# 1

# INTRODUCTION

**R**obotics is a relatively young field of modern technology that crosses traditional engineering boundaries. Understanding the complexity of robots and their applications requires knowledge of electrical engineering, mechanical engineering, systems and industrial engineering, computer science, economics, and mathematics. New disciplines of engineering, such as manufacturing engineering, applications engineering, and knowledge engineering have emerged to deal with the complexity of the field of robotics and factory automation.

This book is concerned with fundamentals of robotics, including **kinematics**, **dynamics**, **motion planning**, **computer vision**, and **control**. Our goal is to provide a complete introduction to the most important concepts in these subjects as applied to industrial robot manipulators, mobile robots, and other mechanical systems. A complete treatment of the discipline of robotics would require several volumes. Nevertheless, at the present time, the majority of robot applications deal with industrial robot arms operating in structured factory environments so that a first introduction to the subject of robotics must include a rigorous treatment of the topics in this text.

The term **robot** was first introduced into our vocabulary by the Czech playwright Karel Capek in his 1920 play *Rossum's Universal Robots*, the word *robota* being the Czech word for work. Since then the term has been applied to a great variety of mechanical devices, such as teleoperators, underwater vehicles, autonomous land rovers, etc. Virtually anything that operates with some degree of autonomy, usually under computer control, has at some point been called a robot. In this text the term robot will mean a computer controlled industrial manipulator of the type shown in Figure 1.1. This type of robot is

*Fig. 1.1*   The ABB IRB6600 Robot. Photo courtesy of ABB.

essentially a mechanical arm operating under computer control. Such devices, though far from the robots of science fiction, are nevertheless extremely complex electro-mechanical systems whose analytical description requires advanced methods, presenting many challenging and interesting research problems.

An official definition of such a robot comes from the **Robot Institute of America** (RIA): *A robot is a reprogrammable multifunctional manipulator designed to move material, parts, tools, or specialized devices through variable programmed motions for the performance of a variety of tasks.*

The key element in the above definition is the reprogrammability of robots. It is the computer brain that gives the robot its utility and adaptability. The so-called robotics revolution is, in fact, part of the larger computer revolution.

Even this restricted version of a robot has several features that make it attractive in an industrial environment. Among the advantages often cited in favor of the introduction of robots are decreased labor costs, increased precision and productivity, increased flexibility compared with specialized machines, and more humane working conditions as dull, repetitive, or hazardous jobs are performed by robots.

The robot, as we have defined it, was born out of the marriage of two earlier technologies: **teleoperators** and **numerically controlled milling machines**. Teleoperators, or master-slave devices, were developed during the second world war to handle radioactive materials. Computer numerical control (CNC) was developed because of the high precision required in the machining of certain items, such as components of high performance aircraft. The first

robots essentially combined the mechanical linkages of the teleoperator with the autonomy and programmability of CNC machines.

The first successful applications of robot manipulators generally involved some sort of material transfer, such as injection molding or stamping, where the robot merely attends a press to unload and either transfer or stack the finished parts. These first robots could be programmed to execute a sequence of movements, such as moving to a location A, closing a gripper, moving to a location B, etc., but had no external sensor capability. More complex applications, such as welding, grinding, deburring, and assembly require not only more complex motion but also some form of external sensing such as vision, tactile, or force-sensing, due to the increased interaction of the robot with its environment.

It should be pointed out that the important applications of robots are by no means limited to those industrial jobs where the robot is directly replacing a human worker. There are many other applications of robotics in areas where the use of humans is impractical or undesirable. Among these are undersea and planetary exploration, satellite retrieval and repair, the defusing of explosive devices, and work in radioactive environments. Finally, prostheses, such as artificial limbs, are themselves robotic devices requiring methods of analysis and design similar to those of industrial manipulators.

## 1.1   MATHEMATICAL MODELING OF ROBOTS

While robots are themselves mechanical systems, in this text we will be primarily concerned with developing and manipulating mathematical models for robots. In particular, we will develop methods to represent basic geometric aspects of robotic manipulation, dynamic aspects of manipulation, and the various sensors available in modern robotic systems. Equipped with these mathematical models, we will be able to develop methods for planning and controlling robot motions to perform specified tasks. Here we describe some of the basic ideas that are common in developing mathematical models for robot manipulators.

