





#### Admissibility and Optimality

- Intuitively:
  - When A\* finds a path of length k, it has already tried every other path which can have length ≤ k
  - Because all frontier nodes have been sorted in ascending order of f(n)=g(n)+h(n)
- Does an admissible heuristic guarantee optimality for greedy search?
- Reminder: f(n) = h(n), always choose node "nearest" goal
- · No sorting beyond that









# Iterative Improvement Search

- Start with an initial guess
- · Gradually improve it until it is legal or optimal
- Some examples:
- Hill climbing
- Simulated annealing
- Constraint satisfaction



#### Hill Climbing Search

- If there exists a successor *s* for the current state *n* such that

  - h(s) > h(n) $h(s) >= h(t) \text{ for all the successors } t \text{ of } n, \\ then move from$ *n*to*s*. Otherwise, halt at*n*.
  - Look one step ahead to determine if any successor is "better" than current state If so, move to the best successor
- A kind of Greedy search in that it uses hBut, does not allow backtracking or jumping to an alternative path Doesn't "remember" where it has been.
- Not complete
- Search will terminate at local minima, plateaux, ridges.





# Drawbacks of Hill Climbing Problems: local maxima, plateaus, ridges Remedies: Random restart: keep restarting the search from random locations until a goal is found. Problem reformulation: reformulate the search space to eliminate these problematic features Some problem spaces are great for hill climbing; others are terrible



#### Some Extensions of Hill Climbing

- · Simulated Annealing
- Escape local maxima by allowing *some* "bad" moves but gradually decreasing their frequency
- Local Beam Search
  - Keep track of *k* states rather than just one
  - At each iteration:
  - All successors of the k states are generated and evaluated
  - Best *k* are chosen for the next iteration











#### Simulated Annealing (IV)

- *f*(*s*) represents the quality of state *n* (high is good)
- A "bad" move from A to B is accepted with a probability  $T_{A}^{(f)}$

 $P(move_{A \rightarrow B}) \approx e^{(f(B) - f(A)) / T}$ 

- (Note that f(B) f(A) will be negative, so bad moves always have a relative probability less than one. Good moves, for which f(B) – f(A) is positive, have a relative probability greater than one.)
- Temperature
  - Higher temperature = more likely to make a "bad" move
  - As T tends to zero, this probability tends to zero
  - SA becomes more link hill climbing
     If T is lowered <u>slowly enough</u>, SA is complete and admissible.
    - domain-specific
      - sometimes hard to determine

#### Local Beam Search

- Begin with *k* random states
  - *k*, instead of one, current state(s)
- Generate all successors of these states
- Keep the *k* best states
- · Stochastic beam search
- Probability of keeping a state is a function of its heuristic value
- More likely to keep "better" successors

#### Genetic Algorithms

• The Idea:

New states are generated by "mutating" a single state or "reproducing" (somehow combining) two parent states Selected according to their fitness



- Similar to stochastic beam search
- Start with *k* random states (the **initial population**)
- Encoding used for the "genome" of an individual strongly affects the behavior of the search
- Must have some combinable representation of state spaces Genetic algorithms / genetic programming are a large and active area of research

#### Tabu Search

- Problem: Hill climbing can get stuck on local maxima
- Solution: Maintain a list of k previously visited states, and prevent the search from revisiting them
- · Why not always do this?

#### Online Search

- Interleave computation and action (search some, act some) Exploration: Can't infer outcomes of actions; must actually perform them to learn what will happen
- Competitive ratio = Path cost found\* / Path cost that could be found\*\* \* On average, or in an adversarial scenario (worst case)
- \*\* If the agent knew the nature of the space, and could use offline search
- Relatively easy if actions are reversible

stuck on local optima.

- LRTA\* (Learning Real-Time A\*): Update h(s) (in state table) based on experience
- More about online search and nondeterministic actions next time...

#### Summary: Informed Search (I)

- State space can be treated as a "landscape" of movement on quality of states where we are trying to find "high" points
- Best-first search is a general search where the minimum-cost nodes are expanded first
- Greedy search uses minimal estimated cost h(n) to the goal state as measure of goodness. Reduces search time, but is neither complete nor optimal.

### Summary: Informed Search (II) · Hill-climbing algorithms keep only a single state in memory, but can get Simulated annealing escapes local optima, and is complete and optimal given a "long enough" cooling schedule.

- Genetic algorithms search a space by modeling biological evolution.
- information.

## Online search algorithms are useful in state spaces with partial/no **Questions?**

Class Exercise: Local Search for N-Queens					
Q					
	Q				
		Q			
			Q		
				Q	
					Q
(more on constraint satisfaction heuristics next time)					