

Machine Learning: Decision Trees



Chapter 18.1-18.3

Some material adopted from notes
by Chuck Dyer

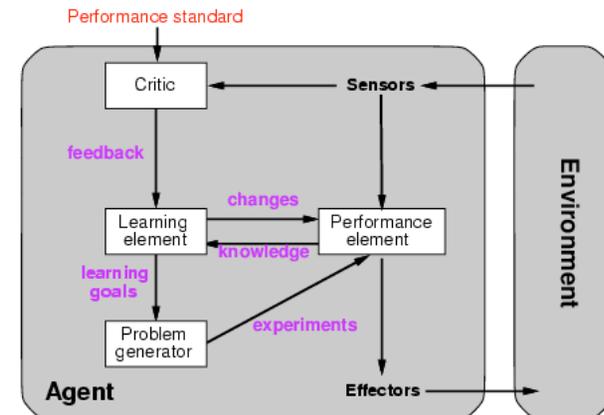
What is learning?

- “Learning denotes changes in a system that ... enable a system to do the same task more efficiently the next time.” –Herbert Simon
- “Learning is constructing or modifying representations of what is being experienced.” –Ryszard Michalski
- “Learning is making useful changes in our minds.” –Marvin Minsky

Why study learning?

- Understand and improve efficiency of human learning
 - Use to improve methods for teaching and tutoring people (e.g., better computer-aided instruction)
- Discover new things or structure previously unknown
 - Examples: data mining, scientific discovery
- Fill in skeletal or incomplete specifications about a domain
 - Large, complex AI systems can’t be completely built by hand and require dynamic updating to incorporate new information
 - Learning new characteristics expands the domain or expertise and lessens the “brittleness” of the system
- Build agents that can adapt to users, other agents, and their environment

A general model of learning agents



Major paradigms of machine learning

- **Rote learning** – One-to-one mapping from inputs to stored representation. “Learning by memorization.” Association-based storage and retrieval.
- **Induction** – Use specific examples to reach general conclusions
- **Clustering** – Unsupervised identification of natural groups in data
- **Analogy** – Determine correspondence between two different representations
- **Discovery** – Unsupervised, specific goal not given
- **Genetic algorithms** – “Evolutionary” search techniques, based on an analogy to “survival of the fittest”
- **Reinforcement** – Feedback (positive or negative reward) given at the end of a sequence of steps

The inductive learning problem

- Extrapolate from a given set of examples to make accurate predictions about future examples
- **Supervised versus unsupervised learning**
 - Learn an unknown function $f(X) = Y$, where X is an input example and Y is the desired output.
 - **Supervised learning** implies we are given a **training set** of (X, Y) pairs by a “teacher”
 - **Unsupervised learning** means we are only given the X s and some (ultimate) feedback function on our performance.
- **Concept learning or classification**
 - Given a set of examples of some concept/class/category, determine if a new one is an instance of the concept or not
 - Instances are *positive examples*, non-instances *negative examples*
 - Or we can make a probabilistic prediction (e.g., using a Bayes net)

Supervised concept learning

- Given a training set of positive and negative examples of a concept
- Construct a description that will accurately classify whether future examples are positive or negative
- That is, learn some good estimate of function f given a training set $\{(x_1, y_1), (x_2, y_2), \dots, (x_n, y_n)\}$ where each y_i is either + (positive) or - (negative), or a probability distribution over +/-

Inductive learning framework

- Raw input data from sensors are typically preprocessed to obtain a **feature vector**, X , that adequately describes all of the relevant features for classifying examples
- Each x is a list of (attribute, value) pairs. For example,
 $X = [\text{Person:Sue, EyeColor:Brown, Age:Young, Sex:Female}]$
- The number of attributes (a.k.a. features) is fixed (positive, finite)
- Each attribute has a fixed, finite number of possible values (or could be continuous)
- Each example is interpreted as a point in an n -dimensional **feature space**, where n is the number of attributes

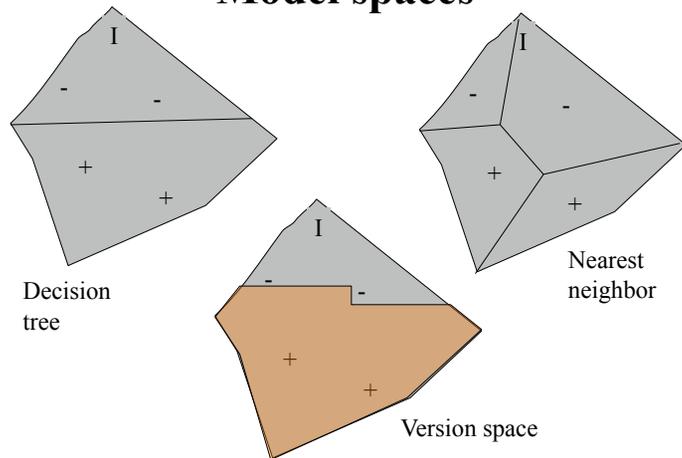
Inductive learning as search

- Instance space I defines the language for the training and test instances
 - Typically, but not always, each instance $i \in I$ is a feature vector
 - Features are sometimes called attributes or variables
 - $I: V_1 \times V_2 \times \dots \times V_k, i = (v_1, v_2, \dots, v_k)$
- Class variable C gives an instance's class (to be predicted)
- Model space M defines the possible classifiers
 - $M: I \rightarrow C, M = \{m_1, \dots, m_n\}$ (possibly infinite)
 - Model space is sometimes, but not always, defined in terms of the same features as the instance space
- Training data can be used to direct the search for a good (consistent, complete, simple) hypothesis in the model space

