## Machine Learning:

## Decision Trees

## Chapter 18.1-18.3

Some material adopted from notes
by Chuck Dyer

## What is learning?

- "Learning denotes changes in a system that ... enable a system to do the same task more efficiently the next time" - $\underline{\text { Herbert Simon }}$
- "Learning is constructing or modifying representations of what is being experienced" - Ryszard Michalski
- "Learning is making useful changes in our minds" - Marvin Minsky


## Why study learning?

- Understand and improve efficiency of human learning
- Use to improve methods for teaching and tutoring people (e.g., better computer-aided instruction)
- Discover new things or structure previously unknown
- Examples: data mining, scientific discovery
- Fill in skeletal or incomplete specifications in a domain
- Large, complex systems can't be completely built by hand \& require dynamic updating to incorporate new information
- Learning new characteristics expands the domain or expertise and lessens the "brittleness" of the system
- Build agents that can adapt to users, other agents, and their environment


## AI \& Learning Today

- Neural network learning was popular in the 60 s
- In the 70s and 80s it was replaced with a paradigm based on manually encoding and using knowledge
- In the 90s, more data and the Web drove interest in new statistical machine learning (ML) techniques and new data mining applications
- Today, ML techniques and big data are behind almost all successful intelligent systems



## Machine Leaning Successes

- Sentiment analysis
- Spam detection
- Machine translation
- Spoken language understanding
- Named entity detection
- Self driving cars
- Motion recognition (Microsoft X-Box)
- Identifying paces in digital images
- Recommender systems (Netflix, Amazon)
- Credit card fraud detection


## A general model of learning agents

Performance standard


## Major paradigms of machine learning

- Rote learning - One-to-one mapping from inputs to stored representation. "Learning by memorization." Association-based storage and retrieval.
- Induction - Use specific examples to reach general conclusions
- Clustering - Unsupervised identification of natural groups in data
- Analogy - Determine correspondence between two different representations
- Discovery - Unsupervised, specific goal not given
- Genetic algorithms - "Evolutionary" search techniques, based on an analogy to "survival of the fittest"
- Reinforcement - Feedback (positive or negative reward) given at the end of a sequence of steps


## The Classification Problem



- Extrapolate from set of examples to make accurate predictions about future ones
- Supervised versus unsupervised learning
- Learn unknown function $f(X)=Y$, where $X$ is an input example and Y is desired output
- Supervised learning implies we're given a training set of (X, Y) pairs by a "teacher"
- Unsupervised learning means we are only given the Xs and some (ultimate) feedback function on our performance.
- Concept learning or classification (aka "induction")
- Given a set of examples of some concept/class/category, determine if a given example is an instance of the concept or not
- If it is an instance, we call it a positive example
- If it is not, it is called a negative example
- Or we can make a probabilistic prediction (e.g., using a Bayes net)


## Supervised Concept Learning



- Given a training set of positive and negative examples of a concept
- Construct a description that will accurately classify whether future examples are positive or negative
- That is, learn some good estimate of function $f$ given a training set $\left\{\left(\mathrm{x}_{1}, \mathrm{y}_{1}\right),\left(\mathrm{x}_{2}, \mathrm{y}_{2}\right), \ldots,\left(\mathrm{x}_{\mathrm{n}}, \mathrm{y}_{\mathrm{n}}\right)\right\}$, where each $y_{i}$ is either + (positive) or - (negative), or a probability distribution over +/-


## Inductive Learning Framework



- Raw input data from sensors are typically preprocessed to obtain a feature vector, X , that adequately describes all of the relevant features for classifying examples
- Each x is a list of (attribute, value) pairs. For example,
X = [Person:Sue, EyeColor:Brown, Age:Young, Sex:Female]
- The number of attributes (a.k.a. features) is fixed (positive, finite)
- Each attribute has a fixed, finite number of possible values (or could be continuous)
- Each example can be interpreted as a point in an
n -dimensional feature space, where n is the number of attributes


## Measuring Model Quality

- How good is a model?
- Predictive accuracy
- False positives / false negatives for a given cutoff threshold
- Loss function (accounts for cost of different types of errors)
- Area under the (ROC) curve
- Minimizing loss can lead to problems with overfitting
- Training error
- Train on all data; measure error on all data
- Subject to overfitting (of course we' 11 make good predictions on the data on which we trained!)
- Regularization
- Attempt to avoid overfitting
- Explicitly minimize the complexity of the function while minimizing loss. Tradeoff is modeled with a regularization parameter


## Cross-Validation

- Holdout cross-validation:
- Divide data into training set and test set
- Train on training set; measure error on test set
- Better than training error, since we are measuring generalization to new data
- To get a good estimate, we need a reasonably large test set
- But this gives less data to train on, reducing our model quality!


