

# Bookkeeping (Lots)

- Many timing changes (mostly so midterm timing isn't awful)
- HW3 due date: **10/19** @ 11:59pm
- Midterm is **next Tuesday** in class
- Project date changes
  - If they don't work for you, let me know immediately

# Today's Class

- Machine learning
  - What is ML?
  - Inductive learning ← Review: What is induction?
    - Supervised
    - Unsupervised
  - Decision trees
- Later: Bayesian learning, naïve Bayes, and BN learning

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# What is Learning?

- "Learning denotes changes in a system that ... enable a system to do the same task more efficiently the next time." –Herbert Simon
- "Learning is constructing or modifying representations of what is being experienced."
  - -Ryszard Michalski
- "Learning is making useful changes in our minds."
  - -Marvin Minsky

# Why Learn?

- Discover previously-unknown new things or structure
  - Data mining, scientific discovery
- Fill in skeletal or incomplete domain knowledge
  - Large, complex AI systems:
    - · Cannot be completely derived by hand and
    - · Require dynamic updating to incorporate new information
  - Learning new characteristics expands the domain or expertise and lessens the "brittleness" of the system
- Build agents that can adapt to users or other agents
- Understand and improve efficiency of human learning
  - Use to improve methods for teaching and tutoring people (e.g., better computer-aided instruction)

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## Pre-Reading Quiz

- What's supervised learning?
  - What's classification? What's regression?
  - What's a hypothesis? What's a hypothesis space?
  - What are the training set and test set?
  - What is Ockham's razor?
- What's unsupervised learning?

# Some Terminology

The Big Idea: given some data, you learn a model of how the world works that lets you predict new data.

- Training Set: Data from which you learn initially.
- Model: What you learn. A "model" of how inputs are associated with outputs.
- Test set: New data you test tour model against.
- Corpus: A body of data. (pl.: corpora)
- Representation: The computational expression of data

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#### Major Paradigms of Machine Learning

- **Rote learning:** 1:1 mapping from **inputs** to stored representation
  - You've seen a problem before
  - Learning by memorization
  - Association-based storage and retrieval
- **Induction:** Specific examples → general conclusions
- Clustering: Unsupervised grouping of data

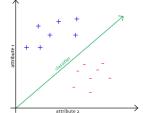
#### Major Paradigms of Machine Learning

- **Analogy:** Model is **correspondence** between two different **representations**
- **Discovery:** Unsupervised, specific goal not given
- **Genetic algorithms:** "Evolutionary" search techniques
  - Based on an analogy to "survival of the fittest"
  - Surprisingly hard to get right/working
- **Reinforcement:** Feedback (positive or negative reward) given at the end of a sequence of steps

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# The Classification Problem (1)

• Extrapolate from **examples** (training data) to make accurate predictions about future data



- Supervised vs. unsupervised learning
  - Learn an unknown function f(X) = Y, where
  - X is an input example
  - Y is the desired output. (*f* is the..?)
  - **Supervised learning** implies we are given a **training set** of (X, Y) pairs by a "teacher"
  - **Unsupervised learning** means we are only given the Xs and some (ultimate) feedback function on our performance

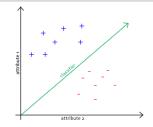
# The Classification Problem (2)

- Concept learning or classification (aka "induction")
  - Given a set of examples of some concept/class/category:
  - Determine if a given example is an instance of the concept (class member) or not
  - If it is, we call it a positive example
  - If it **is not**, it is called a negative example
  - Or we can make a probabilistic prediction (e.g., using a Bayes net)

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# Supervised Concept Learning

- Given a training set of positive and negative examples of a concept
- Construct a description (model) that will accurately classify whether future examples are positive or negative

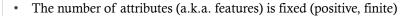


• I.e., learn estimate of function f given a training set:  $\{(x_1, y_1), (x_2, y_2), ..., (x_n, y_n)\}$  where each  $y_i$  is either + (positive) or - (negative), or a probability distribution over +/-

# Inductive Learning Framework

- Raw input data from sensors usually preprocessed to obtain a feature vector, X
  - Relevant features for classifying examples
  - Each x is a list of (attribute, value) pairs:

X = [Person:Sue, EyeColor:Brown, Age:Young, Sex:Female]



- Attributes have fixed, finite number # of possible values
  - · Or continuous within some well-defined space, e.g., "age"
- Examples interpreted as a point in an n-dimensional feature space
  - n is the number of attributes

