

Adversarial Search Aka Games

Chapter 6

Some material adopted from notes by Charles R. Dyer, University of Wisconsin-Madison

Overview

- Game playing
 - State of the art and resources
 - Framework
- Game trees
 - Minimax
 - Alpha-beta pruning
 - Adding randomness

Why study games?

- Interesting, hard problems which require minimal "initial structure"
- Clear criteria for success
- Offer an opportunity to study problems involving {hostile, adversarial, competing} agents and the uncertainty of interacting with the natural world
- Historical reasons: For centuries humans have used them to exert their intelligence
- Fun, good, easy to understand PR potential
- Games often define very large search spaces
 chess 35¹⁰⁰ nodes in search tree, 10⁴⁰ legal states

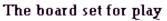
State of the art

• Chess:

- Deep Blue beat Gary Kasparov in 1997
- Garry Kasparav vs. Deep Junior (Feb 2003): tie!
- Kasparov vs. X3D Fritz (November 2003): tie!
- Checkers: Chinook is the world champion
- Checkers: has been solved exactly it's a draw!
- Go: Computer players are decent, at best
- **Bridge**: "Expert" computer players exist, but no world champions yet
- **Poker:** <u>CPRG</u> regularly beats human experts
- Check out: <u>http://www.cs.ualberta.ca/~games/</u>

Chinook

- Chinook is the World Man-Machine Checkers Champion, developed by researchers at the University of Alberta
- It earned this title by competing in human tournaments, winning the right to play for the (human) world championship, and eventually defeating the best players in the world
- Visit http://www.cs.ualberta.ca/~chinook/ to play a version of Chinook over the Internet.
- "<u>One Jump Ahead</u>: Challenging Human Supremacy in Checkers", Jonathan Schaeffer, 1998
- See <u>Checkers Is Solved</u>, J. Schaeffer, et al., Science, v317, n5844, pp1518-22, AAAS, 2007.





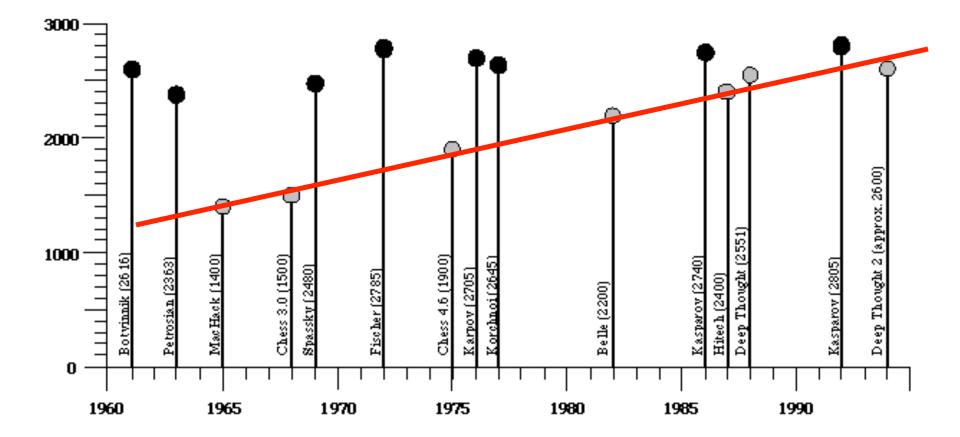
Red to play

Challenging Haman Supremacy in Checkers

Chess early days

- **1948**: Norbert Wiener's book *Cybernetics* describes how a chess program could be developed using a depth-limited minimax search with an evaluation function
- 1950: Claude Shannon publishes one of first papers on playing chess <u>"Programming a Computer for Playing Chess</u>"
- 1951: Alan Turing develops on paper the first program capable of playing a full game of chess
- **1962**: Kotok and McCarthy (MIT) develop first program to play credibly
- **1967**: <u>Mac Hack Six</u>, by Richard Greenblatt et al. (MIT) idefeats a person in regular tournament play