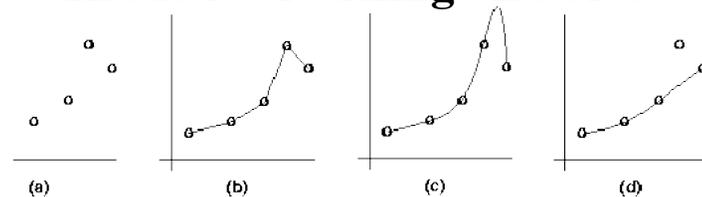
Model spaces

- **Decision trees**
 - Partition the instance space into axis-parallel regions, labeled with class value
- **Version spaces**
 - Search for necessary (lower-bound) and sufficient (upper-bound) partial instance descriptions for an instance to be in the class
- Nearest-neighbor classifiers
 - Partition the instance space into regions defined by the centroid instances (or cluster of k instances)
- Associative rules (feature values \rightarrow class)
- First-order logical rules
- Bayesian networks (probabilistic dependencies of class on attributes)
- Neural networks

Model spaces



Inductive learning and bias



- Suppose that we want to learn a function $f(x) = y$ and we are given some sample (x, y) pairs, as in figure (a)
- There are several hypotheses we could make about this function, e.g.: (b), (c) and (d)
- A preference for one over the others reveals the **bias** of our learning technique, e.g.:
 - prefer piece-wise functions
 - prefer a smooth function
 - prefer a simple function and treat outliers as noise

Preference bias: Ockham's Razor

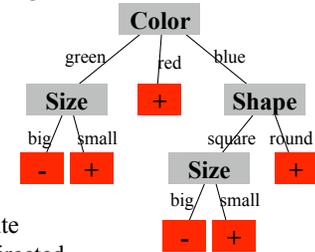
- A.k.a. Occam's Razor, Law of Economy, or Law of Parsimony
- Principle stated by William of Ockham (1285-1347/49), a scholastic, that
 - “*non sunt multiplicanda entia praeter necessitatem*”
 - or, entities are not to be multiplied beyond necessity
- The simplest consistent explanation is the best
- Therefore, the smallest decision tree that correctly classifies all of the training examples is best.
- Finding the provably smallest decision tree is NP-hard, so instead of constructing the absolute smallest tree consistent with the training examples, construct one that is pretty small

Learning decision trees

- Goal: Build a **decision tree** to classify examples as positive or negative instances of a concept using supervised learning from a training set

- A **decision tree** is a tree where

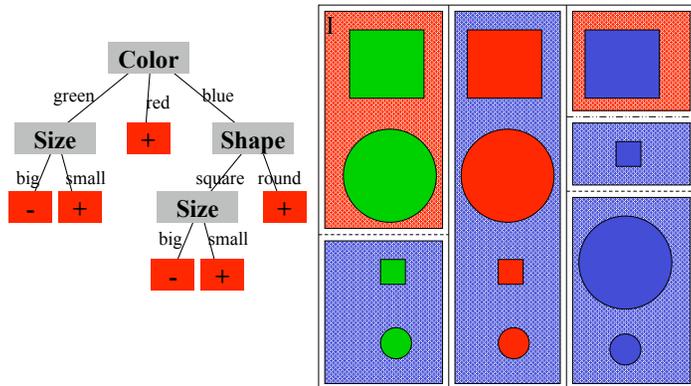
- each non-leaf node has associated with it an attribute (feature)
- each leaf node has associated with it a classification (+ or -)
- each arc has associated with it one of the possible values of the attribute at the node from which the arc is directed



- Generalization: allow for >2 classes

- e.g., for stocks, classify into {sell, hold, buy}

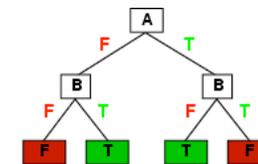
Decision tree-induced partition – example



Expressiveness

- Decision trees can express any function of the input attributes.
- E.g., for Boolean functions, truth table row → path to leaf:

A	B	A xor B
F	F	F
F	T	T
T	F	T
T	T	F



- Trivially, there is a consistent decision tree for any training set with one path to leaf for each example (unless f nondeterministic in x) but it probably won't generalize to new examples
- We prefer to find more **compact** decision trees