## Cross-Validation, cont.

- k-fold cross-validation:
- Divide data into $k$ folds
- Train on $k-1$ folds, use the $k$ th fold to measure error
- Repeat $k$ times; use average error to measure generalization accuracy
- Statistically valid and gives good accuracy estimates
- Leave-one-out cross-validation (LOOCV)
- $k$-fold cross validation where $k=N$ (test data $=1$ instance!)
- Quite accurate, but also quite expensive, since it requires building $N$ models


## Inductive learning as search

- Instance space I defines the language for the training and test instances
- Typically, but not always, each instance $\mathrm{i} \in \mathrm{I}$ is a feature vector
- Features are sometimes called attributes or variables
- I: $V_{1} \times V_{2} \times \ldots \times V_{k}, i=\left(v_{1}, v_{2}, \ldots, v_{k}\right)$
- Class variable $C$ gives an instance's class (to be predicted)
- Model space M defines the possible classifiers
$-\mathrm{M}: \mathrm{I} \rightarrow \mathrm{C}, \mathrm{M}=\{\mathrm{ml}, \ldots \mathrm{mn}\}$ (possibly infinite)
- Model space is sometimes, but not always, defined in terms of the same features as the instance space
- Training data can be used to direct the search for a good (consistent, complete, simple) hypothesis in the model space


## Model spaces

- Decision trees
- Partition the instance space into axis-parallel regions, labeled with class value
- Version spaces
- Search for necessary (lower-bound) and sufficient (upper-bound) partial instance descriptions for an instance to be in the class
- Nearest-neighbor classifiers
- Partition the instance space into regions defined by the centroid instances (or cluster of $k$ instances)
- Associative rules (feature values $\rightarrow$ class)
- First-order logical rules
- Bayesian networks (probabilistic dependencies of class on attributes)
- Neural networks


## Model spaces



## Learning decision trees

- Goal: Build a decision tree to classify examples as positive or negative instances of a concept using supervised learning from a training set
- A decision tree is a tree where
- each non-leaf node has associated with it an attribute (feature)
-each leaf node has associated with it a classification (+ or -)
-each arc has associated with it one
 at the node from which the arc is directed
- Generalization: allow for $>2$ classes -e.g., for stocks, classify into \{sell, hold, buy\}


## Decision tree-induced partition - example



## Expressiveness

- Decision trees can express any function of the input attributes
- E.g., for Boolean functions, truth table row $\rightarrow$ path to leaf:

- Trivially, there's a consistent decision tree for any training set with one path to leaf for each example (unless $f$ nondeterministic in $x$ ), but it probably won't generalize to new examples
- We prefer to find more compact decision trees


## Inductive learning and bias $\frac{(\text { (a) }}{0}$

- Suppose that we want to learn a function $f(x)=y$ and we are given some sample ( $x, y$ ) pairs, as in figure (a)
- There are several hypotheses we could make about this function, e.g.: (b), (c) and (d)
- A preference for one over the others reveals the bias of our learning technique, e.g.:
- prefer piece-wise functions
- prefer a smooth function
- prefer a simple function and treat outliers as noise


## Preference bias: Ockham's Razor

- AKA Occam's Razor, Law of Economy, or Law of Parsimony
- Principle stated by William of Ockham (1285-1347)
- "non sunt multiplicanda entia praeter necessitatem"
- entities are not to be multiplied beyond necessity
- The simplest consistent explanation is the best
- Therefore, the smallest decision tree that correctly classifies all of the training examples is best
- Finding the provably smallest decision tree is NPhard, so instead of constructing the absolute smallest tree consistent with the training examples, construct one that is pretty small