Ratings of human & computer chess champions



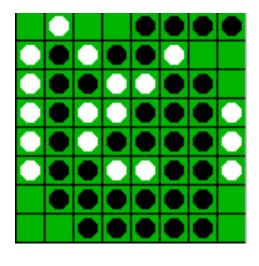




Chess Grand Master Garry Kasparov, left, comtemplates his next move against IBM's Deep Blue chess computer while Chung-Jen Tan, manager of the Deep Blue project looks on iduring the first game of a six-game rematch between Kasparov and Deep Blue in this file photo from 1997. The computer program made history by becoming the first to beat a world chess champion, Kasparov, at a serious game. Photo: Adam Nadel/Associated Press

Othello: Murakami vs. Logistello





open sourced

Takeshi Murakami World Othello Champion

- 1997: The Logistello software crushed Murakami, 6 to 0
- Humans can not win against it
- Othello, with 10²⁸ states, is still not solved

Go: Goemate vs. a young player



Name: Chen Zhixing Profession: Retired Computer skills: self-taught programmer Author of Goemate (arguably the best Go program available today)



Gave Goemate a 9 stone handicap and still easily beat the program, thereby winning \$15,000

Jonathan Schaeffer

Go: Goemate vs. ??



Name: Chen Zhixing Profession: Retired Computer skills:

Go has too high a branching factor for existing search techniques

Current and future software must rely on huge databases and patternrecognition techniques



thereby winning \$15,000

Jonathan Schaeffer

Typical simple case for a game

- 2-person game
- Players alternate moves
- Zero-sum: one player's loss is the other's gain
- **Perfect information**: both players have access to complete information about the state of the game. No information is hidden from either player.
- No chance (e.g., using dice) involved
- Examples: Tic-Tac-Toe, Checkers, Chess, Go, Nim, Othello
- But not: Bridge, Solitaire, Backgammon, Poker, Rock-Paper-Scissors, ...

Can we use ...

- Uninformed serch?
- Heuristic Search?
- Local Search?
- Constraint based search?

How to play a game

- A way to play such a game is to:
 - -Consider all the legal moves you can make
 - -Compute new position resulting from each move
 - -Evaluate each to determine which is best
 - -Make that move
 - –Wait for your opponent to move and repeat
- Key problems are:
 - -Representing the "board" (i.e., game state)
 - -Generating all legal next boards
 - -Evaluating a position

Evaluation function

- Evaluation function or static evaluator is used to evaluate the "goodness" of a game position
 - Contrast with heuristic search where evaluation function was a non-negative estimate of the cost from the start node to a goal and passing through the given node
- Zero-sum assumption lets us use a single evaluation function to describe goodness of a board wrt both players
 - -f(n) >> 0: position n good for me and bad for you
 - $-f(n) \ll 0$: position n bad for me and good for you
 - -f(n) near 0: position n is a neutral position
 - $-\mathbf{f}(\mathbf{n}) = +\mathbf{infinity}$: win for me
 - $-\mathbf{f}(\mathbf{n}) = -\mathbf{infinity}$: win for you