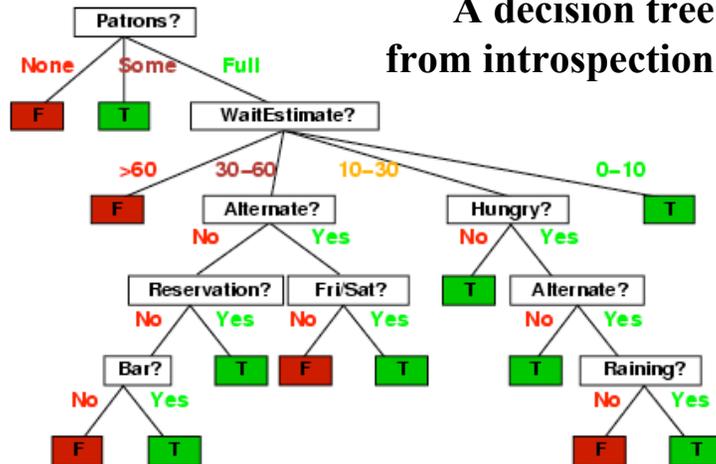
Hypothesis spaces

- **How many distinct decision trees with n Boolean attributes?**
 - = number of Boolean functions
 - = number of distinct truth tables with 2^n rows = 2^{2^n}
 - e.g., with 6 Boolean attributes, 18,446,744,073,709,551,616 trees
- **How many conjunctive hypotheses (e.g., $Hungry \wedge \neg Rain$)?**
 - Each attribute can be in (positive), in (negative), or out $\Rightarrow 3^n$ distinct conjunctive hypotheses
 - e.g., with 6 Boolean attributes, 729 trees
- **A more expressive hypothesis space**
 - increases chance that target function can be expressed
 - increases number of hypotheses consistent with training set \Rightarrow may get worse predictions in practice

R&N's restaurant domain

- Develop a decision tree to model decision a patron makes when deciding whether or not to wait for a table at a restaurant
- Two classes: wait, leave
- Ten attributes: Alternative available? Bar in restaurant? Is it Friday? Are we hungry? How full is the restaurant? How expensive? Is it raining? Do we have a reservation? What type of restaurant is it? What's the purported waiting time?
- Training set of 12 examples
- ~ 7000 possible cases

A decision tree from introspection



Attribute-based representations

Example	Attributes										Target
	Alt	Bar	Fri	Hun	Pat	Price	Rain	Res	Type	Est	Wait
X_1	T	F	F	T	Some	\$\$\$	F	T	French	0-10	T
X_2	T	F	F	T	Full	\$	F	F	Thai	30-60	F
X_3	F	T	F	F	Some	\$	F	F	Burger	0-10	T
X_4	T	F	T	T	Full	\$	F	F	Thai	10-30	T
X_5	T	F	T	F	Full	\$\$\$	F	T	French	>60	F
X_6	F	T	F	T	Some	\$\$	T	T	Italian	0-10	T
X_7	F	T	F	F	None	\$	T	F	Burger	0-10	F
X_8	F	F	F	T	Some	\$\$	T	T	Thai	0-10	T
X_9	F	T	T	F	Full	\$	T	F	Burger	>60	F
X_{10}	T	T	T	T	Full	\$\$\$	F	T	Italian	10-30	F
X_{11}	F	F	F	F	None	\$	F	F	Thai	0-10	F
X_{12}	T	T	T	T	Full	\$	F	F	Burger	30-60	T

- Examples described by **attribute values** (Boolean, discrete, continuous)
 - E.g., situations where I will/won't wait for a table
- Classification of examples is **positive** (T) or **negative** (F)
- Serves as a training set

ID3 Algorithm

- A greedy algorithm for decision tree construction developed by Ross Quinlan circa 1987
- Top-down construction of decision tree by recursively selecting “best attribute” to use at the current node in tree
 - Once attribute is selected for current node, generate child nodes, one for each possible value of selected attribute
 - Partition examples using the possible values of this attribute, and assign these subsets of the examples to the appropriate child node
 - Repeat for each child node until all examples associated with a node are either all positive or all negative

Choosing the best attribute

- Key problem: choosing which attribute to split a given set of examples
- Some possibilities are:
 - **Random:** Select any attribute at random
 - **Least-Values:** Choose the attribute with the smallest number of possible values
 - **Most-Values:** Choose the attribute with the largest number of possible values
 - **Max-Gain:** Choose the attribute that has the largest expected *information gain*—i.e., attribute that results in smallest expected size of subtrees rooted at its children
- The ID3 algorithm uses the Max-Gain method of selecting the best attribute

Restaurant example

Random: Patrons or Wait-time; Least-values: Patrons; Most-values: Type; Max-gain: ???