## Hypothesis spaces

- How many distinct decision trees with $\boldsymbol{n}$ Boolean attributes?
$-=$ number of Boolean functions
$-=$ number of distinct truth tables with $2^{\mathrm{n}}$ rows $=2^{2^{\mathrm{n}}}$
- e.g., with 6 Boolean attributes, 18,446,744,073,709,551,616 trees
- How many conjunctive hypotheses (e.g., Hungry ^ ᄀRain)?
- Each attribute can be in (positive), in (negative), or out
$\Rightarrow 3^{\mathrm{n}}$ distinct conjunctive hypotheses
- e.g., with 6 Boolean attributes, 729 trees
- A more expressive hypothesis space
- increases chance that target function can be expressed
- increases number of hypotheses consistent with training set
$\Rightarrow$ may get worse predictions in practice


## R\&N's restaurant domain

- Develop a decision tree to model decision a patron makes when deciding whether or not to wait for a table at a restaurant
- Two classes: wait, leave
- Ten attributes: Alternative available? Bar in restaurant? Is it Friday? Are we hungry? How full is the restaurant? How expensive? Is it raining? Do we have a reservation? What type of restaurant is it? What' s the purported waiting time?
- Training set of 12 examples
- ~ 7000 possible cases



## Attribute-based representations

| Example | Target |  |  |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | Alt | Bar | Fri | Hun | Pat | Price | Rain | Res | Type | Est | Wait |
| $X_{1}$ | T | F | F | T | Some | $\$ \$ \$$ | F | T | French | $0-10$ | T |
| $X_{2}$ | T | F | F | T | Full | $\$$ | F | F | Thai | $30-60$ | F |
| $X_{3}$ | F | T | F | F | Some | $\$$ | F | F | Burger | $0-10$ | T |
| $X_{4}$ | T | F | T | T | Full | $\$$ | F | F | Thai | $10-30$ | T |
| $X_{5}$ | T | F | T | F | Full | $\$ \$ \$$ | F | T | French | $>60$ | F |
| $X_{6}$ | F | T | F | T | Some | $\$ \$$ | T | T | Italian | $0-10$ | T |
| $X_{7}$ | F | T | F | F | None | $\$$ | T | F | Burger | $0-10$ | F |
| $X_{8}$ | F | F | F | T | Some | $\$ \$$ | T | T | Thai | $0-10$ | T |
| $X_{9}$ | F | T | T | F | Full | $\$$ | T | F | Burger | $>60$ | F |
| $X_{10}$ | T | T | T | T | Full | $\$ \$ \$$ | F | T | Italian | $10-30$ | F |
| $X_{11}$ | F | F | F | F | None | $\$$ | F | F | Thai | $0-10$ | F |
| $X_{12}$ | T | T | T | T | Full | $\$$ | F | F | Burger | $30-60$ | T |

- Examples described by attribute values (Boolean, discrete, continuous), e.g., situations where I will/won't wait for a table
- Classification of examples is positive (T) or negative (F)
- Serves as a training set


## ID3/C4.5 Algorithm

- A greedy algorithm for decision tree construction developed by Ross Quinlan circa 1987
- Top-down construction of decision tree by recursively selecting "best attribute" to use at the current node in tree
- Once attribute is selected for current node, generate child nodes, one for each possible value of selected attribute
- Partition examples using the possible values of this attribute, and assign these subsets of the examples to the appropriate child node
- Repeat for each child node until all examples associated with a node are either all positive or all negative


## Choosing the best attribute

- Key problem: choosing which attribute to split a given set of examples
- Some possibilities are:
- Random: Select any attribute at random
- Least-Values: Choose the attribute with the smallest number of possible values
- Most-Values: Choose the attribute with the largest number of possible values
- Max-Gain: Choose the attribute that has the largest expected information gain-i.e., attribute that results in smallest expected size of subtrees rooted at its children
- The ID3 algorithm uses the Max-Gain method of selecting the best attribute


## Choosing an attribute

Idea: a good attribute splits the examples into subsets that are (ideally) "all positive" or "all negative"



Which is better: Patrons? or Type?

## Restaurant example

Random: Patrons or Wait-time; Least-values: Patrons; Most-values: Type; Max-gain: ???



