#### Two Important Properties for Inference

- Soundness: If KB ⊢ Q then KB ⊨ Q
  - If Q is derived from a set of sentences KB using a given set of rules of inference, then Q is entailed by KB.
  - Hence, inference produces only real entailments, or any sentence that follows deductively from the premises is valid.
- Completeness: If  $KB \models Q$  then  $KB \vdash Q$ 
  - If Q is entailed by a set of sentences KB, then Q can be derived from KB using the rules of inference.
  - Hence, inference produces all entailments, or all valid sentences can be proved from the premises.

#### Sound Rules of Inference

- Here are some examples of sound rules of inference
  - A rule is sound if its conclusion is true whenever the premise is true
- · Each can be shown to be sound using a truth table

RULE	PREMISES	CONCLUSION
Modus Ponens	$A, A \Rightarrow B$	В
And Introduction	А, В	$A \wedge B$
And Elimination	$A \wedge B$	Α
Double Negation	¬ ¬A	Α
Unit Resolution	A ∨ B, ¬B	Α
Resolution	A∨B, ¬B∨C	AVC
de Morgans	¬(A ∨ B)	¬A ∧ ¬B
V/ ⇒ Equivalence	$A \Rightarrow B$	¬A V B

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#### Soundness of Modus Ponens

• If A and A  $\Rightarrow$  B; then B

A	В	$A \rightarrow B$	$OK?$ $(A \land (A \rightarrow B)) \rightarrow B$
True	True	True	
True	False	False	<b>✓</b>
False	True	True	<b>✓</b>
False	False	True	<b>✓</b>

#### Soundness of the Resolution Inference Rule

•  $(\alpha \vee \beta) \wedge (\neg \beta \vee \gamma) \rightarrow (\alpha \vee \gamma)$ 

α .	3	2	αVB	$\neg 3 \lor \gamma$	ανη
False	False	False	False	True	False
False	False	True	False .	True	True
False	True	False	True	False	False
False :	<u>True</u>	<u>True</u>	<u>True</u>	<u>True</u>	True
True	False	<u>False</u>	<u>True</u>	<u>True</u>	True
True	False	True	<u>True</u>	<u>True</u>	True
True	True	False	True	False	True
True	True	<u>True</u>	True	<u>True</u>	True

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#### **Proving Things**

- A proof is a sequence of sentences, where each sentence is either a premise or a sentence derived from earlier sentences in the proof by one of the rules of inference.
- The last sentence is the theorem (also called goal or query) that we want to prove.
- Example for the "weather problem" given above: Is it raining (R=true), given Hu?

I. Hu	Premise	it is numia
2. Hu ⇒ Ho	Premise	"If it is humid, it is hot"
3. Ho	Modus Ponens(1,2)	"It is hot"
4. (Ho $\wedge$ Hu) $\Rightarrow$ R	Premise	"If it's hot & humid, it's raining"
5. Ho ∧ Hu	And Introduction(1,3)	"It is hot and humid"
6. R	Modus Ponens(4,5)	"It is raining"

#### Logical equivalence

• Two sentences are logically equivalent iff true in same models:  $\alpha \equiv \beta$  iff  $\alpha \models \beta$  and  $\beta \models \alpha$ 

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#### Horn Sentences

- A Horn sentence or Horn clause has the form:
   P1 ∧ P2 ∧ P3 ... ∧ Pn ⇒ Q
- or alternatively
   ¬P1 V ¬P2 V ¬P3 ... V ¬Pn V Q

- $(P \to Q) = (\neg P \lor Q)$
- · ...where Ps and Q are non-negated atoms
- To get a proof for Horn sentences, apply Modus Ponens repeatedly until nothing can be done
- We will use the Horn clause form later

#### Propositional Logic is a Weak Language

- Hard to identify "individuals" (e.g., Mary, 3)
- Can't directly talk about properties of individuals or relations between individuals (e.g., "Bill is tall")
- Generalizations, patterns, regularities can't easily be represented (e.g., "all triangles have 3 sides")
- First-Order Logic (abbreviated FOL or FOPC) is expressive enough to concisely represent this kind of information
- FOL adds relations, variables, and quantifiers, e.g.,
  - "Every elephant is gray":  $\forall x \text{ (elephant}(x) \Rightarrow \text{gray}(x))$
  - "There is a white alligator": ∃x (alligator(X) ∧ white(X))

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#### Example

- Consider the problem of representing the following information:
  - Every person is mortal.
  - Confucius is a person.
  - Confucius is mortal.
- How can these sentences be represented so that we can infer the third sentence from the first two?

