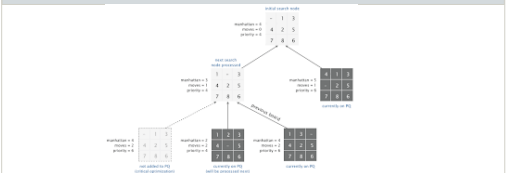


# Artificial Intelligence

## Class 3: Search (Ch. 3.1–3.3)



Some material adopted from notes by Charles R. Dyer, University of Wisconsin-Madison  
 Dr. Cynthia Matuszek – CMSC 671 Slides adapted with thanks from: Dr. Marie desJardins

# Bookkeeping

- TA Office hours: M 3-4, W 2-3
- General HW 1 questions?
- Basic Python
  - Sets, Tuples, Lists, Dictionaries, ...
  - <https://www.tutorialspoint.com/python>
  - <http://tiny.cc/concise-python-guide>
  - <http://www.w3resource.com/python/python-tutorial.php>
  - <https://docs.python.org/3>
    - Especially Library Reference → Built-in Functions

We will put these on Piazza

# Today's Class

- Goal-based agents
- Representing states and operators
- Example problems
- Generic state-space search algorithm

**Everything in AI comes down to search.**

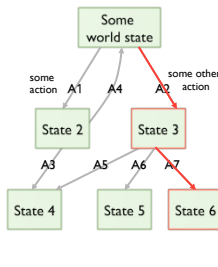
**Goal: understand search, and understand why.**

# Pre-Reading Review

- What is **search** (a.k.a. **state-space search**)?
  - Initial state
  - Actions / transition model
  - State space graph
  - Step cost / path cost
  - Goal test (cf. goal)
  - Solution / optimal solution
- What is an **open-loop system**?
- What is the difference between **expanding** and **generating** a state?
- What is the **frontier** (a.k.a. **open list**)?

# Search: The Core Idea

- For any problem:
  - World is (always) in some state
  - Agents take actions, which change the state
- We need a **sequence of actions** that gets the world into a particular goal state.
- To find it, we **search** the space of actions and states.



# Building Goal-Based Agents

- To build a goal-based agent we need to decide:
  - What is the goal to be achieved?
  - What are the actions?
  - What *relevant* information must be encoded?
    - To describe the state of the world
    - To describe the available transitions
    - To solve the problem



## What is the Goal?

- A situation we want to achieve
- A set of properties that we want to hold
- Must define a **“goal test”**
  - What does it mean to achieve it?
  - Have we done so?
- This is a hard question that is rarely tackled in AI!
  - Often, we assume the system designer or user will specify the goal
- For people, we stress the importance of establishing clear goals for as the first step towards solving a problem.
  - What are your goals?
  - What problem(s) are you trying to solve?

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## What Are Actions?

- **Primitive actions** or events:
  - Make changes in the world
  - In order to achieve a (sub)goal
  - Actions are also known as operators or moves
- **Examples:**
  - Chess: “advance a pawn”
  - Chess: “get a queen in position”
  - Navigation: “take a step”
  - Navigation: “go home”
  - Finance: “sell 10% of stock X”
  - Finance: “sell best-return shares”

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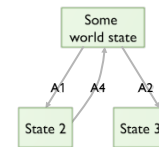
## Actions and Determinism

- In a **deterministic** world there is no uncertainty in an action's effects
- *Current world state + chosen action* fully specifies:
  - Whether that action can be applied to the current world
    - Is it applicable?
    - Is it legal?
  - What the state of the world is after the action is performed
    - No need for “history” information
    - Everything is encapsulated by state

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## Representing Actions

- Actions here are:
  - **Discrete events**
  - That occur at an **instant of time**
- **For example:**
  - State: “Mary is in class”
  - Action “Go home”
  - New state: “Mary is at home”
  - There is no representation of a state where she is in between (i.e., in the state of “going home”).



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## Sliding Tile Puzzles

- 15-puzzles, 8-puzzles
- How do we represent states?
- How do we represent actions?
  - Tile-1 moves north
  - Tile-1 moves west
  - Tile-1 moves east
  - Tile-1 moves south
  - Tile-2 moves north
  - Tile-2 moves west
  - ...



commons.wikimedia.org/wiki/File:15-puzzle-shuffled.svg, commons.wikimedia.org/wiki/File:15-puzzle-loyd-bis2.svg

## Representing Actions

- Number of actions / operators depends on **representation** used in describing a state
- 8-puzzle:
  - Could specify 4 possible moves (actions) for each of the 8 tiles:
    - **4\*8=32 operators.**
  - Or, could specify four moves for the “blank” square:
    - **4 operators!**
- **Careful representation can simplify a problem!**



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## Representing States

- What information about the world sufficiently describes all aspects **relevant** to solving the goal?
- That is: what knowledge must be in a state description to adequately describe the current state of the world?
- The **size of a problem** is usually described in terms of the **number of states** that are possible
  - Tic-Tac-Toe has about  $3^9$  states.
  - Checkers has about  $10^{40}$  states.
  - Rubik's Cube has about  $10^{19}$  states.
  - Chess has about  $10^{120}$  states in a typical game.