# ID3-induced 



Full


## Compare the two Decision Trees



## Information theory 101

- Information theory sprang almost fully formed from the seminal work of Claude E. Shannon at Bell Labs A Mathematical Theory of Communication, Bell System Technical Journal, 1948.
- Intuitions
- Common words (a, the, dog) shorter than less common ones (parlimentarian, foreshadowing)
- Morse code: common (probable) letters have shorter encodings
- Information is measured in minimum number of bits needed to store or send some information
- Wikipedia: The measure of data, known as information entropy, is usually expressed by the average number of bits needed for storage or communication.


## Information theory 101

- Information is measured in bits
- Information conveyed by message depends on its probability
- For $n$ equally probable possible messages, each has prob. $1 / n$
- Information conveyed by message is $-\log (\mathrm{p})=\log (\mathrm{n})$
e.g., with 16 messages, then $\log (16)=4$ and we need 4 bits to identify/send each message
- Given probability distribution for n messages $\mathrm{P}=\left(\mathrm{p}_{1}, \mathrm{p}_{2} \ldots \mathrm{p}_{\mathrm{n}}\right)$, the information conveyed by distribution (aka entropy of P ) is: $\mathrm{I}(\mathrm{P})=-\left(\mathrm{p}_{1}{ }^{*} \log \left(\mathrm{p}_{1}\right)+\mathrm{p}_{2} * \log \left(\mathrm{p}_{2}\right)+. .+\mathrm{p}_{\mathrm{n}}{ }^{*} \log \left(\mathrm{p}_{\mathrm{n}}\right)\right)$


## Information theory II

- Information conveyed by distribution (aka entropy of P ):

$$
\mathrm{I}(\mathrm{P})=-\left(\mathrm{p}_{1} * \log \left(\mathrm{p}_{1}\right)+\mathrm{p}_{2} * \log \left(\mathrm{p}_{2}\right)+. .+\mathrm{p}_{\mathrm{n}}{ }^{*} \log \left(\mathrm{p}_{\mathrm{n}}\right)\right)
$$

- Examples:
- If P is $(0.5,0.5)$ then $\mathrm{I}(\mathrm{P})=.5^{*} 1+0.5^{*} 1=1$
- If P is $(0.67,0.33)$ then $\mathrm{I}(\mathrm{P})=-(2 / 3 * \log (2 / 3)+$ $1 / 3 * \log (1 / 3))=0.92$
- If P is $(1,0)$ then $\mathrm{I}(\mathrm{P})=1 * 1+0 * \log (0)=0$
- The more uniform the probability distribution, the greater its information: more information is conveyed by a message telling you which event actually occurred
- Entropy is the average number of bits/message needed to represent a stream of messages


## Example: Huffman code

- In 1952 MIT student David Huffman devised, in the course of doing a homework assignment, an elegant coding scheme which is optimal in the case where all symbols' probabilities are integral powers of $1 / 2$.
- A Huffman code can be built in the following manner:
- Rank all symbols in order of probability of occurrence
- Successively combine the two symbols of the lowest probability to form a new composite symbol; eventually we will build a binary tree where each node is the probability of all nodes beneath it
- Trace a path to each leaf, noticing direction at each node


## Huffman code example

M $\quad \mathbf{P}$
A .125
B .125
C .25
D .5

| M | code length |  |  | prob |
| :--- | ---: | ---: | ---: | ---: |
| A | 000 | 3 | 0.125 | 0.375 |
| B | 001 | 3 | 0.125 | 0.375 |
| C | 01 | 2 | 0.250 | 0.500 |
| D | 1 | 1 | 0.500 | 0.500 |
| namana maconma lanoth |  |  |  | 1750 |

If we use this code to many messages ( $\mathrm{A}, \mathrm{B}, \mathrm{C}$ or D ) with this probability distribution, then, over time, the average bits/message should approach 1.75

## Information for classification

If a set T of records is partitioned into disjoint exhaustive classes $\left(\mathrm{C}_{1}, \mathrm{C}_{2}, . ., \mathrm{C}_{\mathrm{k}}\right)$ on the basis of the value of the class attribute, then information needed to identify class of an element of T is:

$$
\operatorname{Info}(\mathrm{T})=\mathrm{I}(\mathrm{P})
$$

where P is the probability distribution of partition $\left(\mathrm{C}_{1}, \mathrm{C}_{2}, . ., \mathrm{C}_{\mathrm{k}}\right)$ :

$$
\mathrm{P}=\left(\left|\mathrm{C}_{1}\right| /|\mathrm{T}|,\left|\mathrm{C}_{2}\right| /|\mathrm{T}|, \ldots,\left|\mathrm{C}_{\mathrm{k}}\right| /|\mathrm{T}|\right)
$$