### 1.1.1   Symbolic Representation of Robots

Robot Manipulators are composed of **links** connected by **joints** to form a **kinematic chain**. Joints are typically rotary (revolute) or linear (prismatic). A **revolute** joint is like a hinge and allows relative rotation between two links. A **prismatic** joint allows a linear relative motion between two links. We denote revolute joints by $R$ and prismatic joints by $P$, and draw them as shown in Figure 1.2. For example, a three-link arm with three revolute joints is an RRR arm.

Each joint represents the interconnection between two links. We denote the axis of rotation of a revolute joint, or the axis along which a prismatic joint translates by $z_i$ if the joint is the interconnection of links $i$ and $i + 1$. The
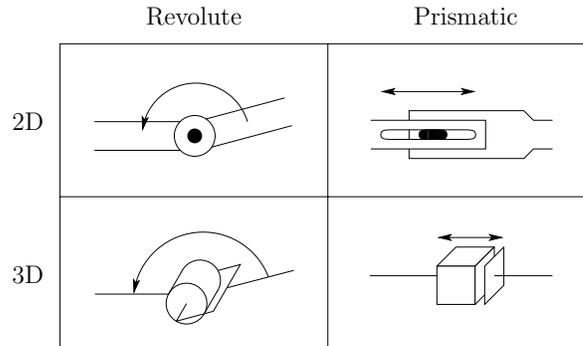
*Fig. 1.2*   Symbolic representation of robot joints.

**joint variables**, denoted by $\theta$ for a revolute joint and $d$ for the prismatic joint, represent the relative displacement between adjacent links. We will make this precise in Chapter 3.

### 1.1.2   The Configuration Space

A **configuration** of a manipulator is a complete specification of the location of every point on the manipulator. The set of all possible configurations is called the **configuration space**. In our case, if we know the values for the joint variables (i.e., the joint angle for revolute joints, or the joint offset for prismatic joints), then it is straightforward to infer the position of any point on the manipulator, since the individual links of the manipulator are assumed to be rigid, and the base of the manipulator is assumed to be fixed. Therefore, in this text, we will represent a configuration by a set of values for the joint variables. We will denote this vector of values by $q$, and say that the robot is in configuration $q$ when the joint variables take on the values $q_1 \cdots q_n$, with $q_i = \theta_i$ for a revolute joint and $q_i = d_1$ for a prismatic joint.

An object is said to have $n$ **degrees-of-freedom** (DOF) if its configuration can be minimally specified by $n$ parameters. Thus, the number of DOF is equal to the dimension of the configuration space. For a robot manipulator, the number of joints determines the number DOF. A rigid object in three-dimensional space has six DOF: three for **positioning** and three for **orientation** (e.g., roll, pitch and yaw angles). Therefore, a manipulator should typically possess at least six independent DOF. With fewer than six DOF the arm cannot reach every point in its work environment with arbitrary orientation. Certain applications such as reaching around or behind obstacles may require more than six DOF. A manipulator having more than six links is referred to as a **kinematically redundant** manipulator. The difficulty of controlling a manipulator increases rapidly with the number of links.

### 1.1.3 The State Space

A configuration provides an instantaneous description of the geometry of a manipulator, but says nothing about its dynamic response. In contrast, the **state** of the manipulator is a set of variables that, together with a description of the manipulator's dynamics and input, are sufficient to determine any future state of the manipulator. The **state space** is the set of all possible states. In the case of a manipulator arm, the dynamics are Newtonian, and can be specified by generalizing the familiar equation $F = ma$. Thus, a state of the manipulator can be specified by giving the values for the joint variables $q$ and for joint velocities $\dot{q}$ (acceleration is related to the derivative of joint velocities). We typically represent the state as a vector $x = (q, \dot{q})^T$. The dimension of the state space is thus $2n$ if the system has $n$ DOF.

### 1.1.4 The Workspace

The **workspace** of a manipulator is the total volume swept out by the end-effector as the manipulator executes all possible motions. The workspace is constrained by the geometry of the manipulator as well as mechanical constraints on the joints. For example, a revolute joint may be limited to less than a full 360° of motion. The workspace is often broken down into a **reachable workspace** and a **dexterous workspace**. The reachable workspace is the entire set of points reachable by the manipulator, whereas the dexterous workspace consists of those points that the manipulator can reach with an arbitrary orientation of the end-effector. Obviously the dexterous workspace is a subset of the reachable workspace. The workspaces of several robots are shown later in this chapter.