Type variable	French	Y	N	
	Italian	Y	N	
	Thai	N	Y	N Y
	Burger	N	Y	N Y
	Empty	Some	Full	
	Patrons variable			

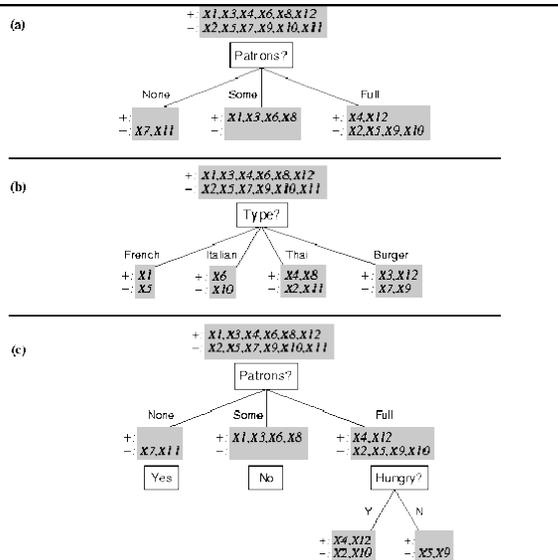
Choosing an attribute

Idea: a good attribute splits the examples into subsets that are (ideally) “all positive” or “all negative”

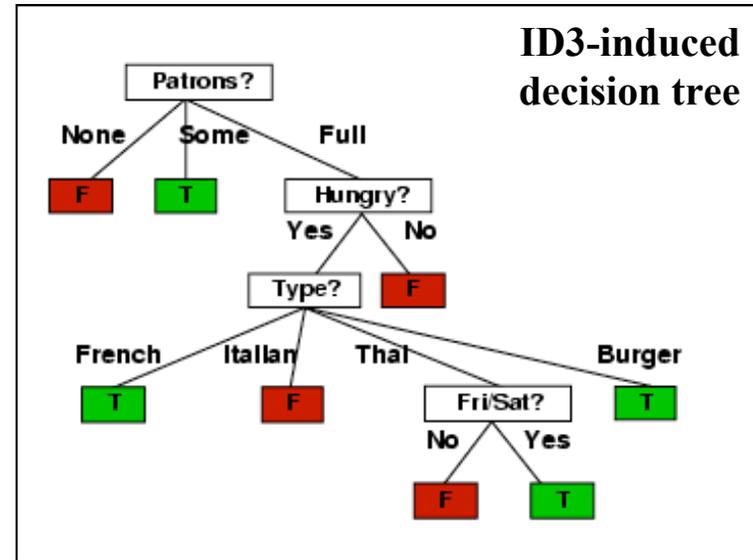


Which is better: *Patrons?* or *Type?*

Splitting examples by testing attributes



ID3-induced decision tree



Information theory 101

- Information theory sprang almost fully formed from the seminal work of Claude E. Shannon at Bell Labs
 - A Mathematical Theory of Communication, *Bell System Technical Journal*, 1948.
- Intuitions
 - Common words (a, the, dog) are shorter than less common ones (parliamentarian, foreshadowing)
 - In Morse code, common (probable) letters have shorter encodings
- Information is measured in minimum number of bits needed to store or send some information
- Wikipedia: The measure of data, known as [information entropy](#), is usually expressed by the average number of [bits](#) needed for storage or communication.

Information theory 101

- Information is measured in bits
- Information conveyed by message depends on its probability
- With n equally probable possible *messages*, the probability p of each is 1/n
- Information conveyed by message is $-\log(p) = \log(n)$
 - e.g., with 16 messages, then $\log(16) = 4$ and we need 4 bits to identify/send each message
- Given probability distribution for n messages $P = (p_1, p_2, \dots, p_n)$, the information conveyed by distribution (aka *entropy* of P) is:

$$I(P) = -(p_1 * \log(p_1) + p_2 * \log(p_2) + \dots + p_n * \log(p_n))$$

probability of msg 2 info in msg 2

Information theory II

- Information conveyed by distribution (a.k.a. *entropy* of P):

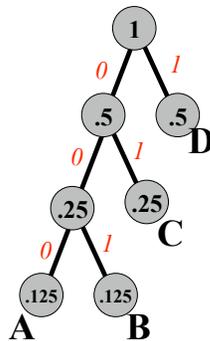
$$I(P) = -(p_1 \cdot \log(p_1) + p_2 \cdot \log(p_2) + \dots + p_n \cdot \log(p_n))$$
- Examples:
 - If P is (0.5, 0.5) then $I(P) = .5 \cdot 1 + 0.5 \cdot 1 = 1$
 - If P is (0.67, 0.33) then $I(P) = -(2/3 \cdot \log(2/3) + 1/3 \cdot \log(1/3)) = 0.92$
 - If P is (1, 0) then $I(P) = 1 \cdot 1 + 0 \cdot \log(0) = 0$
- The more uniform the probability distribution, the greater its information: More information is conveyed by a message telling you which event actually occurred
- Entropy is the average number of bits/message needed to represent a stream of messages

Huffman code

- In 1952 MIT student David Huffman devised, in the course of doing a homework assignment, an elegant coding scheme which is optimal in the case where all symbols' probabilities are integral powers of 1/2.
- A Huffman code can be built in the following manner:
 - Rank all symbols in order of probability of occurrence
 - Successively combine the two symbols of the lowest probability to form a new composite symbol; eventually we will build a binary tree where each node is the probability of all nodes beneath it
 - Trace a path to each leaf, noticing the direction at each node

Huffman code example

M	P
A	.125
B	.125
C	.25
D	.5



M	code	length	prob
A	000	3	0.125 0.375
B	001	3	0.125 0.375
C	01	2	0.250 0.500
D	1	1	0.500 0.500

average message length: 1.750

If we use this code to many messages (A,B,C or D) with this probability distribution, then, over time, the average bits/message should approach **1.75**