Low information
High information

## Information for classification II

If we partition $T$ w.r.t attribute $X$ into sets $\left\{\mathrm{T}_{1}, \mathrm{~T}_{2}, . ., \mathrm{T}_{\mathrm{n}}\right\}$ then the information needed to identify the class of an element of T becomes the weighted average of the information needed to identify the class of an element of $T_{i}$, i.e. the weighted average of $\operatorname{Info}\left(\mathrm{T}_{\mathrm{i}}\right)$ :

$$
\operatorname{Info}(\mathrm{X}, \mathrm{~T})=\sum_{\left|\mathrm{T}_{\mathrm{i}}\right| /|\mathrm{T}| *} \operatorname{Info}\left(\mathrm{~T}_{\mathrm{i}}\right)
$$



High information


Low information

## Information gain

- Consider the quantity Gain(X,T) defined as

$$
\operatorname{Gain}(\mathrm{X}, \mathrm{~T})=\operatorname{Info}(\mathrm{T})-\operatorname{Info}(\mathrm{X}, \mathrm{~T})
$$

- This represents the difference between
- info needed to identify element of T and
- info needed to identify element of T after value of attribute X known
- This is the gain in information due to attribute $X$
- Use to rank attributes and build DT where each node uses attribute with greatest gain of those not yet considered (in path from root)
- The intent of this ordering is to:
- Create small DTs so records can be identified with few questions
- Match a hoped-for minimality of the process represented by the records being considered (Occam's Razor)


## Computing Information Gain

$$
\begin{aligned}
& \cdot \mathrm{I}(\mathrm{~T})=? \\
& \cdot \mathrm{I}(\text { Pat, } \mathrm{T})=\text { ? } \\
& \cdot \mathrm{I}(\text { Type, } \mathrm{T})=?
\end{aligned}
$$

| French |  | Y | N |
| :---: | :---: | :---: | :---: |
| Italian |  | Y | N |
| Thai | N | Y | N Y |
| Burger | N | Y | N Y |
|  | Empty | Some | Full |

$\operatorname{Gain}(\operatorname{Pat}, \mathbf{T})=?$
$\operatorname{Gain}(\operatorname{Type}, T)=?$

## Computing information gain

$$
\begin{aligned}
& =.47
\end{aligned}
$$

I (Type, $\mathbf{T})=$
2/12 (1) + 2/12 (1) +
$4 / 12(1)+4 / 12(1)=1$

Gain (Pat, $\mathbf{T})=1-.47=.53$
Gain $($ Type, $T)=1-1=0$

The ID3 algorithm builds a decision tree, given a set of non-categorical attributes $\mathrm{C} 1, \mathrm{C} 2, \ldots$, Cn , the class attribute C , and a training set T of records
function ID3(R:input attributes, C:class attribute, S:training set) returns decision tree;

If $S$ is empty, return single node with value Failure;
If every example in $S$ has same value for $C$, return single node with that value;
If $R$ is empty, then return a single node with most frequent of the values of $C$ found in examples $S$;
\# causes errors -- improperly classified record
Let $D$ be attribute with largest $G a i n(D, S)$ among $R$;
Let $\{d j \mid j=1,2, \ldots, m\}$ be values of attribute $D ;$
Let $\left\{S_{j} \mid j=1,2, \ldots, m\right\}$ be subsets of $S$ consisting of records with value dj for attribute D;
Return tree with root labeled $D$ and arcs labeled d1..dm going to the trees ID3 (R-\{D\}, C, S1). ID3 (R-\{D\}, C, Sm) ;

## How well does it work?

Many case studies have shown that decision trees are at least as accurate as human experts.