## 1.2 ROBOTS AS MECHANICAL DEVICES

There are a number of physical aspects of robotic manipulators that we will not necessarily consider when developing our mathematical models. These include mechanical aspects (e.g., how are the joints actually implemented), accuracy and repeatability, and the tooling attached at the end effector. In this section, we briefly describe some of these.

### 1.2.1 Classification of Robotic Manipulators

Robot manipulators can be classified by several criteria, such as their **power source**, or way in which the joints are actuated, their **geometry**, or kinematic structure, their intended **application area**, or their **method of control**. Such classification is useful primarily in order to determine which robot is right for a given task. For example, a hydraulic robot would not be suitable for food handling or clean room applications. We explain this in more detail below.

*Power Source.*   Typically, robots are either electrically, hydraulically, or pneumatically powered. Hydraulic actuators are unrivaled in their speed of response and torque producing capability. Therefore hydraulic robots are used primarily for lifting heavy loads. The drawbacks of hydraulic robots are that they tend to leak hydraulic fluid, require much more peripheral equipment (such as pumps, which require more maintenance), and they are noisy. Robots driven by DC- or AC-servo motors are increasingly popular since they are cheaper, cleaner and quieter. Pneumatic robots are inexpensive and simple but cannot be controlled precisely. As a result, pneumatic robots are limited in their range of applications and popularity.

*Application Area.*   Robots are often classified by application into **assembly** and **non-assembly robots**. Assembly robots tend to be small, electrically driven and either revolute or SCARA (described below) in design. The main nonassembly application areas to date have been in welding, spray painting, material handling, and machine loading and unloading.

*Method of Control.*   Robots are classified by control method into **servo** and **non-servo** robots. The earliest robots were non-servo robots. These robots are essentially open-loop devices whose movement is limited to predetermined mechanical stops, and they are useful primarily for materials transfer. In fact, according to the definition given previously, fixed stop robots hardly qualify as robots. Servo robots use closed-loop computer control to determine their motion and are thus capable of being truly multifunctional, reprogrammable devices.

Servo controlled robots are further classified according to the method that the controller uses to guide the end-effector. The simplest type of robot in this class is the **point-to-point** robot. A point-to-point robot can be taught a discrete set of points but there is no control on the path of the end-effector in between taught points. Such robots are usually taught a series of points with a teach pendant. The points are then stored and played back. Point-to-point robots are severely limited in their range of applications. In **continuous path** robots, on the other hand, the entire path of the end-effector can be controlled. For example, the robot end-effector can be taught to follow a straight line between two points or even to follow a contour such as a welding seam. In addition, the velocity and/or acceleration of the end-effector can often be controlled. These are the most advanced robots and require the most sophisticated computer controllers and software development.

*Geometry.*   Most industrial manipulators at the present time have six or fewer degrees-of-freedom. These manipulators are usually classified kinematically on the basis of the first three joints of the arm, with the wrist being described separately. The majority of these manipulators fall into one of five geometric types: **articulated (RRR)**, **spherical (RRP)**, **SCARA (RRP)**, **cylindrical (RPP)**, or **Cartesian (PPP)**. We discuss each of these below.

Each of these five manipulator arms are **serial link** robots. A sixth distinct class of manipulators consists of the so-called **parallel robot**. In a parallel manipulator the links are arranged in a closed rather than open kinematic chain. Although we include a brief discussion of parallel robots in this chapter, their kinematics and dynamics are more difficult to derive than those of serial link robots and hence are usually treated only in more advanced texts.

### 1.2.2 Robotic Systems

A robot manipulator should be viewed as more than just a series of mechanical linkages. The mechanical arm is just one component in an overall **Robotic System**, illustrated in Figure 1.3, which consists of the **arm**, **external power**
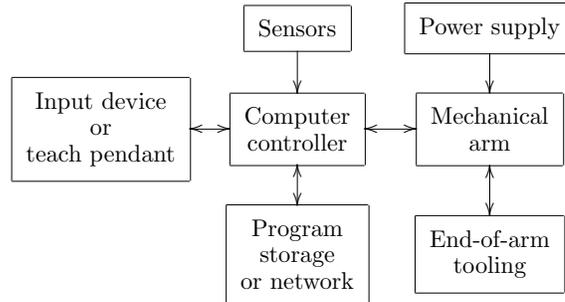


*Fig. 1.3*   Components of a robotic system.