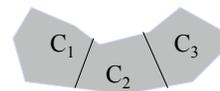
Information for classification

If a set T of records is partitioned into disjoint exhaustive classes (C_1, C_2, \dots, C_k) on the basis of the value of the class attribute, then information needed to identify class of an element of T is:

$$\text{Info}(T) = I(P)$$

where P is the probability distribution of partition (C_1, C_2, \dots, C_k):

$$P = (|C_1|/|T|, |C_2|/|T|, \dots, |C_k|/|T|)$$



High information

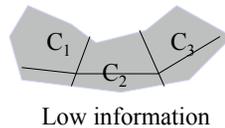
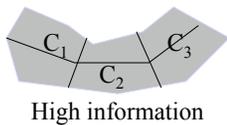


Low information

Information for classification II

If we partition T w.r.t attribute X into sets $\{T_1, T_2, \dots, T_n\}$ then the information needed to identify the class of an element of T becomes the weighted average of the information needed to identify the class of an element of T_i , i.e. the weighted average of $\text{Info}(T_i)$:

$$\text{Info}(X, T) = \sum |T_i|/|T| * \text{Info}(T_i)$$



Information gain

- Consider the quantity $\text{Gain}(X, T)$ defined as

$$\text{Gain}(X, T) = \text{Info}(T) - \text{Info}(X, T)$$
- This represents the difference between
 - info needed to identify element of T and
 - info needed to identify element of T after value of attribute X known
- This is the **gain in information due to attribute X**
- Use to rank attributes and build DT where each node uses attribute with greatest gain of those not yet considered (in path from root)
- The intent of this ordering is to:
 - Create small DTs so records can be identified with few questions
 - Match a hoped-for minimality of the process represented by the records being considered (Occam's Razor)

Computing information gain

$\begin{aligned} \mathbf{I(T)} &= \\ &= (.5 \log .5 + .5 \log .5) \\ &= .5 + .5 = 1 \end{aligned}$	French		Y	N
	Italian		Y	N
	Thai	N	Y	N Y
	Burger	N	Y	N Y
$\begin{aligned} \mathbf{I(Pat, T)} &= \\ &= 2/12 (0) + 4/12 (0) + \\ &= 6/12 (- (4/6 \log 4/6 + \\ &\quad 2/6 \log 2/6)) \\ &= 1/2 (2/3 * .6 + \\ &\quad 1/3 * 1.6) \\ &= .47 \end{aligned}$	Empty	Some	Full	
$\begin{aligned} \mathbf{I(Type, T)} &= \\ &= 2/12 (1) + 2/12 (1) + \\ &= 4/12 (1) + 4/12 (1) = 1 \end{aligned}$	$\begin{aligned} \mathbf{Gain(Pat, T)} &= 1 - .47 = .53 \\ \mathbf{Gain(Type, T)} &= 1 - 1 = 0 \end{aligned}$			

The ID3 algorithm builds a decision tree, given a set of non-categorical attributes C_1, C_2, \dots, C_n , the class attribute C, and a training set T of records

```
function ID3(R:input attributes, C:class attribute,
S:training set) returns decision tree;
    If S is empty, return single node with value Failure;
    If every example in S has same value for C, return
    single node with that value;
    If R is empty, then return a single node with most
    frequent of the values of C found in examples S;
    # causes errors -- improperly classified record
    Let D be attribute with largest Gain(D,S) among R;
    Let {dj| j=1,2, .., m} be values of attribute D;
    Let {Sj| j=1,2, .., m} be subsets of S consisting of
    records with value dj for attribute D;
    Return tree with root labeled D and arcs labeled
    d1..dm going to the trees ID3(R-{D},C,S1) . . .
    ID3(R-{D},C,Sm);
```

How well does it work?

Many case studies have shown that decision trees are at least as accurate as human experts.

- A study for diagnosing breast cancer had humans correctly classifying the examples 65% of the time; the decision tree classified 72% correct
- British Petroleum designed a decision tree for gas-oil separation for offshore oil platforms that replaced an earlier rule-based expert system
- Cessna designed an airplane flight controller using 90,000 examples and 20 attributes per example

Extensions of ID3

- Using gain ratios
- Real-valued data
- Noisy data and overfitting
- Generation of rules
- Setting parameters
- Cross-validation for experimental validation of performance
- C4.5 is an extension of ID3 that accounts for unavailable values, continuous attribute value ranges, pruning of decision trees, rule derivation, and so on

Using gain ratios

- The information gain criterion favors attributes that have a large number of values
 - If we have an attribute D that has a distinct value for each record, then $\text{Info}(D, T)$ is 0, thus $\text{Gain}(D, T)$ is maximal
- To compensate for this Quinlan suggests using the following ratio instead of Gain:

$$\text{GainRatio}(D, T) = \text{Gain}(D, T) / \text{SplitInfo}(D, T)$$
- $\text{SplitInfo}(D, T)$ is the information due to the split of T on the basis of value of categorical attribute D

$$\text{SplitInfo}(D, T) = I(|T_1|/|T|, |T_2|/|T|, \dots, |T_m|/|T|)$$
 where $\{T_1, T_2, \dots, T_m\}$ is the partition of T induced by value of D