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# Inductive Learning as Search

- Instance space, I, is set of all possible examples
  - Defines the language for the training and test instances
  - Usually each instance  $i \in I$  is a **feature vector**
  - Features are also sometimes called attributes or variables
  - I:  $V_1 \times V_2 \times ... \times V_k$ ,  $i = (v_1, v_2, ..., v_k)$
- Class variable C gives an instance's class (to be predicted)
- Model space M defines the possible classifiers
  - M: I  $\rightarrow$  C, M = {m<sub>1</sub>, ... m<sub>n</sub>} (possibly infinite)
  - Model space is sometimes defined in terms using same features as the instance space (not always)
- Training data directs the search for a good (consistent, complete, simple) hypothesis in the model space

# Model Spaces (1)

- Decision trees
  - Partition the instance space into axis-parallel regions
  - · Labeled with class value
- Nearest-neighbor classifiers
  - Partition the instance space into regions defined by centroid instances (or cluster of k instances)
- Bayesian networks
  - Probabilistic dependencies of class on attributes)
  - Naïve Bayes: special case of BNs where class → each attribute

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# Model Spaces (2)

- Neural networks
  - Nonlinear feed-forward functions of attribute values
- Support vector machines
  - Find a separating plane in a high-dimensional feature space
- Associative rules (feature values → class)
- First-order logical rules

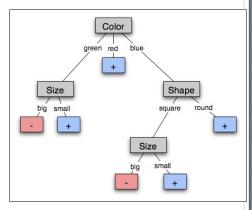
### Learning Decision Trees

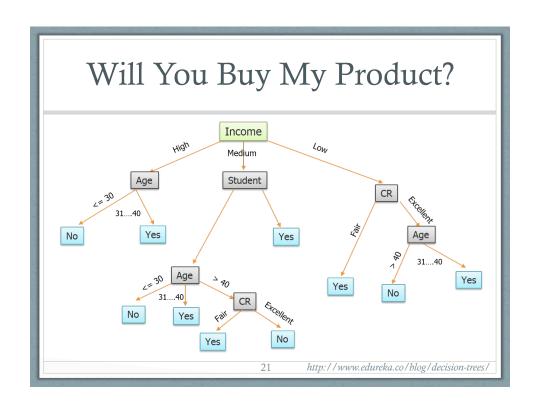
- Goal: Build a decision tree to classify examples as positive or negative instances of a concept using supervised learning from a training set
- A decision tree is a tree where:
  - Each **non-leaf** node is associated with an attribute (feature)
  - Each **leaf** node has associated with it a classification (+ or -)
    - Positive and negative data points
  - Each **arc** is associated with one possible value of the attribute at the node from which the arc is directed
- Generalization: allow for >2 classes
  - e.g., {sell, hold, buy}

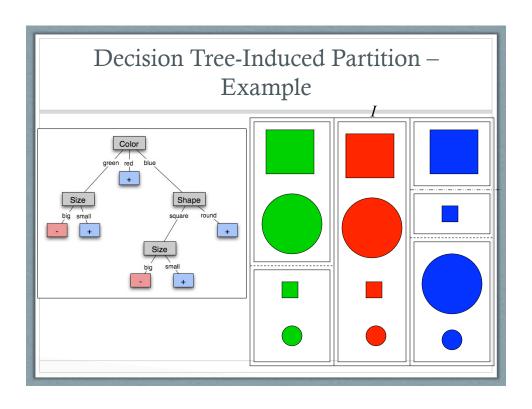
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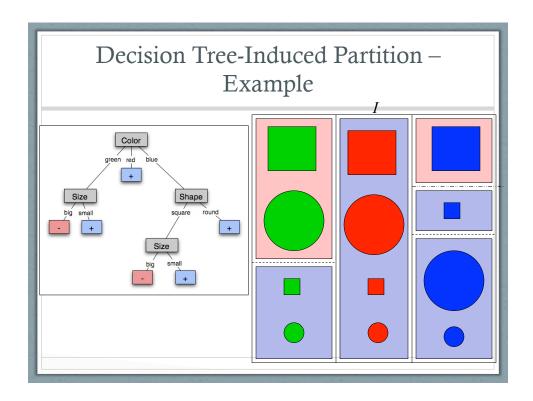
# Learning Decision Trees