**source**, **end-of-arm tooling**, **external and internal sensors**, **computer interface**, and **control computer**. Even the programmed software should be considered as an integral part of the overall system, since the manner in which the robot is programmed and controlled can have a major impact on its performance and subsequent range of applications.

### 1.2.3 Accuracy and Repeatability

The **accuracy** of a manipulator is a measure of how close the manipulator can come to a given point within its workspace. **Repeatability** is a measure of how close a manipulator can return to a previously taught point. The primary method of sensing positioning errors in most cases is with position encoders located at the joints, either on the shaft of the motor that actuates the joint or on the joint itself. There is typically no direct measurement of the end-effector position and orientation. One must rely on the assumed geometry of the manipulator and its rigidity to infer (i.e., to calculate) the end-effector position from the measured joint positions. Accuracy is affected therefore by computational errors, machining accuracy in the construction of the manipulator, flexibility effects such as the bending of the links under gravitational and other loads,

gear backlash, and a host of other static and dynamic effects. It is primarily for this reason that robots are designed with extremely high rigidity. Without high rigidity, accuracy can only be improved by some sort of direct sensing of the end-effector position, such as with vision.

Once a point is taught to the manipulator, however, say with a teach pendant, the above effects are taken into account and the proper encoder values necessary to return to the given point are stored by the controlling computer. Repeatability therefore is affected primarily by the controller resolution. **Controller resolution** means the smallest increment of motion that the controller can sense. The resolution is computed as the total distance traveled by the tip divided by $2^n$, where $n$ is the number of bits of encoder accuracy. In this context, linear axes, that is, prismatic joints, typically have higher resolution than revolute joints, since the straight line distance traversed by the tip of a linear axis between two points is less than the corresponding arc length traced by the tip of a rotational link.

In addition, as we will see in later chapters, rotational axes usually result in a large amount of kinematic and dynamic coupling among the links with a resultant accumulation of errors and a more difficult control problem. One may wonder then what the advantages of revolute joints are in manipulator design. The answer lies primarily in the increased dexterity and compactness of revolute joint designs. For example, Figure 1.4 shows that for the same range of motion,
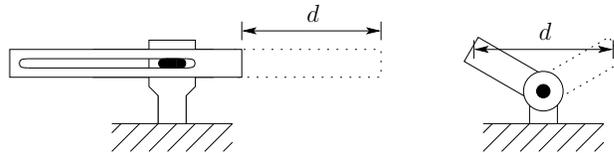


*Fig. 1.4*   Linear vs. rotational link motion.

a rotational link can be made much smaller than a link with linear motion. Thus manipulators made from revolute joints occupy a smaller working volume than manipulators with linear axes. This increases the ability of the manipulator to work in the same space with other robots, machines, and people. At the same time revolute joint manipulators are better able to maneuver around obstacles and have a wider range of possible applications.

### 1.2.4   Wrists and End-Effectors

The joints in the kinematic chain between the arm and end effector are referred to as the **wrist**. The wrist joints are nearly always all revolute. It is increasingly common to design manipulators with **spherical wrists**, by which we mean wrists whose three joint axes intersect at a common point. The spherical wrist is represented symbolically in Figure 1.5.
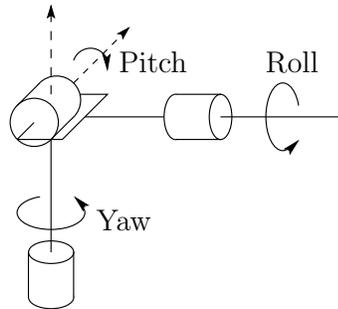
***Fig. 1.5***  Structure of a spherical wrist.

The spherical wrist greatly simplifies the kinematic analysis, effectively allowing one to decouple the positioning and orientation of the end effector. Typically therefore, the manipulator will possess three degrees-of-freedom for position, which are produced by three or more joints in the arm. The number of degrees-of-freedom for orientation will then depend on the degrees-of-freedom of the wrist. It is common to find wrists having one, two, or three degrees-of-freedom depending of the application. For example, the SCARA robot shown in Figure 1.14 has four degrees-of-freedom: three for the arm, and one for the wrist, which has only a rotation about the final $z$-axis.