Computing gain ratio

$$\bullet I(T) = 1$$

$$\bullet I(\text{Pat}, T) = .47$$

$$\bullet I(\text{Type}, T) = 1$$

$$\text{Gain}(\text{Pat}, T) = .53$$

$$\text{Gain}(\text{Type}, T) = 0$$

$$\text{SplitInfo}(\text{Pat}, T) = -(1/6 \log 1/6 + 1/3 \log 1/3 + 1/2 \log 1/2) = 1/6 * 2.6 + 1/3 * 1.6 + 1/2 * 1 = 1.47$$

$$\text{SplitInfo}(\text{Type}, T) = 1/6 \log 1/6 + 1/6 \log 1/6 + 1/3 \log 1/3 + 1/3 \log 1/3 = 1/6 * 2.6 + 1/6 * 2.6 + 1/3 * 1.6 + 1/3 * 1.6 = 1.93$$

$$\text{GainRatio}(\text{Pat}, T) = \text{Gain}(\text{Pat}, T) / \text{SplitInfo}(\text{Pat}, T) = .53 / 1.47 = .36$$

$$\text{GainRatio}(\text{Type}, T) = \text{Gain}(\text{Type}, T) / \text{SplitInfo}(\text{Type}, T) = 0 / 1.93 = 0$$

French		Y	N
Italian		Y	N
Thai	N	Y	N Y
Burger	N	Y	N Y
	Empty	Some	Full

Real-valued data

- Select a set of thresholds defining intervals
- Each interval becomes a discrete value of the attribute
- Use some simple heuristics...
 - always divide into quartiles
- Use domain knowledge...
 - divide age into infant (0-2), toddler (3 - 5), school-aged (5-8)
- Or treat this as another learning problem
 - Try a range of ways to discretize the continuous variable and see which yield “better results” w.r.t. some metric
 - E.g., try midpoint between every pair of values

Noisy data

- Many kinds of “noise” can occur in the examples:
- Two examples have same attribute/value pairs, but different classifications
- Some values of attributes are incorrect because of errors in the data acquisition process or the preprocessing phase
- The classification is wrong (e.g., + instead of -) because of some error
- Some attributes are irrelevant to the decision-making process, e.g., color of a die is irrelevant to its outcome

Overfitting

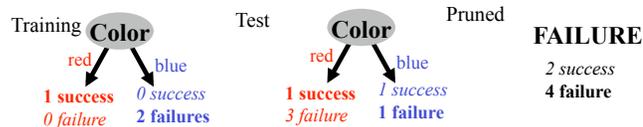
- Irrelevant attributes, can result in *overfitting* the training example data
- If hypothesis space has many dimensions (large number of attributes), we may find **meaningless regularity** in the data that is irrelevant to the true, important, distinguishing features
- If we have too little training data, even a reasonable hypothesis space will ‘overfit’

Overfitting

- Fix by removing irrelevant features
 - E.g., remove ‘year observed’, ‘month observed’, ‘day observed’, ‘observer name’ from feature vector
- Fix by getting more training data
- Fix by pruning lower nodes in the decision tree
 - E.g., if gain of the best attribute at a node is below a threshold, stop and make this node a leaf rather than generating children nodes

Pruning decision trees

- Pruning of the decision tree is done by replacing a whole subtree by a leaf node
- The replacement takes place if a decision rule establishes that the expected error rate in the subtree is greater than in the single leaf. E.g.,
 - Training: one training red success and two training blue failures
 - Test: three red failures and one blue success
 - Consider replacing this subtree by a single Failure node.
- After replacement we will have only two errors instead of five:



Converting decision trees to rules

- It is easy to derive rules from a decision tree: write a rule for each path from the root to a leaf
- In that rule the left-hand side is built from the label of the nodes and the labels of the arcs
- The resulting rules set can be simplified:
 - Let LHS be the left hand side of a rule
 - LHS' obtained from LHS by eliminating some conditions
 - Replace LHS by LHS' in this rule if the subsets of the training set satisfying LHS and LHS' are equal
 - A rule may be eliminated by using meta-conditions such as "if no other rule applies"

<http://archive.ics.uci.edu/ml>

UCI Machine Learning Repository

UCI Machine Learning Repository

Center for Machine Learning and Intelligent Systems

Welcome to the UC Irvine Machine Learning Repository!

We currently maintain 187 data sets as a service to the machine learning community. You may view all data sets through our searchable interface. Our old web site is still available, for those who prefer the old format. For a general overview of the Repository, please visit our About page. For information about citing data sets in publications, please read our citation policy. If you wish to donate a data set, please consult our donation policy. For any other questions, feel free to contact the Repository librarians. We have also set up a mirror site for the Repository.

Supported By: In Collaboration With:

Latest News:

- 10-16-2009: Two new data sets have been added.
- 09-21-2009: The Netflix Prize data set is now available.
- 09-14-2009: Several data sets have been added.
- 07-23-2008: Repository mirror has been set up.
- 03-24-2008: New data sets have been added!