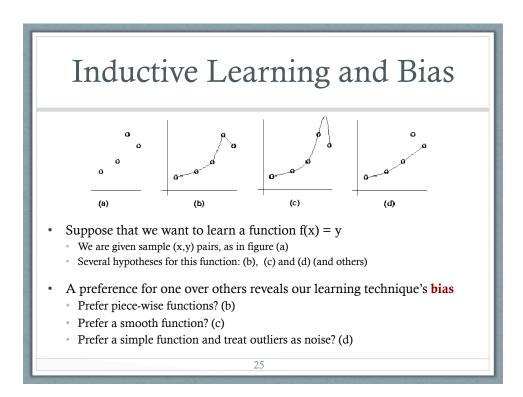
- Each non-leaf node is associated with an attribute (feature)
- Each **leaf** node is associated with a classification (+ or -)
- Each arc is associated with one possible value of the attribute at the node from which the arc is directed











#### Preference Bias: Ockham's Razor

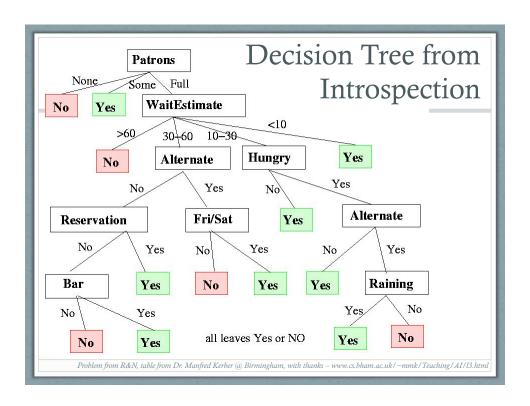
- A.k.a. Occam's Razor, Law of Economy, or Law of Parsimony
- Principle stated by William of Ockham (1285-1347/49), a scholastic:
  - "Non sunt multiplicanda entia praeter necessitatem"
  - "Entities are not to be multiplied beyond necessity"
- The simplest consistent explanation is the best
- Smallest decision tree that correctly classifies all training examples
- Finding the provably smallest decision tree is NP-hard!
- So, instead of constructing the absolute smallest tree consistent with the training examples, construct one that is "pretty small"

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#### R&N's Restaurant Domain

- Model decision a patron makes when deciding whether to wait for a table
  - Two classes (outcomes): wait, leave
  - Ten attributes: Alternative available? ∃ Bar? Is it Friday? Hungry? How full is restaurant? How expensive? Is it raining? Do we have a reservation? What type of restaurant is it? What's purported waiting time?
- Training set of 12 examples
- ~ 7000 possible cases

	A Training Set										
Datum	Attributes								Outcome		
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	Wait
$\mathbf{x}_1$	Yes	No	No	Yes	Some	£££	No	Yes	French	0-10	Yes
$X_2$	Yes	No	No	Yes	Full	£	No	No	Thai	30-60	No
$X_3$	No	Yes	No	No	Some	£	No	No	Burger	0-10	Yes
$X_4$	Yes	No	Yes	Yes	Full	£	Yes	No	Thai	10-30	Yes
$X_5$	Yes	No	Yes	No	Full	£££	No	Yes	French	>60	No
$X_6$	No	Yes	No	Yes	Some	££	Yes	Yes	Italian	0-10	Yes
$X_7$	No	Yes	No	No	None	£	Yes	No	Burger	0-10	No
$X_8$	No	No	No	Yes	Some	££	Yes	Yes	Thai	0-10	Yes
$X_9$	No	Yes	Yes	No	Full	£	Yes	No	Burger	>60	No
$X_{10}$	Yes	Yes	Yes	Yes	Full	£££	No	Yes	Italian	10-30	No
$\mathbf{X}_{11}$	No	No	No	No	None	£	No	No	Thai	0-10	No
$X_{12}$	Yes	Yes	Yes	Yes	Full	£	No	No	Burger	30-60	Yes



#### ID3/C4.5

- A greedy algorithm for decision tree construction
  - Ross Quinlan, 1987
- Top-down construction of decision tree by recursively selecting the "best attribute" to use at current node
  - Once attribute is selected for current node, generate children nodes, one for each possible value of selected attribute
  - Partition examples using possible values of this attribute, and assign these subsets of examples to the appropriate child node
  - Repeat for each child node until all examples associated with a node are either all positive or all negative