It has been said that a robot is only as good as its **hand** or **end-effector**. The arm and wrist assemblies of a robot are used primarily for positioning the end-effector and any tool it may carry. It is the end-effector or tool that actually performs the work. The simplest type of end-effectors are grippers, which usually are capable of only two actions, **opening** and **closing**. While this is adequate for materials transfer, some parts handling, or gripping simple tools, it is not adequate for other tasks such as welding, assembly, grinding, etc. A great deal of research is therefore devoted to the design of special purpose end-effectors as well as to tools that can be rapidly changed as the task dictates. There is also much research on the development of anthropomorphic hands. Such hands have been developed both for prosthetic use and for use in manufacturing. Since we are concerned with the analysis and control of the manipulator itself and not in the particular application or end-effector, we will not discuss end-effector design or the study of grasping and manipulation.

## 1.3  COMMON KINEMATIC ARRANGEMENTS OF MANIPULATORS

Although there are many possible ways use prismatic and revolute joints to construct kinematic chains, in practice only a few of these are commonly used. Here we briefly describe several arrangements that are most typical.

### 1.3.1    Articulated manipulator (RRR)

The articulated manipulator is also called a **revolute**, or **anthropomorphic** manipulator. The ABB IRB1400 articulated arm is shown in Figure 1.6. A



*Fig. 1.6*   The ABB IRB1400 Robot. Photo courtesy of ABB.

common revolute joint design is the **parallelogram linkage** such as the Motoman SK16, shown in Figure 1.7. In both of these arrangements joint axis



*Fig. 1.7*   The Motoman SK16 manipulator.

$z_2$ is parallel to $z_1$ and both $z_1$ and $z_2$ are perpendicular to $z_0$. This kind of manipulator is known as an elbow manipulator. The structure and terminology associated with the elbow manipulator are shown in Figure 1.8. Its workspace is shown in Figure 1.9.

The revolute manipulator provides for relatively large freedom of movement in a compact space. The parallelogram linkage, although typically less dexterous than the elbow manipulator manipulator, nevertheless has several advantages that make it an attractive and popular design. The most notable feature of the
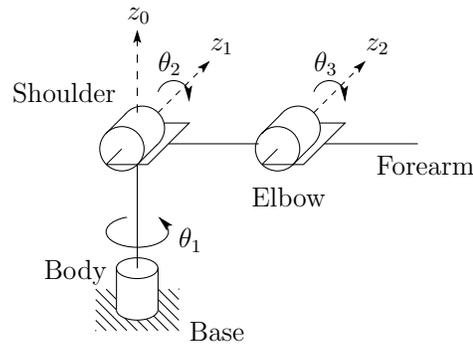
*Fig. 1.8*   Structure of the elbow manipulator.
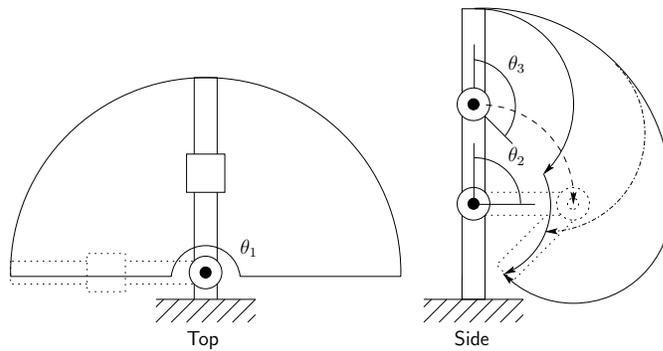


*Fig. 1.9*   Workspace of the elbow manipulator.

parallelogram linkage manipulator is that the actuator for joint 3 is located on link 1. Since the weight of the motor is born by link 1, links 2 and 3 can be made more lightweight and the motors themselves can be less powerful. Also the dynamics of the parallelogram manipulator are simpler than those of the elbow manipulator, thus making it easier to control.

