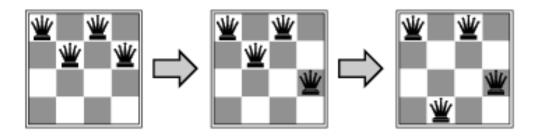
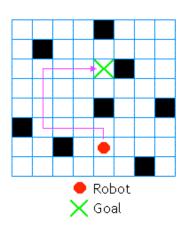
Local Search AI Class 6 (Ch. 4.1-4.2)

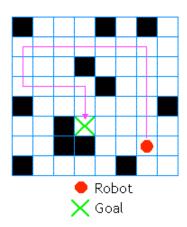


Based on slides by Dr. Marie desJardin. Some material also adapted from slides by Dr. Matuszek @ Villanova University, which are based on Hwee Tou Ng at Berkeley, which are based on Russell at Berkeley. Some diagrams are based on AIMA.

Bookkeeping

- HW 1 due last night
 - Grades within 1.5 weeks (hopefully sooner)
 - Discussions after grading
- HW 2 out tonight 11:59
 - Due 10/3, 11:59pm





Today's Class

- Iterative improvement methods
- Hill climbing
- Simulated annealing
- Local beam search
- Genetic algorithms
- Online search

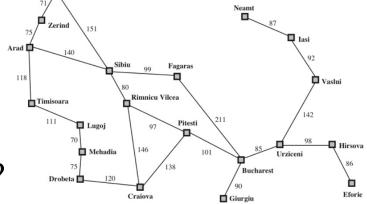
"If the path to the goal does not matter... [we can use] a single current node and move to neighbors of that node."

- R&N pg. 121

Admissibility

- Admissibility is a property of heuristics
 - They are *optimistic* think goal is closer than it is
 - (Or, exactly right)
- Admissible algorithms can be pretty bad!





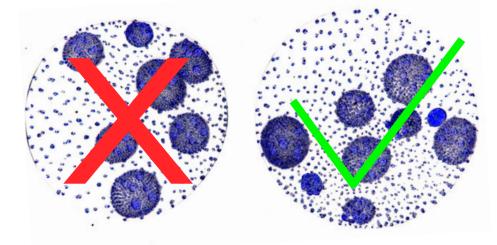
• Using admissible heuristics guarantees that the first solution found will be optimal, for some algorithms (A*).

Admissibility and Optimality

- Intuitively:
 - When A* finds a path of length k, it has already tried every other path which can have length $\leq k$
 - Because all frontier nodes have been sorted in ascending order of f(n)=g(n)+h(n)
- Does an admissible heuristic guarantee optimality for greedy search?
 - Reminder: f(n) = h(n), always choose node "nearest" goal
 - No sorting beyond that

Local Search Algorithms

- Sometimes the path to the goal is irrelevant
 - Goal state itself is the solution
 - **3** an **objective function** to evaluate states
- In such cases, we can use local search algorithms
- Keep a single "current" state, try to improve it