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#### ID3/C4.5

- 1. Select an attribute for current node
- 2. Generate child nodes
  - One for each possible value of selected attribute
- 3. Partition examples (training set) using attribute values
- 4. Assign subsets of examples to appropriate child node
- 5. Repeat for each child node until all examples are either positive or negative at that node
  - These are leaves

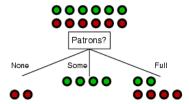
# Choosing the Best Attribute

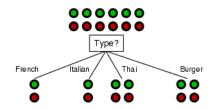
- **Key problem:** choose which attribute to split a set of examples
- Some possibilities are:
  - Random: Select any attribute at random
  - Least-Values: Choose the attribute with the smallest number of possible values
  - Most-Values: Choose the attribute with the largest number of possible values
  - Max-Gain: Choose the attribute that has the largest expected information gain—i.e., the attribute that will result in the smallest expected size of the subtrees rooted at its children
- ID3 uses Max-Gain to select the best attribute

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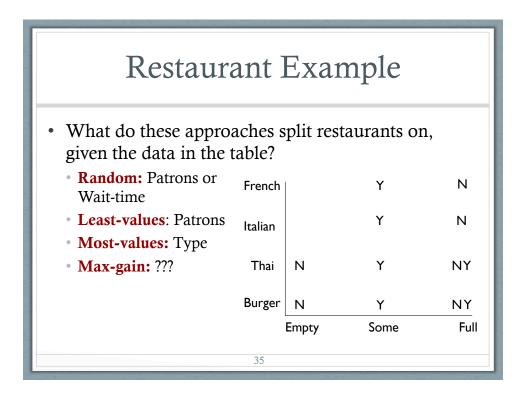
# Choosing an Attribute

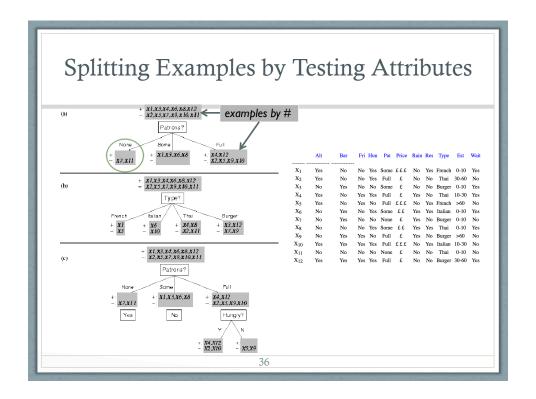
• Idea: a good attribute splits the examples into subsets that are (ideally) "all positive" or "all negative"

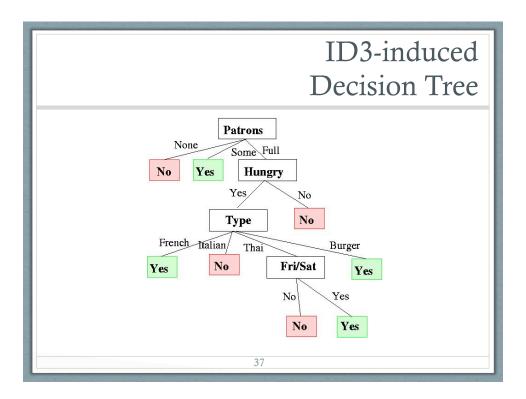




- Which is better: *Patrons?* or *Type?*
- Why?







# Information Theory 101

- **Information** is defined as the **minimum number of bits** needed to store or send some information
  - Wikipedia: "The measure of data, known as information entropy, is usually expressed by the average number of bits needed for storage or communication"
- Intuitions
  - Common words (a, the, dog) are shorter than less common ones (parliamentarian, foreshadowing)
  - In Morse code, common (probable) letters have shorter encodings
- "A Mathematical Theory of Communication," Bell System Technical Journal, 1948, Claude E. Shannon, Bell Labs

## Information Theory 103

- Entropy is the average number of bits/message needed to represent a stream of messages
- Information conveyed by distribution (a.k.a. **entropy** of P):  $I(P) = -(p_1*log_2(p_1) + p_2*log_2(p_2) + ... + p_n*log_2(p_n))$
- Examples:
  - If P is (0.5, 0.5) then  $I(P) = 1 \rightarrow$  entropy of a fair coin flip
  - If P is (0.67, 0.33) then I(P) = 0.92
  - If Pis (0.99, 0.01) then I(P) = 0.08
  - If P is (1, 0) then I(P) = 0
- As the distribution becomes more skewed, the amount of information decreases
  - ...because I can just predict the most likely element, and usually be right