### 1.3.2   Spherical Manipulator (RRP)

By replacing the third or elbow joint in the revolute manipulator by a prismatic joint one obtains the spherical manipulator shown in Figure 1.10. The term **spherical manipulator** derives from the fact that the spherical coordinates defining the position of the end-effector with respect to a frame whose origin lies at the intersection of the three $z$ axes are the same as the first three joint variables. Figure 1.11 shows the Stanford Arm, one of the most well-
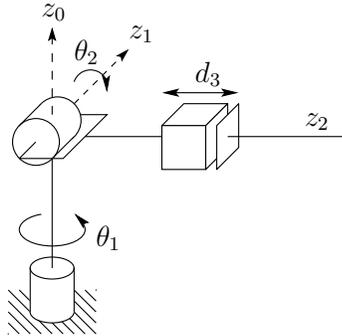
*Fig. 1.10*   The spherical manipulator.

known spherical robots.  The workspace of a spherical manipulator is shown in
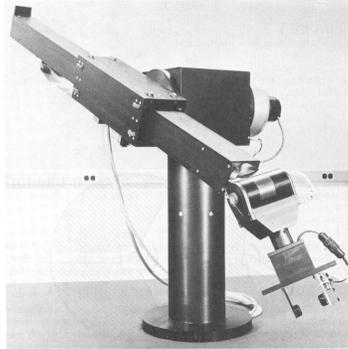


*Fig. 1.11*   The Stanford Arm. Photo courtesy of the Coordinated Science Lab, University of Illinois at Urbana-Champaign.

Figure 1.12.

### 1.3.3   SCARA Manipulator (RRP)

The **SCARA** arm (for **S**elective **C**ompliant **A**rticulated **R**obot for **A**ssembly) shown in Figure 1.13 is a popular manipulator, which, as its name suggests, is tailored for assembly operations. Although the SCARA has an RRP structure, it is quite different from the spherical manipulator in both appearance and in its range of applications. Unlike the spherical design, which has $z_0$ perpendicular to $z_1$, and $z_1$ perpendicular to $z_2$, the SCARA has $z_0, z_1$, and $z_2$ mutually parallel. Figure 1.14 shows the Epson E2L653S, a manipulator of this type. The SCARA manipulator workspace is shown in Figure 1.15.
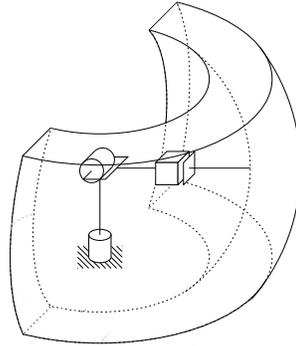
*Fig. 1.12* Workspace of the spherical manipulator.
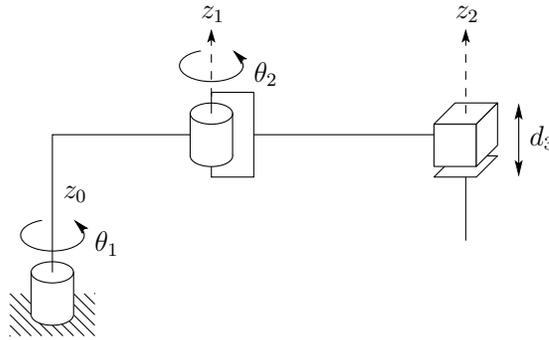


*Fig. 1.13* The SCARA (Selective Compliant Articulated Robot for Assembly).

### 1.3.4 Cylindrical Manipulator (RPP)

The cylindrical manipulator is shown in Figure 1.16. The first joint is revolute and produces a rotation about the base, while the second and third joints are prismatic. As the name suggests, the joint variables are the cylindrical coordinates of the end-effector with respect to the base. A cylindrical robot, the Seiko RT3300, is shown in Figure 1.17, with its workspace shown in Figure 1.18.

*Fig. 1.14*   The Epson E2L653S SCARA Robot. Photo Courtesy of Epson.
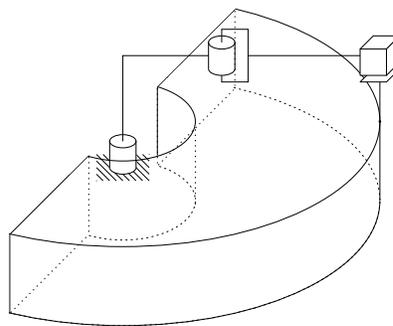


*Fig. 1.15*   Workspace of the SCARA manipulator.

### 1.3.5   Cartesian manipulator (PPP)

A manipulator whose first three joints are prismatic is known as a Cartesian manipulator, shown in Figure 1.19.