- A study for diagnosing breast cancer had humans correctly classifying the examples $65 \%$ of the time; the decision tree classified $72 \%$ correct
-British Petroleum designed a decision tree for gasoil separation for offshore oil platforms that replaced an earlier rule-based expert system
-Cessna designed an airplane flight controller using 90,000 examples and 20 attributes per example


## Extensions of ID3

- Using gain ratios
- Real-valued data
- Noisy data and overfitting
- Generation of rules
- Setting parameters
- Cross-validation for experimental validation of performance
- C4.5 is an extension of ID3 that accounts for unavailable values, continuous attribute value ranges, pruning of decision trees, rule derivation, and so on


## Using gain ratios

- The information gain criterion favors attributes that have a large number of values
- If we have an attribute D that has a distinct value for each record, then $\operatorname{Info}(\mathrm{D}, \mathrm{T})$ is 0 , thus $\operatorname{Gain}(\mathrm{D}, \mathrm{T})$ is maximal
- To compensate for this Quinlan suggests using the following ratio instead of Gain:
GainRatio(D,T) $=\operatorname{Gain}(\mathrm{D}, \mathrm{T}) / \operatorname{SplitInfo}(\mathrm{D}, \mathrm{T})$
- $\operatorname{SplitInfo}(\mathrm{D}, \mathrm{T})$ is the information due to the split of T on the basis of value of categorical attribute D

SplitInfo(D, T$)=\mathrm{I}(|\mathrm{T} 1| /|\mathrm{T}|,|\mathrm{T} 2| /|\mathrm{T}|, . .,|\mathrm{Tm}| /|\mathrm{T}|)$
where $\{\mathrm{T} 1, \mathrm{~T} 2, . . \mathrm{Tm}\}$ is the partition of T induced by value of D

## Computing gain ratio

$\cdot \mathrm{I}(\mathrm{T})=1$
-I $(\mathrm{Pat}, \mathrm{T})=.47$
-I $($ Type, $T)=1$

Gain (Pat, T) $=.53$
Gain $($ Type, $T)=0$

| French |  | Y | N |
| :---: | :---: | :---: | :---: |
| Italian |  | Y | N |
| Thai | N | Y | N Y |
| Burger | N | Y | NY |
|  | Empty | Some | Full |

SplitInfo $($ Pat, $T)=-(1 / 6 \log 1 / 6+1 / 3 \log 1 / 3+1 / 2 \log 1 / 2)=1 / 6 * 2.6+1 / 3 * 1.6+1 / 2 * 1$ $=1.47$

SplitInfo $($ Type, $T)=1 / 6 \log 1 / 6+1 / 6 \log 1 / 6+1 / 3 \log 1 / 3+1 / 3 \log 1 / 3$

$$
=1 / 6 * 2.6+1 / 6 * 2.6+1 / 3 * 1.6+1 / 3 * 1.6=1.93
$$

GainRatio $($ Pat, $T)=$ Gain $($ Pat, $T) / \operatorname{SplitInfo}($ Pat, $T)=.53 / 1.47=.36$
GainRatio $($ Type, $T)=$ Gain $($ Type,$T) /$ SplitInfo $($ Type, $T)=0 / 1.93=0$

## Real-valued data

- Select a set of thresholds defining intervals
- Each interval becomes a discrete value of the attribute
- Use some simple heuristics...
- always divide into quartiles
- Use domain knowledge...
- divide age into infant (0-2), toddler (3-5), school-aged (5-8)
- Or treat this as another learning problem
- Try a range of ways to discretize the continuous variable and see which yield "better results" w.r.t. some metric
- E.g., try midpoint between every pair of values


## Noisy data

- Many kinds of "noise" can occur in the examples:
- Two examples have same attribute/value pairs, but different classifications
- Some values of attributes are incorrect because of errors in the data acquisition process or the preprocessing phase
- The classification is wrong (e.g., + instead of -) because of some error
- Some attributes are irrelevant to the decision-making process, e.g., color of a die is irrelevant to its outcome


## Overfitting

- Irrelevant attributes, can result in overfitting the training example data
- If hypothesis space has many dimensions (large number of attributes), we may find meaningless regularity in the data that is irrelevant to the true, important, distinguishing features
- If we have too little training data, even a reasonable hypothesis space will 'overfit'


## Overfitting

- Fix by by removing irrelevant features
- E.g., remove ‘year observed’, ‘month observed', 'day observed', 'observer name' from feature vector
- Fix by getting more training data
- Fix by pruning lower nodes in the decision tree
- E.g., if gain of the best attribute at a node is below a threshold, stop and make this node a leaf rather than generating children nodes