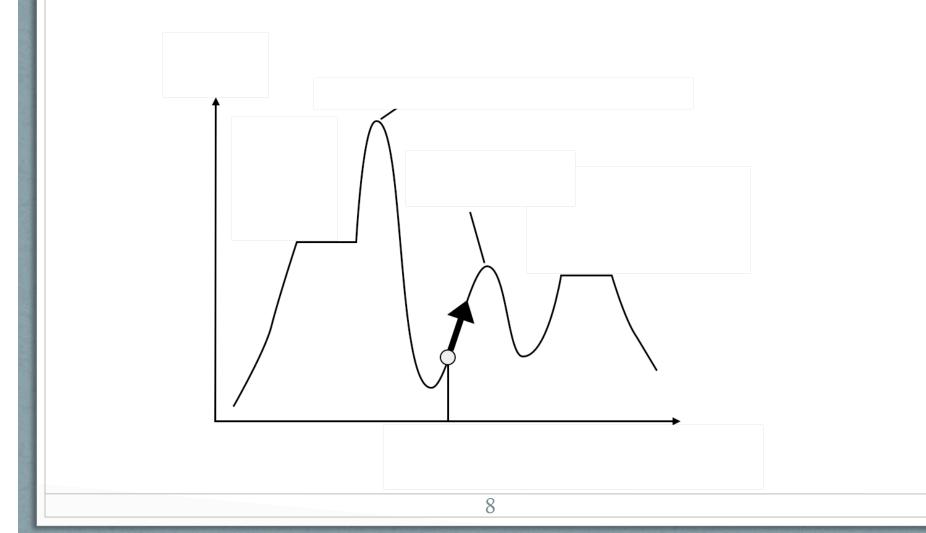
Local Search Algorithms

- Sometimes the path to the goal is irrelev Very efficient!
 - Goal state itself is the solution
 - **3** an **objective function** to evaluate states

Why?

- State space = set of "complete" configurations
 - That is, all elements of a solution are present
 - Find configuration satisfying constraints
 - Example?
- In such cases, we can use local search algorithms
- Keep a single "current" state, try to improve it

What Is This?

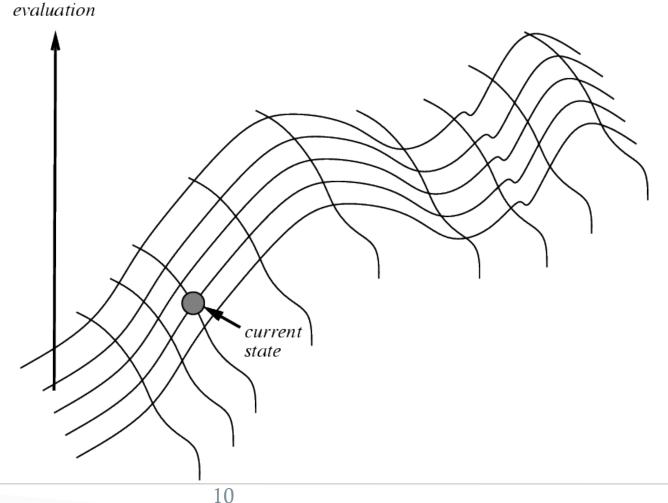


Iterative Improvement Search

- Start with an initial guess
- Gradually improve it until it is legal or optimal
- Some examples:
 - Hill climbing
 - Simulated annealing
 - Constraint satisfaction

Hill Climbing on State Surface

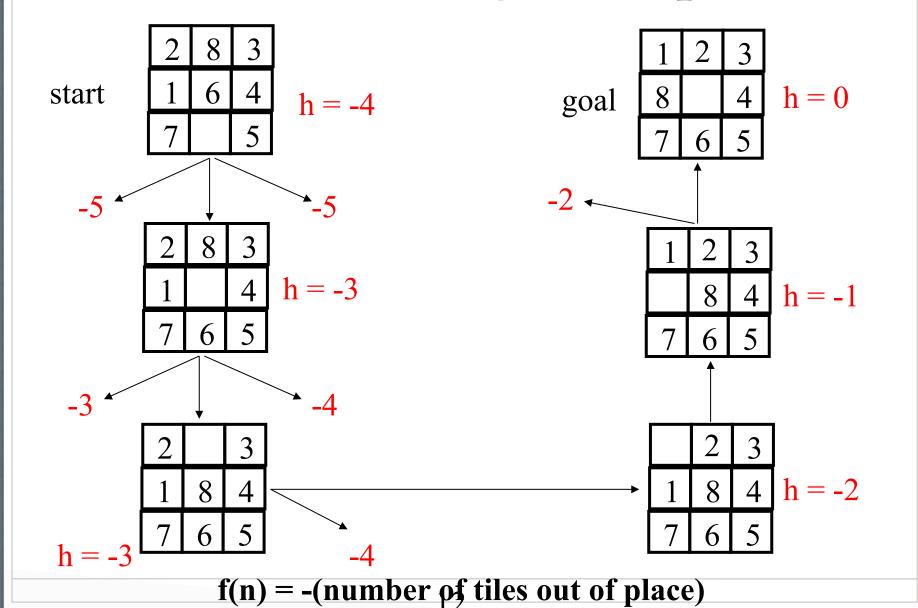
- Concept: trying to reach the "highest" (most desirable) point (state)
- "Height" Defined by Evaluation Function