Newest Data Sets:

- 10-15-2009: URL Reputation
- 10-07-2009: Wine Quality
- 09-21-2009: Netflix Prize

Most Popular Data Sets (hits since 2007):

- 100631: Iris
- 77391: Adult
- 67481: Wine

Example: zoo data

UCI Machine Learning Repository: Zoo Data Set

UCI Machine Learning Repository

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Zoo Data Set

Download: [Data Folder](#) [Data Set Description](#)

Abstract: Artificial, 7 classes of animals

Data Set Characteristics:	Multivariate	Number of Instances:	101	Area:	Life
Attribute Characteristics:	Categorical, Integer	Number of Attributes:	17	Date Donated:	1990-05-15
Associated Tasks:	Classification	Missing Values?	No	Number of Web Hits:	18038

<http://archive.ics.uci.edu/ml/datasets/Zoo>

animal name: string
 hair: Boolean
 feathers: Boolean
 eggs: Boolean
 milk: Boolean
 airborne: Boolean
 aquatic: Boolean
 predator: Boolean
 toothed: Boolean
 backbone: Boolean
 breathes: Boolean
 venomous: Boolean
 fins: Boolean
 legs: {0,2,4,5,6,8}
 tail: Boolean
 domestic: Boolean
 catsize: Boolean
 type: {mammal, fish, bird, shellfish, insect, reptile, amphibian}

Zoo data

101 examples

```

aardvark,1,0,0,1,0,0,1,1,1,1,0,0,4,0,0,1,mammal
antelope,1,0,0,1,0,0,0,1,1,1,0,0,4,1,0,1,mammal
bass,0,0,1,0,0,1,1,1,1,0,0,1,0,1,0,0,fish
bear,1,0,0,1,0,0,1,1,1,1,0,0,4,0,0,1,mammal
boar,1,0,0,1,0,0,1,1,1,1,0,0,4,1,0,1,mammal
buffalo,1,0,0,1,0,0,0,1,1,1,0,0,4,1,0,1,mammal
calf,1,0,0,1,0,0,0,1,1,1,0,0,4,1,1,1,mammal
carp,0,0,1,0,0,1,0,1,1,0,0,1,0,1,1,0,fish
catfish,0,0,1,0,0,1,1,1,1,0,0,1,0,1,0,0,fish
cavy,1,0,0,1,0,0,0,1,1,1,0,0,4,0,1,0,mammal
cheetah,1,0,0,1,0,0,1,1,1,1,0,0,4,1,0,1,mammal
chicken,0,1,1,0,1,0,0,0,1,1,0,0,2,1,1,0,bird
chub,0,0,1,0,0,1,1,1,1,0,0,1,0,1,0,0,fish
clam,0,0,1,0,0,0,1,0,0,0,0,0,0,0,0,0,shellfish
crab,0,0,1,0,0,1,1,0,0,0,0,0,4,0,0,0,shellfish
...
  
```

Zoo example

```

aima-python> python
>>> from learning import *
>>> zoo
<DataSet(zoo): 101 examples, 18 attributes>
>>> dt = DecisionTreeLearner()
>>> dt.train(zoo)
>>> dt.predict(['shark',0,0,1,0,0,1,1,1,1,0,0,1,0,1,0,0])
'fish'
>>> dt.predict(['shark',0,0,0,0,0,1,1,1,1,0,0,1,0,1,0,0])
'mammal'
  
```

Zoo example

```

>> dt.dt
DecisionTree(13, 'legs', {0: DecisionTree(12, 'fins', {0:
DecisionTree(8, 'toothed', {0: 'shellfish', 1: 'reptile'}), 1:
DecisionTree(3, 'eggs', {0: 'mammal', 1: 'fish'})}), 2:
DecisionTree(1, 'hair', {0: 'bird', 1: 'mammal'}), 4:
DecisionTree(1, 'hair', {0: DecisionTree(6, 'aquatic', {0:
'reptile', 1: DecisionTree(8, 'toothed', {0: 'shellfish', 1:
'amphibian'})}), 1: 'mammal'}), 5: 'shellfish', 6:
DecisionTree(6, 'aquatic', {0: 'insect', 1: 'shellfish'}), 8:
'shellfish'})
  
```

Zoo example

```

>>> dt.dt.display()
Test legs
legs = 0 ==> Test fins
  fins = 0 ==> Test toothed
    toothed = 0 ==> RESULT = shellfish
    toothed = 1 ==> RESULT = reptile
  fins = 1 ==> Test eggs
    eggs = 0 ==> RESULT = mammal
    eggs = 1 ==> RESULT = fish
legs = 2 ==> Test hair
  hair = 0 ==> RESULT = bird
  hair = 1 ==> RESULT = mammal
legs = 4 ==> Test hair
  hair = 0 ==> Test aquatic
    aquatic = 0 ==> RESULT = reptile
    aquatic = 1 ==> Test toothed
      toothed = 0 ==> RESULT = shellfish
      toothed = 1 ==> RESULT = amphibian
  hair = 1 ==> RESULT = mammal
legs = 5 ==> RESULT = shellfish
legs = 6 ==> Test aquatic
  aquatic = 0 ==> RESULT = insect
  aquatic = 1 ==> RESULT = shellfish
legs = 8 ==> RESULT = shellfish
  