## Pruning decision trees

- Pruning of the decision tree is done by replacing a whole subtree by a leaf node
- The replacement takes place if a decision rule establishes that the expected error rate in the subtree is greater than in the single leaf. E.g.,
- Training: one training red success and two training blue failures
- Test: three red failures and one blue success
- Consider replacing this subtree by a single Failure node.
- After replacement we will have only two errors instead of five:



FAILURE
2 success
4 failure

## Converting decision trees to rules

- It is easy to derive rules from a decision tree: write a rule for each path from the root to a leaf
- In that rule the left-hand side is built from the label of the nodes and the labels of the arcs
- The resulting rules set can be simplified:
- Let LHS be the left hand side of a rule
- LHS' obtained from LHS by eliminating some conditions
- Replace LHS by LHS' in this rule if the subsets of the training set satisfying LHS and LHS' are equal
- A rule may be eliminated by using meta-conditions such as "if no other rule applies"
$\leftarrow \rightarrow C$
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## Latest News:

2010-03-01: Note from donor regarding Netflix data
2009-10-16: Two new data sets have been added.
2009-09-14: Several data sets have been added.
2008-07-23: Repository mirror has been set up.
2008-03-24: New data sets have been added!
2007-06-25: Two new data sets have been added: UJI Pen Characters, MAGIC Gamma Telescope
2007-04-13: Research papers that cite the repository have been associated to specific data sets.

## Featured Data Set: Yeast



Task: Classification Data Type: Multivariate
\# Attributes: 8 \# Instances: 1484


## Zoo Data Set

Download: Data Folder, Data Set Description
Abstract: Artificial, 7 classes of animals

## http://archive.ics.uci.edu/ml/datasets/Zoo

| Data Set <br> Characteristics: | Multivariate | Number of <br> Instances: | 101 | Area: | Life |
| :--- | :--- | :--- | :--- | :--- | :--- |
| Attribute <br> Characteristics: | Categorical, <br> Integer | Number of <br> Attributes: | 17 | Date Donated | $1990-05-$ <br> 15 |
| Associated Tasks: | Classification | Missing Values? | No | Number of Web <br> Hits: | 18038 |

animal name: string hair: Boolean feathers: Boolean eggs: Boolean milk: Boolean airborne: Boolean aquatic: Boolean
predator: Boolean toothed: Boolean backbone: Boolean breathes: Boolean venomous: Boolean fins: Boolean legs: $\{0,2,4,5,6,8\}$ tail: Boolean domestic: Boolean catsize: Boolean type: \{mammal, fish, bird, shellfish, insect, reptile, amphibian $\}$

## Zoo data

## 101 examples

aardvark, $1,0,0,1,0,0,1,1,1,1,0,0,4,0,0,1$, mammal antelope, $1,0,0,1,0,0,0,1,1,1,0,0,4,1,0,1, \mathrm{mammal}$ bass, $0,0,1,0,0,1,1,1,1,0,0,1,0,1,0,0$, fish bear, $1,0,0,1,0,0,1,1,1,1,0,0,4,0,0,1, \mathrm{mammal}$ boar, $1,0,0,1,0,0,1,1,1,1,0,0,4,1,0,1, \mathrm{mammal}$ buffalo, $1,0,0,1,0,0,0,1,1,1,0,0,4,1,0,1$, mammal calf, $1,0,0,1,0,0,0,1,1,1,0,0,4,1,1,1, \mathrm{mammal}$ carp, $0,0,1,0,0,1,0,1,1,0,0,1,0,1,1,0$, fish catfish, $0,0,1,0,0,1,1,1,1,0,0,1,0,1,0,0$, fish cavy, $1,0,0,1,0,0,0,1,1,1,0,0,4,0,1,0, \mathrm{mammal}$ cheetah, $1,0,0,1,0,0,1,1,1,1,0,0,4,1,0,1, \mathrm{mammal}$ chicken, $0,1,1,0,1,0,0,0,1,1,0,0,2,1,1,0$, bird chub, $0,0,1,0,0,1,1,1,1,0,0,1,0,1,0,0$, fish clam, $0,0,1,0,0,0,1,0,0,0,0,0,0,0,0,0$, shellfish crab, $0,0,1,0,0,1,1,0,0,0,0,0,4,0,0,0$, shellfish