This is ten quintillion states.

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## Closed World Assumption

- We generally use the **Closed World Assumption**:
  - “All necessary information about a problem domain is available in each percept so that each state is a complete description of the world.”
- No incomplete information at any point in time.
  - A statement that is true is always known to be true.
  - ∴ If we do not know something is true, it is false.

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[en.wikipedia.org/wiki/Closed-world\\_assumption](http://en.wikipedia.org/wiki/Closed-world_assumption)

## Some Example Problems

- Toy problems and micro-worlds
  - 8-Puzzle
  - Boat Problems
  - Cryptarithmic
  - Remove 5 Sticks
  - Water Jug Problem
- Real-world problems

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## 8-Puzzle

Given an initial configuration of 8 numbered tiles on a 3 x 3 board, move the tiles in such a way so as to produce a desired goal configuration of the tiles.

5	4	
6	1	8
7	3	2

Start State

1	2	3
8		4
7	6	5

Goal State

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## 8-Puzzle

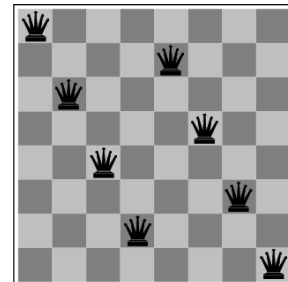
- **State:** 3 x 3 array describing where tiles are
- **Operators:** Move blank square Left, Right, Up or Down
  - This is a more efficient encoding of the operators!
- **Initial State:** Starting configuration of the board
- **Goal:** Some configuration of the board

5	4	
6	1	8
7	3	2

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## The 8-Queens Problem

Place eight (or N) queens on a chessboard such that no queen can reach any other



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## Boat Problems

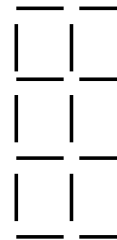
1 sheep, 1 wolf, 1 cabbage, 1 boat

- **Goal:** Move everything across the river.
- **Constraints:**
  - The boat can hold you plus one thing.
  - Wolf can never be alone with sheep.
  - Sheep can never be alone with cabbage.
- **State:** location of sheep, wolf, cabbage on shores and boat.
- **Operators:** Move ferry containing some set of occupants across the river (in either direction) to the other side.

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## Remove 5 Sticks

- Given the following configuration of sticks, remove exactly 5 sticks in such a way that the remaining configuration forms exactly 3 squares.



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## Some Real-World Problems

- Route finding
- Touring (traveling salesman)
- Logistics
- VLSI layout
- Robot navigation
- Learning

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## Knowledge Representation Issues

- What's in a state?
  - Is the color of the tiles relevant to solving an 8-puzzle?
  - Is sunspot activity relevant to predicting the stock market?
- What to represent is a very hard problem!
  - Usually left to the system designer to specify.
- What **level of abstraction** to describe the world?
  - Too fine-grained and we "miss the forest for the trees"
  - Too coarse-grained and we miss critical information

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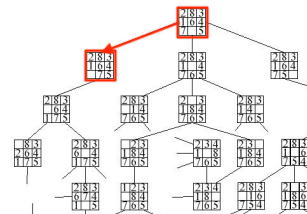
## Knowledge Representation Issues

- Number of states depends on
  - Representation
  - Level of abstraction
- In the Remove-5-Sticks problem:
  - If we represent individual sticks, then there are 17-choose-5 possible ways of removing 5 sticks (6188)
  - If we represent the "squares" defined by 4 sticks, there are 6 squares initially and we must remove 3
  - So, 6-choose-3 ways of removing 3 squares (20)

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## Formalizing Search in a State Space

- A *state space* is a **graph** (V, E):
  - V is a set of **nodes**
  - E is a set of **arcs**
  - Each arc is directed from a node to another node
- How does that work for 8-puzzle?



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## Formalizing Search in a State Space

- V: A **node** is a data structure that contains a state description plus other information such as the parent of the node, the name of the operator that generated the node from that parent, and other bookkeeping data
- E: Each **arc** corresponds to an instance of one of the operators. When the operator is applied to the state associated with the arc's source node, then the resulting state is the state associated with the arc's destination node

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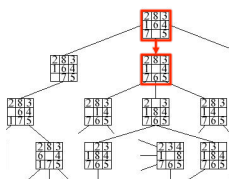
## Formalizing Search

- Each arc has a fixed, positive **cost**
  - Corresponding to the cost of the operator
  - What is "cost" of doing that action?
- Each node has a set of **successor nodes**
  - Corresponding to all operators (actions) that can apply at source node's state
  - **Expanding** a node is **generating** successor nodes, and adding them (and associated arcs) to the state-space graph

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## Formalizing Search II

- One or more nodes are designated as **start nodes**
- A **goal test** predicate is applied to a *state* to determine if its associated node is a goal node



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## Water Jug Problem

Given a full 5-gallon jug and an empty 2-gallon jug, the goal is to fill the 2-gallon jug with exactly one gallon of water.

