

Review: Independence

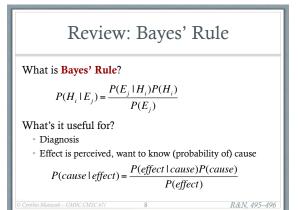
What does it mean for A and B to be **independent**?

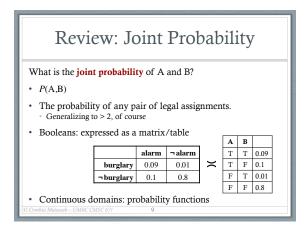
- P(A) **L** P(B)
- A and B do not affect each other's probability
- $P(A \land B) = P(A) P(B)$

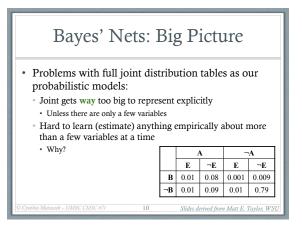


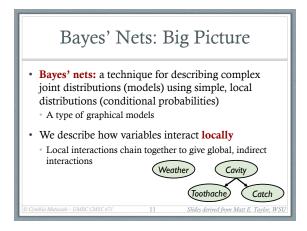
What does it mean for A and B to be **conditionally independent given C?**

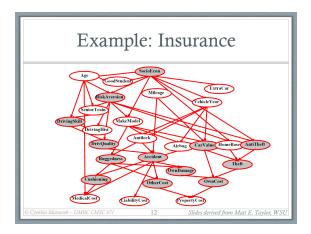
- A and B don't affect each other **if C is known**
- $P(A \land B | C) = P(A | C) P(B | C)$