For the Cartesian manipulator the joint variables are the Cartesian coordinates of the end-effector with respect to the base. As might be expected the kinematic description of this manipulator is the simplest of all manipulators. Cartesian manipulators are useful for table-top assembly applications and, as gantry robots, for transfer of material or cargo. An example of a Cartesian robot, from Epson-Seiko, is shown in Figure 1.20. The workspace of a Cartesian manipulator is shown in Figure 1.21.
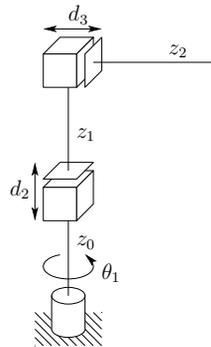
*Fig. 1.16*   The cylindrical manipulator.



*Fig. 1.17*   The Seiko RT3300 Robot. Photo courtesy of Seiko.

### 1.3.6   Parallel Manipulator

A **parallel manipulator** is one in which some subset of the links form a closed chain. More specifically, a parallel manipulator has two or more independent kinematic chains connecting the base to the end-effector. Figure 1.22 shows the ABB IRB 940 Tricept robot, which is a parallel manipulator. The closed chain kinematics of parallel robots can result in greater structural rigidity, and hence greater accuracy, than open chain robots. The kinematic description of parallel robots is fundamentally different from that of serial link robots and therefore requires different methods of analysis.
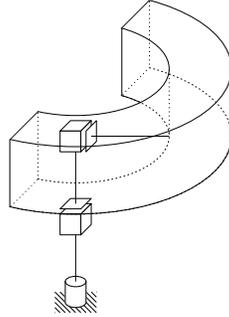
*Fig. 1.18*   Workspace of the cylindrical manipulator.
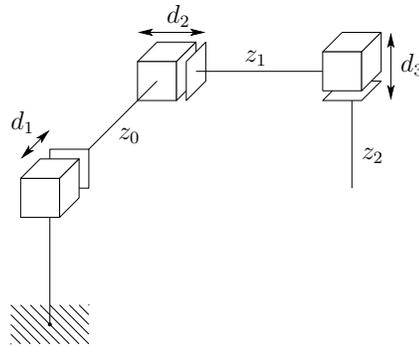


*Fig. 1.19*   The Cartesian manipulator.

## 1.4   OUTLINE OF THE TEXT

A typical application involving an industrial manipulator is shown in Figure 1.23. The manipulator is shown with a grinding tool that it must use to remove a certain amount of metal from a surface. In the present text we are concerned with the following question: *What are the basic issues to be resolved and what must we learn in order to be able to program a robot to perform such tasks?*

The ability to answer this question for a full six degree-of-freedom manipulator represents the goal of the present text. The answer is too complicated to be presented at this point. We can, however, use the simple two-link planar mechanism to illustrate some of the major issues involved and to preview the topics covered in this text.

*Fig. 1.20*   The Epson Cartesian Robot. Photo courtesy of Epson.
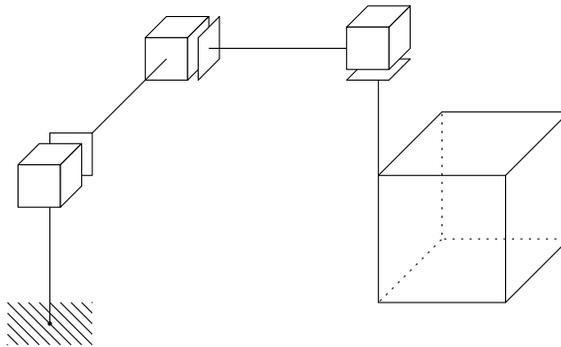


*Fig. 1.21*   Workspace of the Cartesian manipulator.

Suppose we wish to move the manipulator from its **home** position to position $A$, from which point the robot is to follow the contour of the surface $S$ to the point $B$, at constant velocity, while maintaining a prescribed force $F$ normal to the surface. In so doing the robot will cut or grind the surface according to a predetermined specification. To accomplish this and even more general tasks, a we must solve a number of problems. Below we give examples of these problems, all of which will be treated in more detail in the remainder of the text.

### Forward Kinematics

The first problem encountered is to describe both the position of the tool and the locations $A$ and $B$ (and most likely the entire surface $S$) with respect to a common coordinate system. In Chapter 2 we give some background on repre-