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# Entropy as Measure of **Homogeneity of Examples**

- Entropy can be used to characterize the (im)purity of an arbitrary collection of examples
- Low entropy implies high homogeneity
  - Given a collection *S* (e.g., the table with 12 examples for the restaurant domain), containing positive and negative examples of some target concept, the entropy of S relative to its Boolean classification is:

$$I(S) = -(p_{+}*log_{2}(p_{+}) + p_{-}*log_{2}(p_{-}))$$

Entropy([6+, 6-]) = 1  $\rightarrow$  entropy of the restaurant dataset Entropy([9+, 5-]) = 0.940

#### Information Gain

- **Information gain** is based on:
  - Decrease in entropy
  - After a dataset is split on an attribute.
  - → High homogeneity e.g., likelihood samples will have the same class.
- Constructing a decision tree is all about finding attribute that returns the highest information gain (i.e., the most homogeneous branches)

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#### How Well Does it Work?

Decision trees are at least as accurate as human experts!

- A study for diagnosing breast cancer had humans correctly classifying the examples 65% of the time; the decision tree classified 72% correct
- British Petroleum designed a decision tree for gas-oil separation for offshore oil platforms that replaced an earlier rule-based expert system
- Cessna designed an airplane flight controller using 90,000 examples and 20 attributes per example
- SKICAT (Sky Image Cataloging and Analysis Tool) used a decision tree to classify sky objects that were an order of magnitude fainter than was previously possible, with an accuracy of over 90%.

# Extensions of the Decision Tree Learning Algorithm

- Using gain ratios
- Real-valued data
- · Noisy data and overfitting
- Generation of rules
- Setting parameters
- Cross-validation for experimental validation of performance
- C4.5 is an extension of ID3 that accounts for unavailable values, continuous attribute value ranges, pruning of decision trees, rule derivation, and so on

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#### Real-Valued Data

- Select a set of thresholds defining intervals
- Each interval becomes a discrete value of the attribute
- Use some simple heuristics...
  - always divide into quartiles
- Use domain knowledge…
  - divide age into infant (0-2), toddler (3 5), school-aged (5-8)
- Or treat this as another learning problem
  - Try a range of ways to discretize the continuous variable and see which yield "better results" w.r.t. some metric
  - E.g., try midpoint between every pair of values

# Measuring Model Quality

- How good is a model?
  - Predictive accuracy
  - False positives / false negatives for a given cutoff threshold
    - Loss function (accounts for cost of different types of errors)
  - Area under the (ROC) curve
  - Minimizing loss can lead to problems with overfitting
- Overfitting: coming up with a model that is TOO specific to your training data

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## Measuring Model Quality

- Training error
  - Train on all data; measure error on all data
  - Subject to overfitting (of course we'll make good predictions on the data on which we trained!)
- Regularization
  - Attempt to avoid overfitting
  - Explicitly minimize the complexity of the function while minimizing loss
  - Tradeoff is modeled with a regularization parameter

#### Cross-Validation

- Holdout cross-validation:
  - Divide data into training set and test set
  - Train on training set; measure error on test set
  - Better than training error, since we are measuring *generalization to new data*
  - To get a good estimate, we need a reasonably large test set
  - But this gives less data to train on, reducing our model quality!

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# Cross-Validation, cont.

- k-fold cross-validation:
  - Divide data into *k* folds
  - Train on *k-1* folds, use the *k*th fold to measure error
  - Repeat *k* times; use average error to measure generalization accuracy
  - Statistically valid and gives good accuracy estimates
- Leave-one-out cross-validation (LOOCV)
  - k-fold cross validation where k=N (test data = 1 instance!)
  - Quite accurate, but also quite expensive, since it requires building *N* models

# Summary: Decision Tree Learning

- Inducing decision trees is one of the most widely used learning methods in practice
- Can out-perform human experts in many problems
- Strengths include
  - Fast
  - Simple to implement
  - Can convert result to a set of easily interpretable rules Empirically valid in many commercial products

  - Handles noisy data
- Weaknesses:
  - Univariate splits/partitioning using only one attribute at a time so limits types of possible trees
  - Large decision trees may be hard to understand Requires fixed-length feature vectors Non-incremental (i.e., batch method)