```

```

>>> dt.dt.display()
Test legs
legs = 0 ==> Test fins
  fins = 0 ==> Test toothed
    toothed = 0 ==> RESULT = shellfish
    toothed = 1 ==> RESULT = reptile
  fins = 1 ==> Test milk
    milk = 0 ==> RESULT = fish
    milk = 1 ==> RESULT = mammal
legs = 2 ==> Test hair
  hair = 0 ==> RESULT = bird
  hair = 1 ==> RESULT = mammal
legs = 4 ==> Test hair
  hair = 0 ==> Test aquatic
    aquatic = 0 ==> RESULT = reptile
    aquatic = 1 ==> Test toothed
      toothed = 0 ==> RESULT = shellfish
      toothed = 1 ==> RESULT = amphibian
  hair = 1 ==> RESULT = mammal
legs = 5 ==> RESULT = shellfish
legs = 6 ==> Test aquatic
  aquatic = 0 ==> RESULT = insect
  aquatic = 1 ==> RESULT = shellfish
legs = 8 ==> RESULT = shellfish

```

Zoo example

Add the shark example
to the training set and
retrain

Evaluation methodology

- Standard methodology:
 1. Collect large set of examples with correct classifications
 2. Randomly divide collection into two disjoint sets: *training* and *test*
 3. Apply learning algorithm to training set giving hypothesis H
 4. Measure performance of H w.r.t. test set
- Important: keep the training and test sets disjoint!
- Study efficiency and robustness of algorithm: repeat steps 2-4 for different training sets and sizes of training sets
- On modifying algorithm, restart with step 1 to avoid evolving algorithm to work well on just this collection

K-fold Cross Validation

- Problem: getting “ground truth” data can be expensive
- Problem: ideally need different test data each time we test
- Problem: experimentation is needed to find right “feature space” and parameters for ML algorithm
- Goal: minimize amount of training+test data needed
- Idea: split training data into K subsets, use K-1 for *training*, and one for *development testing*
- Common K values are 5 and 10

Zoo evaluation

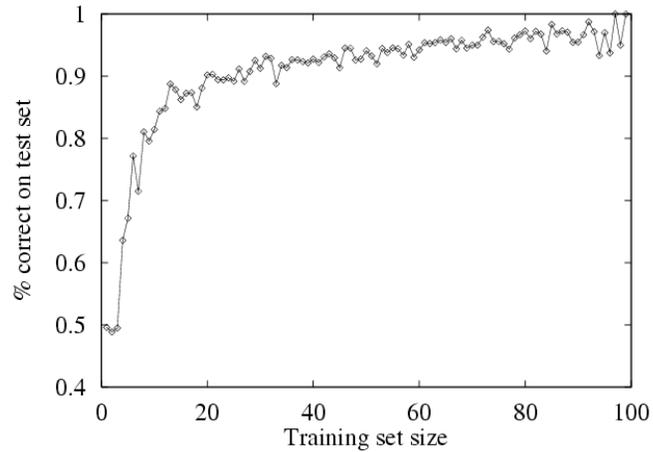
```

>>> train_and_test(DecisionTreeLearner(), zoo, 0, 10)
1.0
>>> train_and_test(DecisionTreeLearner(), zoo, 90, 100)
0.80000000000000004
>>> train_and_test(DecisionTreeLearner(), zoo, 90, 101)
0.81818181818181823
>>> train_and_test(DecisionTreeLearner(), zoo, 80, 90)
0.90000000000000002
>>> cross_validation(DecisionTreeLearner(), zoo, 10, 20)
0.95500000000000007
>>> leave1out(DecisionTreeLearner(), zoo)
0.97029702970297027

```

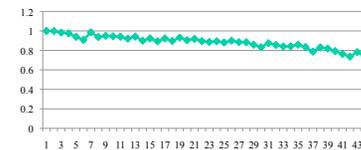
Learning curve

Learning curve = % correct on test set as a function of training set size



Zoo

```
>>> learningcurve(DecisionTreeLearner(), zoo)
[(2, 1.0), (4, 1.0), (6, 0.9833333333333333), (8,
0.9749999999999999), (10, 0.9400000000000000), (12,
0.9083333333333333), (14, 0.9857142857142857), (16,
0.9375), (18, 0.9499999999999999), (20,
0.9449999999999999), ... (86, 0.78255813953488373), (88,
0.7363636363636364), (90, 0.7077777777777778)]
```



Summary: Decision tree learning

- Inducing decision trees is one of the most widely used learning methods in practice
- Can out-perform human experts in many problems
- Strengths include
 - Fast
 - Simple to implement
 - Can convert result to a set of easily interpretable rules
 - Empirically valid in many commercial products
 - Handles noisy data
- Weaknesses include:
 - Univariate splits/partitioning using only one attribute at a time so limits types of possible trees
 - Large decision trees may be hard to understand
 - Requires fixed-length feature vectors
 - Non-incremental (i.e., batch method)