Hill Climbing Search

- If there exists a successor s for the current state n such that
 - h(s) < h(n)
 - $h(s) \le h(t)$ for all the successors t of n, then move from n to s. Otherwise, halt at n.
- Look one step ahead to determine if any successor is "better" than current state
 - If so, move to the best successor
- A kind of Greedy search in that it uses *h*
 - But, does not allow backtracking or jumping to an alternative path
 - Doesn't "remember" where it has been.
- Not *complete*
 - Search will terminate at local minima, plateaux, ridges.

Hill Climbing Example



Exploring the Landscape

Local Maxima:

• Peaks that aren't the highest point in the space

• Plateaus:

 A broad flat region that gives the search algorithm no direction (random walk)

Ridges:

 Flat like a plateau, but with drop-offs to the sides; steps to the North, East, South and West may go down, but a step to the NW may go up.

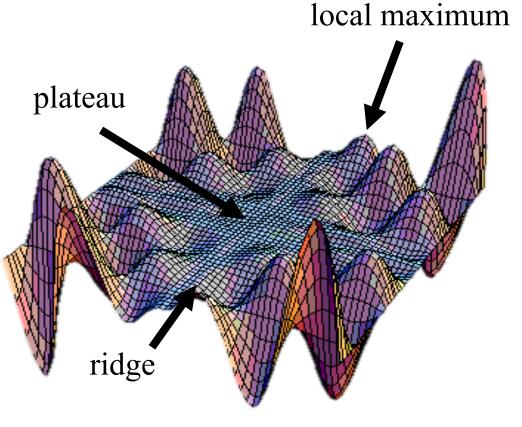
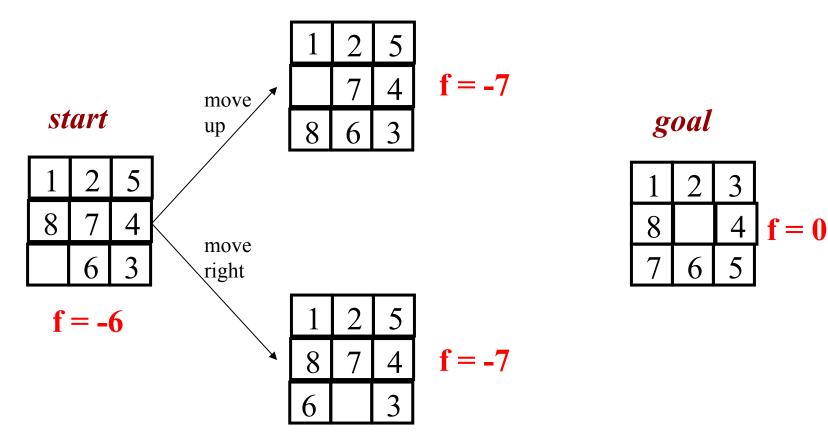


Image from: http://classes.yale.edu/fractals/CA/GA/Fitness/Fitness.html

Drawbacks of Hill Climbing

- Problems: local maxima, plateaus, ridges
- Remedies:
 - Random restart: keep restarting the search from random locations until a goal is found.
 - **Problem reformulation:** reformulate the search space to eliminate these problematic features
- Some problem spaces are great for hill climbing;
 others are terrible

Example of a Local Optimum



f = -(manhattan distance)