## Zoo example

aima-python> python
$\ggg$ from learning import *
>>> zoo
$<$ DataSet(zoo): 101 examples, 18 attributes $>$
$\ggg \mathrm{dt}=$ DecisionTreeLearner()
$\ggg$ dt.train(zoo)
>>> dt.predict(['shark',0,0,1,0,0,1,1,1,1,0,0,1,0,1,0,0])
'fish'
>>> dt.predict(['shark', $0,0,0,0,0,1,1,1,1,0,0,1,0,1,0,0])$
'mammal'

## Zoo example

$\gg d t . d t$
DecisionTree(13, 'legs', $\{0$ : DecisionTree(12, 'fins', $\{0$ : DecisionTree( 8 , 'toothed', $\{0$ : 'shellfish', 1 : 'reptile' $\}$ ), 1 : DecisionTree(3, 'eggs', $\{0$ : 'mammal', 1: 'fish'\}) \}), 2: DecisionTree(1, 'hair', \{0: 'bird', 1: 'mammal'\}), 4:
DecisionTree(1, 'hair', \{0: DecisionTree(6, 'aquatic', \{0: 'reptile', 1: DecisionTree(8, 'toothed', \{0: 'shellfish', 1: 'amphibian'\})\}), 1: 'mammal'\}), 5: 'shellfish', 6:
DecisionTree(6, 'aquatic', \{0: 'insect', 1: 'shellfish'\} ), 8: 'shellfish'\})
>>> dt.dt.display()
Test legs

```
legs =0==> Test fins
    fins =0 ==> Test toothed
        toothed =0 =}>>\mathrm{ RESULT }=\mathrm{ shellfish
        toothed = 1 ==> RESULT = reptile
    fins = 1 ==> Test eggs
        eggs =0 ==> RESULT = mammal
        eggs = 1 ==> RESULT = fish
legs =2 ==> Test hair
    hair = 0 ==> RESULT = bird
    hair = 1 ==> RESULT = mammal
legs = 4 ==> Test hair
    hair =0==> Test aquatic
        aquatic =0 = > RESULT = reptile
        aquatic =1 ==> Test toothed
            toothed =0 ==> RESULT = shellfish
            toothed = 1 ==> RESULT = amphibian
    hair = 1 ==> RESULT = mammal
legs =5 ==> RESULT = shellfish
legs =6 ==> Test aquatic
    aquatic = 0 = P RESULT = insect
    aquatic = 1 ==> RESULT = shellfish
legs = 8 ==> RESULT = shellfish
```

Zoo example
>>> dt.dt.display()
Test legs

```
legs = 0==> Test fins
    fins =0 ==> Test toothed
        toothed =0 ==> RESULT = shellfish
        toothed = 1 ==> RESULT = reptile
    fins = 1 ==> Test milk
        milk =0==> RESULT = fish
        milk = 1 ==> RESULT = mammal
legs =2 ==> Test hair
    hair =0 ==> RESULT = bird
    hair = 1 ==> RESULT = mammal
legs =4 ==> Test hair
    hair =0==> Test aquatic
        aquatic =0 ==> RESULT = reptile
        aquatic =1 ==> Test toothed
            toothed =0 ==> RESULT = shellfish
            toothed = 1 ==> RESULT = amphibian
    hair = 1 ==> RESULT = mammal
legs =5 => RESULT = shellfish
legs =6 ==> Test aquatic
    aquatic =0 => RESULT = insect
    aquatic = 1 ==> RESULT = shellfish
legs = 8 ==> RESULT = shellfish
```

                    Zoo example
    Add the shark example
to the training set and
retrain

## Summary: Decision tree learning

- Widely used learning methods in practice
- Can out-perform human experts in many problems
- Strengths include
- Fast and simple to implement
- Can convert result to a set of easily interpretable rules
- Empirically valid in many commercial products
- Handles noisy data
- Weaknesses include
- Univariate splits/partitioning using only one attribute at a time so limits types of possible trees
- Large decision trees may be hard to understand
- Requires fixed-length feature vectors
- Non-incremental (i.e., batch method)