Evaluation function examples

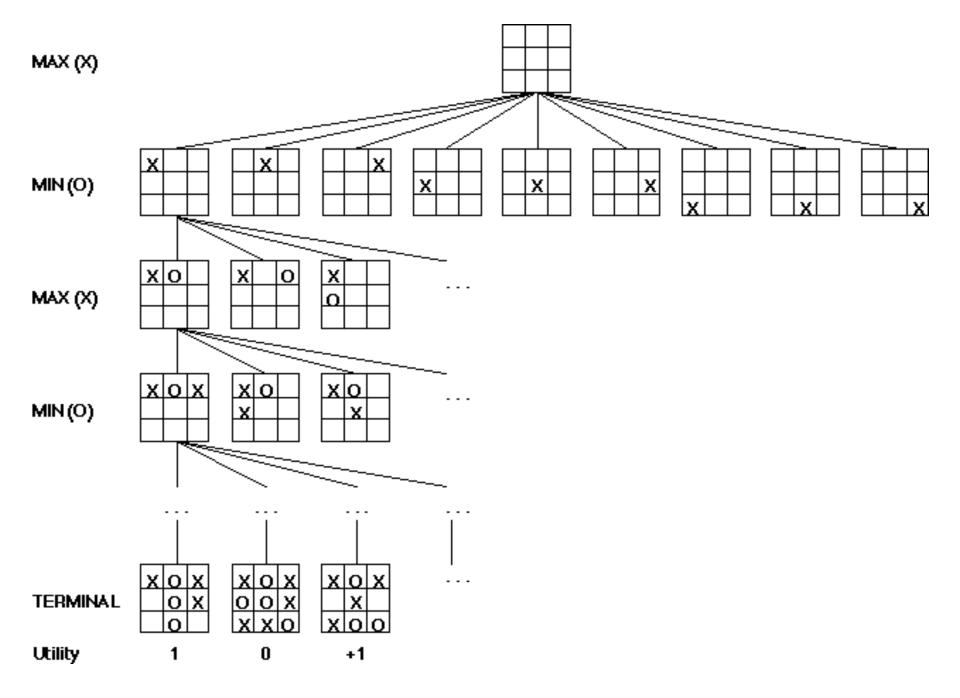
- Example of an evaluation function for Tic-Tac-Toe f(n) = [# of 3-lengths open for me] - [# of 3-lengths open for you] where a 3-length is a complete row, column, or diagonal
- Alan Turing's function for chess
 - f(n) = w(n)/b(n) where w(n) = sum of the point value of white's pieces and b(n) = sum of black's
- Most evaluation functions specified as a weighted sum of position features

 $f(n) = w_1 * feat_1(n) + w_2 * feat_2(n) + ... + w_n * feat_k(n)$

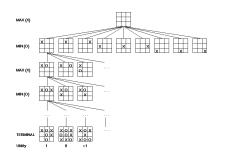
- Example features for chess are piece count, piece placement, squares controlled, etc.
- Deep Blue had >8K features in its evaluation function

That's not how people play

- People use "look ahead"
- i.e. enumerate actions, consider opponent's possible responses, REPEAT
- Producing a complete <u>game tree</u> is only possible for simple games
- So, generate a partial game tree for some number of plys
 - -Move = each player takes a turn
 - -Ply = one player' s turn
- What do we do with the game tree?