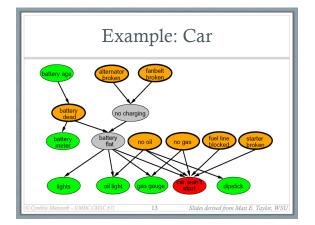


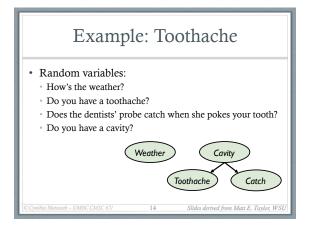


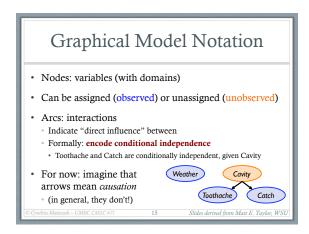


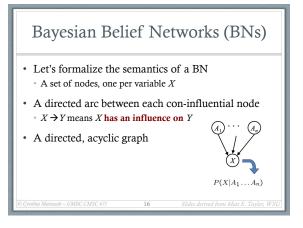


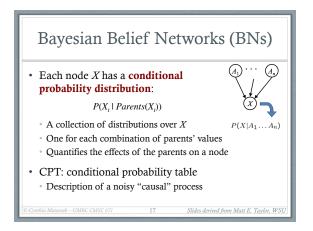


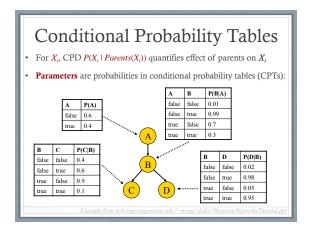


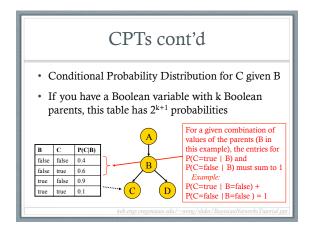


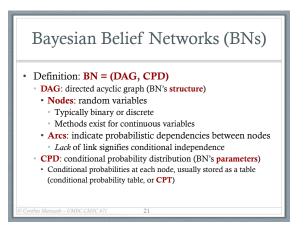


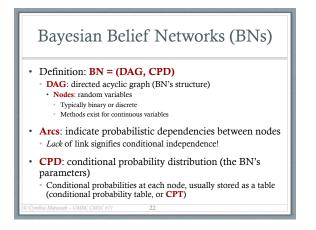


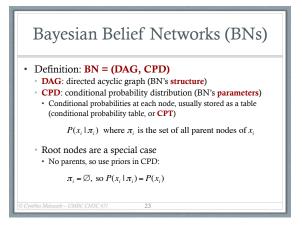


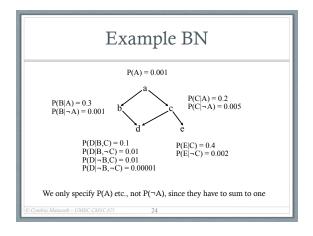


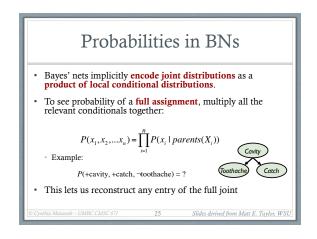


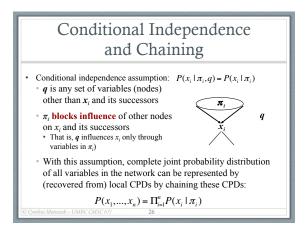


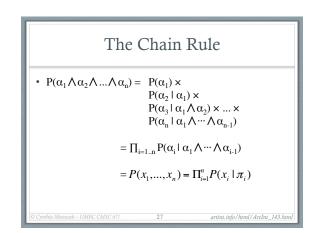


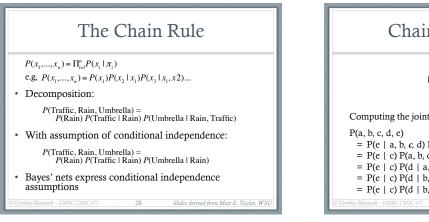


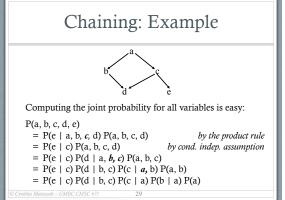


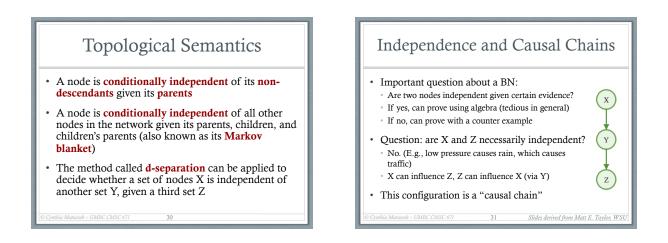


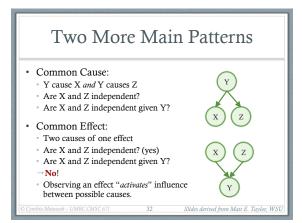


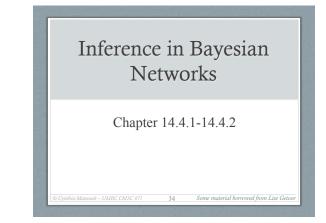








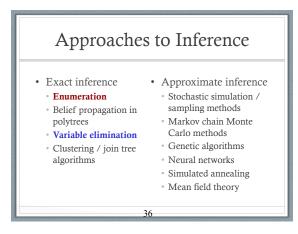






- Simple queries: Compute posterior marginal P(X_i | E=e) • E.g., P(NoGas | Gauge=empty, Lights=on, Starts=false)
- Conjunctive queries:
 P(X_i, X_j | E=e) = P(X_i | e=e) P(X_j | X_i, E=e)
- Optimal decisions:
- *Decision networks* include utility information
 Probabilistic inference gives P(outcome | action, evidence)
- Value of information: Which evidence should we seek next?
- Sensitivity analysis: Which probability values are most critical?
- **Explanation:** Why do I need a new starter motor?

) Cvnthia Matuszek – UMBC CMSC 671



Direct Inference with BNs Instead of computing the joint, suppose we just want the probability for *one* variable Exact methods of computation: Enumeration Variable elimination

• Join trees: get the probabilities associated with every query variable

Inference by Enumeration

- Add all of the terms (atomic event probabilities) from the full joint distribution
- If E are the evidence (observed) variables and Y are the other (unobserved) variables, then:
 P(X | e) = α P(X, E) = α Σ P(X, E, Y)
- Each P(X, E, Y) term can be computed using the chain rule
- Computationally expensive!