Some Extensions of Hill Climbing

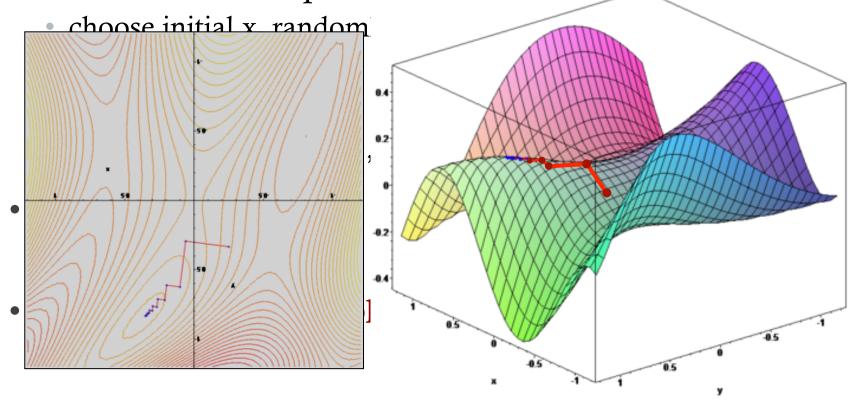
- Simulated Annealing
 - Escape local maxima by allowing *some* "bad" moves but gradually decreasing their frequency
- Local Beam Search
 - Keep track of *k* states rather than just one
 - At each iteration:
 - All successors of the *k* states are generated and evaluated
 - Best *k* are chosen for the next iteration

Some Extensions of Hill Climbing

- Stochastic Beam Search
 - Chooses semi-randomly from "uphill" possibilities
 - "Steeper" moves have a higher probability of being chosen
- Random-Restart Climbing
 - Can actually be applied to any form of search
 - Pick random starting points until one leads to a solution
- Genetic Algorithms
 - Each successor is generated from two predecessor (parent) states

Gradient Ascent / Descent

• Gradient descent procedure for finding the ara min fly)



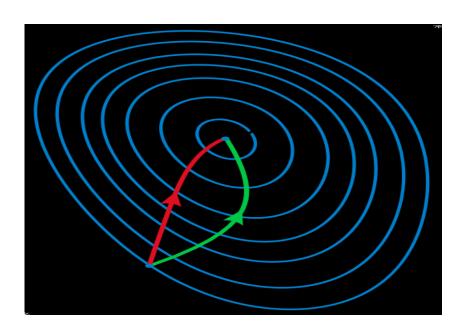
18 Images from http://en.wikipedia.org/wiki/Gradient_descent

Gradient Methods vs. Newton's Method

 A reminder of Newton's method from Calculus:

$$\mathbf{x}_{i+1} \leftarrow \mathbf{x}_i - \eta f'(\mathbf{x}_i) / f''(\mathbf{x}_i)$$

- Newton's method uses 2nd order information (the second derivative, or, **curvature**) to take a more direct route to the minimum.
- The second-order information is more expensive to compute, but converges more quickly.



Contour lines of a function Gradient descent (green) Newton's method (red)

Simulated Annealing

- Simulated annealing (SA): analogy between the way metal cools into a minimum-energy crystalline structure and the search for a minimum generally
 - In very hot metal, molecules can move fairly freely
 - But, they are slightly less likely to move out of a stable structure
 - As you slowly cool the metal, more molecules are "trapped" in place
- Conceptually: Escape local maxima by allowing some "bad" (locally counterproductive) moves but gradually decreasing their frequency

Simulated Annealing (II)

- Can avoid becoming trapped at local minima.
- Uses a random local search that:
 - Accepts changes that increase objective function f
 - As well as some that decrease it
- Uses a control parameter T
 - By analogy with the original application
 - Is known as the system "temperature"
- T starts out high and gradually decreases toward 0

Simulated Annealing (IIII)

- f(s) represents the quality of state n (high is good)
- A "bad" move from A to B is accepted with a probability

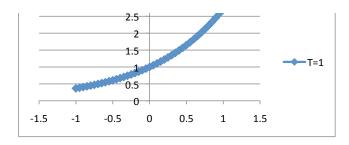
$$P(\text{move}_{A\rightarrow B}) \approx e^{(f(B)-f(A))/T}$$

• (Note that f(B) - f(A) will be negative, so bad moves always have a relatively probability less than one. Good moves, for which f(B) - f(A) is positive, have a relative probability greater than one.)