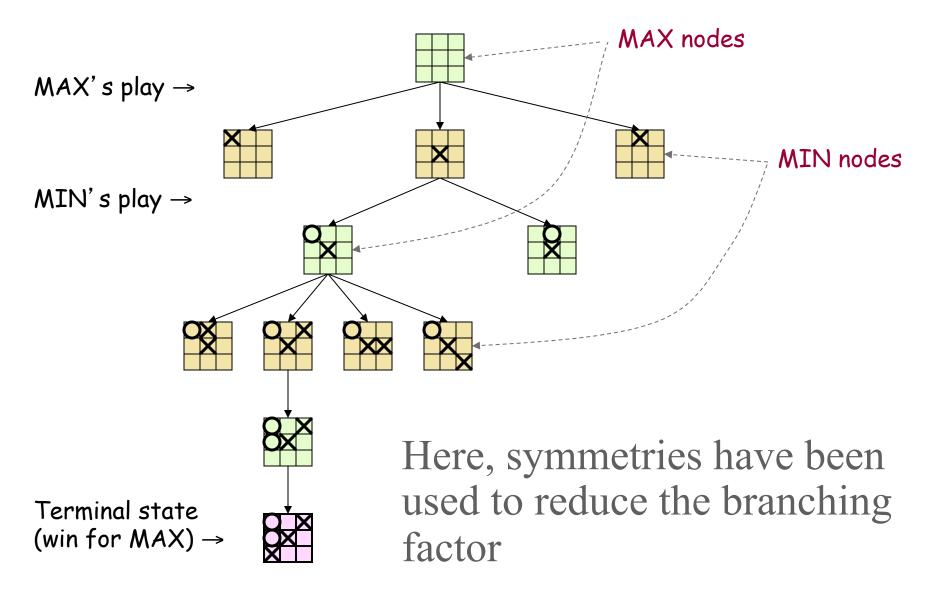


Game trees



- Problem spaces for typical games are trees
- Root node represents the current board configuration; player must decide the best single move to make next
- Static evaluator function rates a board position f(board) a real, >0 for me <0 for opponent
- Arcs represent the possible legal moves for a player
- If it is **my turn** to move, then the root is labeled a "**MAX**" node; otherwise it is labeled a "**MIN**" node, indicating **my opponent's turn**.
- Each level of the tree has nodes that are all MAX or all MIN; nodes at level i are of the opposite kind from those at level i+1

Game Tree for Tic-Tac-Toe



Minimax procedure

- Create start node as a MAX node with current board configuration
- Expand nodes down to some **depth** (a.k.a. **ply**) of lookahead in the game
- Apply the evaluation function at each of the leaf nodes
- "Back up" values for each of the non-leaf nodes until a value is computed for the root node
 - At MIN nodes, the backed-up value is the minimum of the values associated with its children.
 - At MAX nodes, the backed-up value is the maximum of the values associated with its children.
- Pick the operator associated with the child node whose backed-up value determined the value at the root

Minimax theorem

- Intuition: assume your opponent is at least as smart as you are and play accordingly. If he's not, you can only do better.
- Von Neumann, J: *Zur Theorie der Gesellschaftsspiele* Math. Annalen. **100** (1928) 295-320

For every two-person, zero-sum game with finite strategies, there exists a value V and a mixed strategy for each player, such that (a) given player 2's strategy, the best payoff possible for player 1 is V, and (b) given player 1's strategy, the best payoff possible for player 2 is -V.

• You can think of this as:

-Minimizing your maximum possible loss

-Maximizing your minimum possible gain

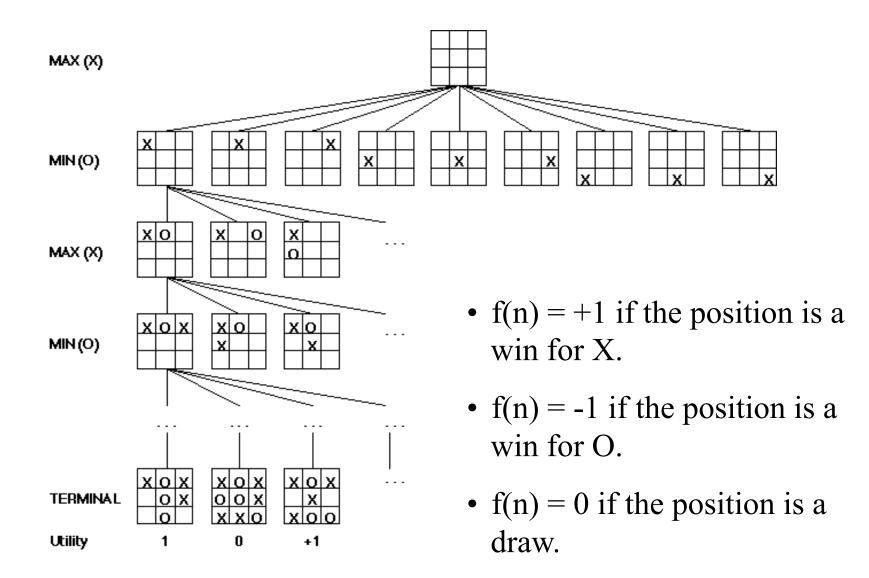
Minimax Algorithm

Static evaluator value

This is the move selected by minimax



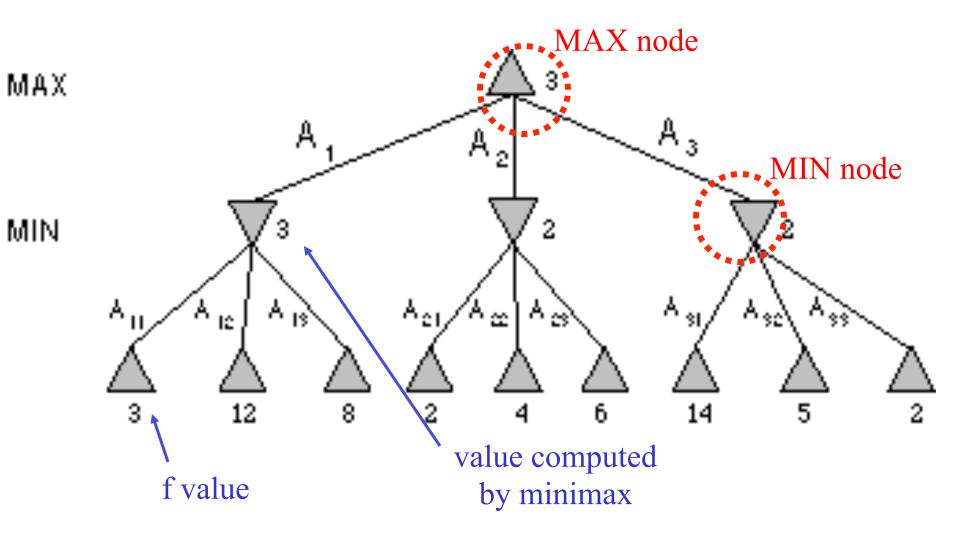
Partial Game Tree for Tic-Tac-Toe



Why use backed-up values?

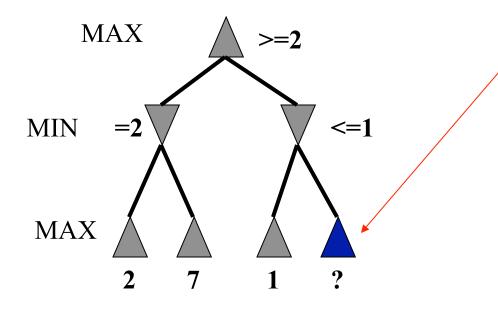
- Intuition: if our evaluation function is good, doing look ahead and backing up the values with Minimax should do better
- At each non-leaf node N, the backed-up value is the value of the best state that MAX can reach at depth h if MIN plays well (by the same criterion as MAX applies to itself)
- If e is to be trusted in the first place, then the backed-up value is a better estimate of how favorable STATE(N) is than e(STATE(N))
- We use a horizon **h** because in general, our time to compute a move is limited

Minimax Tree



Alpha-beta pruning

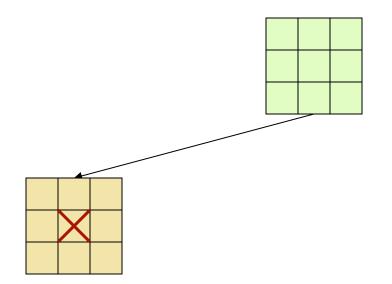
- We can improve on the performance of the minimax algorithm through **alpha-beta pruning**
- Basic idea: *"If you have an idea that is surely bad, don't take the time to see how truly awful it is." --* Pat Winston