Operator table

Name	Cond.	Transition	Effect
Empty5	–	$(x,y) \rightarrow (0,y)$	Empty 5-gal. jug
Empty2	–	$(x,y) \rightarrow (x,0)$	Empty 2-gal. jug
2to5	$x \leq 3$	$(x,2) \rightarrow (x+2,0)$	Pour 2-gal. into 5-gal.
5to2	$x \geq 2$	$(x,0) \rightarrow (x-2,2)$	Pour 5-gal. into 2-gal.
5to2part	$y < 2$	$(1,y) \rightarrow (0,y+1)$	Pour partial 5-gal. into 2-gal.

State =  $(x,y)$ , where  $x$  is the number of gallons of water in the 5-gallon jug and  $y$  is # of gallons in the 2-gallon jug

Initial State =  $(5,0)$

Goal State =  $(*,1)$   
(\* means any amount)

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## CLASS EXERCISE

- Representing a Sudoku puzzle as a search space
  - What are the states?
  - What are the operators?
  - What are the constraints (on operator application)?
  - What is the description of the goal state?
- Let's try it!

	3		
			1
3			
		2	

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## Formalizing Search III

- A **solution** is a sequence of operators that is associated with a path in a state space from a start node to a goal node.
- The **cost of a solution** is the sum of the arc costs on the solution path.
  - If all arcs have the same (unit) cost, then the solution cost is just the length of the solution (number of steps / state transitions)

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## Formalizing Search IV

- **State-space search:** searching through a state space for a solution by **making explicit** a sufficient portion of an **implicit** state-space graph to find a goal node
  - Initially  $V = \{S\}$ , where  $S$  is the start node
  - When  $S$  is **expanded**, its successors are **generated**; those nodes are added to  $V$  and the arcs are added to  $E$
  - This process continues until a goal node is found
- It isn't usually practical to represent entire space

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## Formalizing Search V

- Each node implicitly or explicitly represents a partial **solution path** (and cost of the partial solution path) from the start node to the given node.
  - In general, from a node there are many possible paths (and therefore solutions) that have this partial path as a prefix



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## State-Space Search Algorithm

```
function general-search (problem, QUEUEING-FUNCTION)
;; problem describes start state, operators, goal test,
;; and operator costs
;; queueing-function is a comparator function that
;; ranks two states
;; returns either a goal node or failure
```

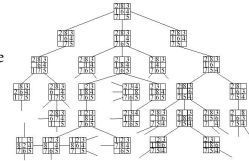
```
nodes = MAKE-QUEUE(MAKE-NODE(problem.INITIAL-STATE))
loop
  if EMPTY(nodes) then return "failure"
  node = REMOVE-FRONT(nodes)
  if problem.GOAL-TEST(node.STATE) succeeds
    then return node
  nodes = QUEUEING-FUNCTION(nodes, EXPAND(node,
    problem.OPERATORS))
end
;; Note: The goal test is NOT done when nodes are generated
;; Note: This algorithm does not detect loops
```



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## Key Procedures

- **EXPAND**
  - Generate **all** successor nodes of a given node
    - "What nodes can I reach from here (by taking what actions)?"
- **GOAL-TEST**
  - Test if state satisfies goal conditions
- **QUEUEING-FUNCTION**
  - Used to maintain a **ranked** list of nodes that are candidates for expansion
    - "What should I explore next?"



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## Algorithm Bookkeeping

- Typical node data structure includes:
  - State at this node
  - Parent node
  - Operator applied to get to this node
  - Depth of this node
    - That is, number of operator applications since initial state
  - Cost of the path
    - Sum of each operator application so far

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## Some Issues

- Search process constructs a search tree, where:
  - **Root** is the initial state and
  - **Leaf nodes** are nodes that are either:
    - Not yet expanded (i.e., they are in the list "nodes") or
    - Have no successors (i.e., they're "dead ends", because no operators can be applied, but they are not goals)
- Search tree may be infinite
  - Even for small search space
  - How?

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## Some Issues

- Return a path or a node depending on problem
  - In 8-queens return a **node**
  - 8-puzzle return a **path**
  - What about Sheep & Wolves?
- Changing definition of Queueing-Function → different search strategies
  - How do you choose what to expand next?

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## Evaluating Search Strategies

- Completeness:
  - Guarantees finding a solution if one exists
- Time complexity:
  - How long (worst or average case) does it take to find a solution?
  - Usually measured in number of states visited/nodes expanded
- Space complexity:
  - How much space is used by the algorithm?
  - Usually measured in maximum size of the "nodes" list during search
- Optimality / Admissibility
  - If a solution is found, is it guaranteed to be optimal (the solution with minimum cost)?

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