#### Example II

In PL we have to create propositional symbols to stand for all or part of each sentence. For example, we might have:

```
P = "person"; Q = "mortal"; R = "Confucius"
```

so the above 3 sentences are represented as:

$$P \Rightarrow Q; R \Rightarrow P; R \Rightarrow Q$$

- Although the third sentence is entailed by the first two, we needed an explicit symbol, R, to represent an individual, Confucius, who is a member of the classes "person" and "mortal"
- To represent other individuals we must introduce separate symbols for each one, with some way to represent the fact that all individuals who are "people" are also "mortal"

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#### The "Hunt the Wumpus" Agent

Some atomic propositions:

S12 = There is a stench in cell (1,2)

B34 = There is a breeze in cell (3,4)

W13 = The Wumpus is in cell (1,3)

V11 = We have visited cell (1,1)

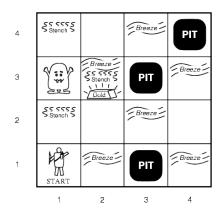
OK11 = Cell (1,1) is safe.

etc

Some rules:

(Rule 1)  $\neg S11 \rightarrow \neg W11 \land \neg W12 \land \neg W21$  $\neg \$21 \rightarrow \neg \$11 \land \neg \$21 \land \neg \$22 \land \neg \$31$ 

(Rule 3)  $\neg$ S12  $\rightarrow$   $\neg$ W11  $\land$   $\neg$  W12  $\land$   $\neg$  W22  $\land$   $\neg$  W13 (Rule 4) S12  $\rightarrow$  W13  $\lor$  W12  $\lor$  W22  $\lor$  W11



Note that the lack of variables requires us to give similar rules for each cell

#### YOUR MISSION

 Prove that the Wumpus is in (1,3) and there is a pit in (3,1), given the observations shown and these rules:

#### Rules

- If there is no stench in a cell, then there is no wumpus in any adjacent cell
- If there is a stench in a cell, then there is a wumpus in some adjacent cell
- If there is no breeze in a cell, then there is no pit in any adjacent cell
- If there is a breeze in a cell, then there is a pit in some adjacent cell
- If a cell has been visited, it has neither a wumpus nor a pit
- FIRST write the propositional rules for the relevant cells
- NEXT write the proof steps and indicate what inference rules you used in each step

#### Prove it!

A = Agent
B = Breeze
G = Glitter, Gold
OK = Safe square
P = Pit
S = Stench

V = Visited W = Wumpus

V12 S12 -B12	V22 -S22 -B22	
V11 -S11 -B11	V21 B21 -S21	

#### INFERENCE RULES

Modus Ponens  $A, A \rightarrow B$ 

ergo B

And Introduction

A, B

 $ergo\:A\wedge B$ 

And Elimination

 $\boldsymbol{A} \wedge \boldsymbol{B}$ 

ergo A Double Negation

 $\neg \neg A$ 

ergo A

Unit Resolution  $A \lor B, \neg B$ 

 $A \lor B, \neg B$  ergo A

Resolution

 $A \lor B, \neg B \lor C$  ergo  $A \lor C$ 

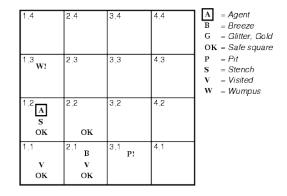
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#### Proving W<sub>13</sub>

- Apply MP with ¬S11 and Rule 1:
  - $\neg$  W11  $\land$   $\neg$  W12  $\land$   $\neg$  W21
- Apply And-Elimination to this, yielding three sentences:
  - ¬ W11, ¬ W12, ¬ W21
- Apply MP to ~S21 and Rule 2, then apply And-Elimination:
   ¬ W22, ¬ W21, ¬ W31
- Apply MP to S12 and Rule 4 to obtain:
  - W13 \lefty W12 \lefty W22 \lefty W11
- Apply Unit Resolution on (W13  $\vee$  W12  $\vee$  W22  $\vee$  W11) and  $\neg$ W11: W13  $\vee$  W12  $\vee$  W22
- Apply Unit Resolution with (W13  $\vee$  W12  $\vee$  W22) and  $\neg$ W22: W13  $\vee$  W12
- Apply UR with (W13  $\vee$  W12) and  $\neg$ W12: W13
- QED

#### After the Third Move

- We can prove that the Wumpus is in (1,3) using the four rules given.
- See R&N section 7.5



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#### Problems with the Propositional Wumpus Hunter

- · Lack of variables prevents stating more general rules
  - We need a set of similar rules for each cell
- · Change of the KB over time is difficult to represent
  - Standard technique is to index facts with the time when they're true
  - This means we have a separate KB for every time point

#### Summary: Knowledge-Based Agents

- Knowledge-based agents use a knowledge base to store everything they know about the world
  - Everything is represented as sentences in that KB
- As they learn more about the world, they make changes to the KB
  - Add and delete facts based on percepts and reasoning
- They use inference over represented sentences to perform reasoning
  - · Requires the use of an inference engine
  - You can draw conclusions from facts and rules by proving new sentences
- Simplest kind of logic that we'll see is propositional logic
  - It works, but lacks certain capabilities that would be useful

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#### Summary: Inference

- The process of deriving new sentences from old ones is called inference.
  - Sound inference processes derives true conclusions given true premises
  - Complete inference processes derive all true conclusions from a set of premises
- A valid sentence is true in all worlds under all interpretations
- If an implication sentence (rule) can be shown to be valid, then—given its premise—its consequent can be derived
- Different logics make different commitments about what the world is made of and what kind of beliefs we can have regarding the facts
  - Logics are useful for the commitments they do not make because lack of commitment gives the knowledge base engineer more freedom
- Propositional logic commits only to the existence of facts that may or may not be the case in the world being represented
  - · It has a simple syntax and simple semantics. It suffices to illustrate the process of inference
  - · Propositional logic quickly becomes impractical, even for very small worlds