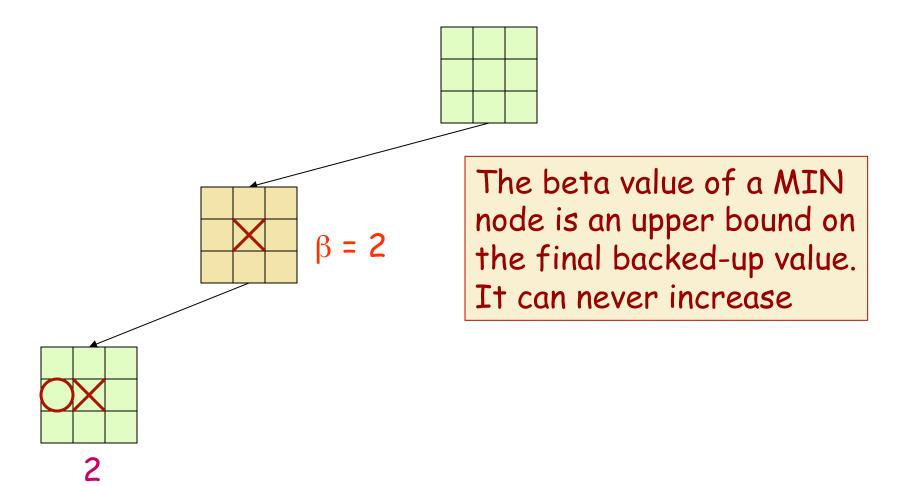


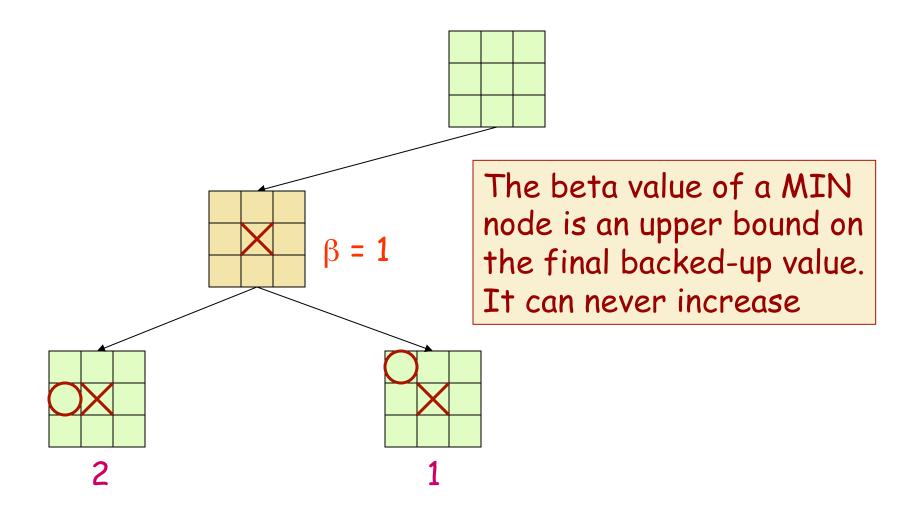
- We don't need to compute the value at this node.
- No matter what it is, it can't affect the value of the root node.