• Temperature

- The higher the temperature, the more likely it is that a "bad" move can be made.
- As T tends to zero, this probability tends to zero, and SA becomes more like hill climbing
- If T is lowered slowly enough, SA is complete and admissible.

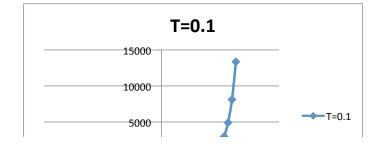
Visualizing SA Probabilities

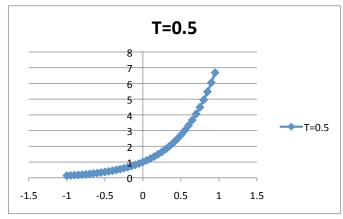


p(neg) = 0.1422741

[-1,1] ratio = 49.402449

p(neg) = 0.0202419





[-1,1] ratio = 294267566

The Simulated Annealing Algorithm

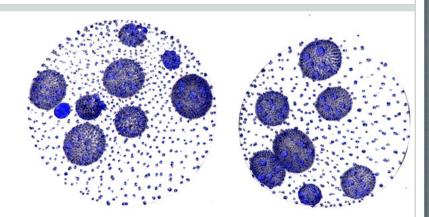
Local Beam Search

- Begin with *k* random states
 - k, instead of one, current state(s)
- Generate all successors of these states
- Keep the *k* best states
- Stochastic beam search
 - Probability of keeping a state is a **function** of its heuristic value
 - More likely to keep "better" successors

Genetic Algorithms

• The Idea:

- New states are generated by "mutating" a single state or "reproducing" (somehow combining) two parent states
- Selected according to their fitness



- Similar to stochastic beam search
- Start with *k* random states (the **initial population**)
 - Encoding used for the "genome" of an individual strongly affects the behavior of the search
 - Genetic algorithms / genetic programming are a large and active area of research

Class Exercise: Local Search for N-Queens

Q					
	Q				
		Q			
			Q		
				Q	
					Q

(more on constraint satisfaction heuristics next time...)

Tabu Search

- Problem: Hill climbing can get stuck on local maxima
- Solution: Maintain a list of *k* previously visited states, and prevent the search from revisiting them
- Why not always do this?

Online Search

- Interleave computation and action (search some, act some)
 - Exploration: Can't infer outcomes of actions; must actually perform them to learn what will happen
- Competitive ratio = Path cost found* / Path cost that could be found**
 - * On average, or in an adversarial scenario (worst case)
 - ** If the agent knew the nature of the space, and could use offline search
- Relatively easy if actions are reversible
- LRTA* (Learning Real-Time A*): Update *h*(*s*) (in state table) based on experience
- More about online search and nondeterministic actions next time...

Summary: Informed Search

- **Best-first search** is general search where the minimum-cost nodes are expanded first.
- Greedy search uses minimal estimated cost h(n) to the goal state as measure
- Reduces the search time, but is neither complete nor optimal.
- **A* search** combines uniform-cost search and greedy search: f(n) = g(n) + h(n). A* handles state repetitions and h(n) never overestimates.
 - Complete and optimal, but space complexity is high
 - The time complexity depends on the quality of the heuristic function
 - IDA* and SMA* reduce the memory requirements of A*
- Hill-climbing algorithms keep only a single state in memory, but can get stuck on local optima.
- **Simulated annealing** escapes local optima, and is complete and optimal given a "long enough" cooling schedule.
- **Genetic algorithms** can search a large space by modeling biological evolution.
- Online search algorithms are useful in state spaces with partial/no information.