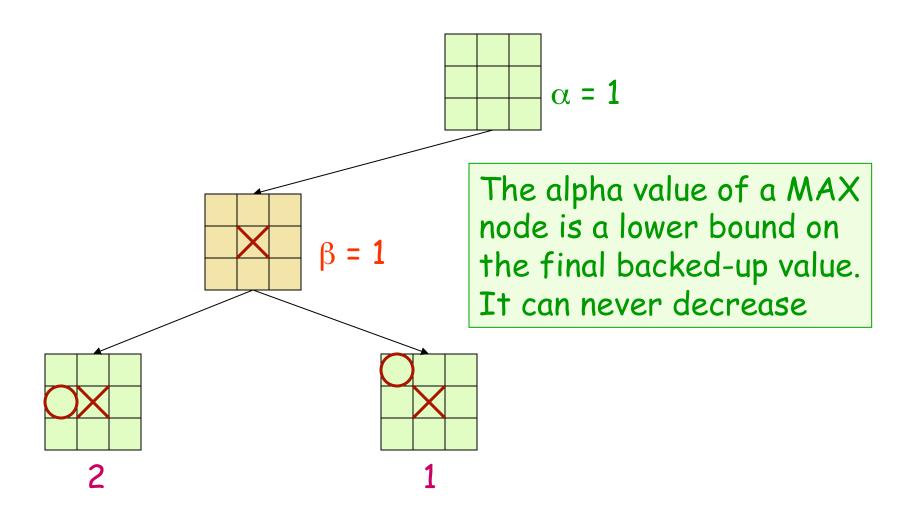
Alpha-beta pruning

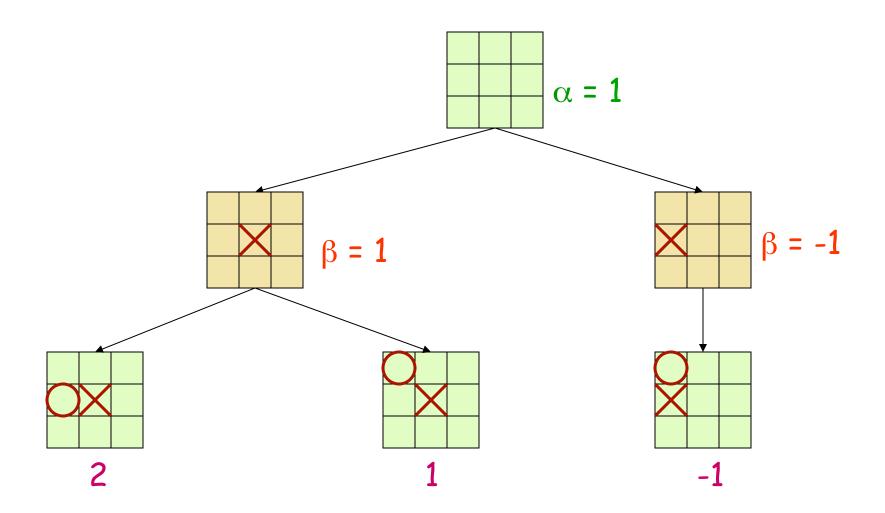
- Traverse the search tree in depth-first order
- At each MAX node n, alpha(n) = maximum value found so far
- At each MIN node n, beta(n) = minimum value found so far
 - The alpha values start at $-\infty$ and only increase, while beta values start at $+\infty$ and only decrease
- Beta cutoff: Given MAX node n, cut off search below n (i.e., don't generate/examine any more of n's children) if alpha(n) >= beta(i) for some MIN node ancestor i of n.
- Alpha cutoff: stop searching below MIN node n if beta(n) <= alpha(i) for some MAX node ancestor i of n.

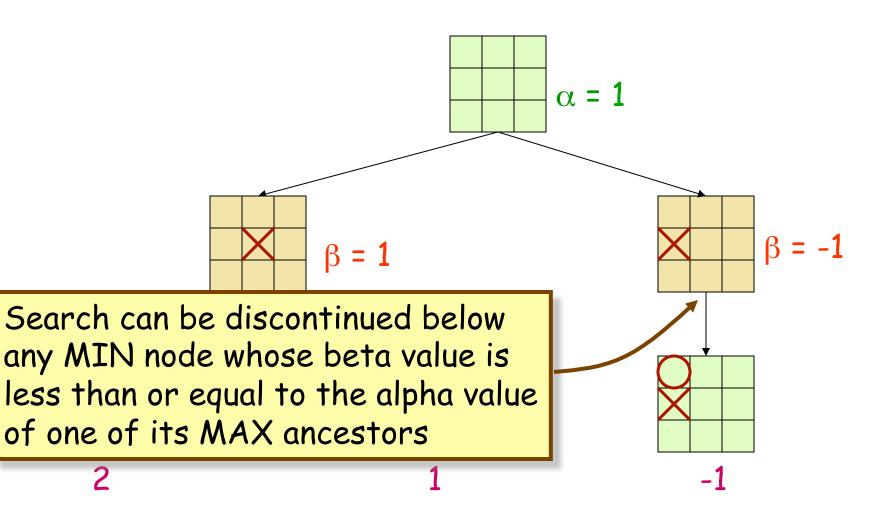




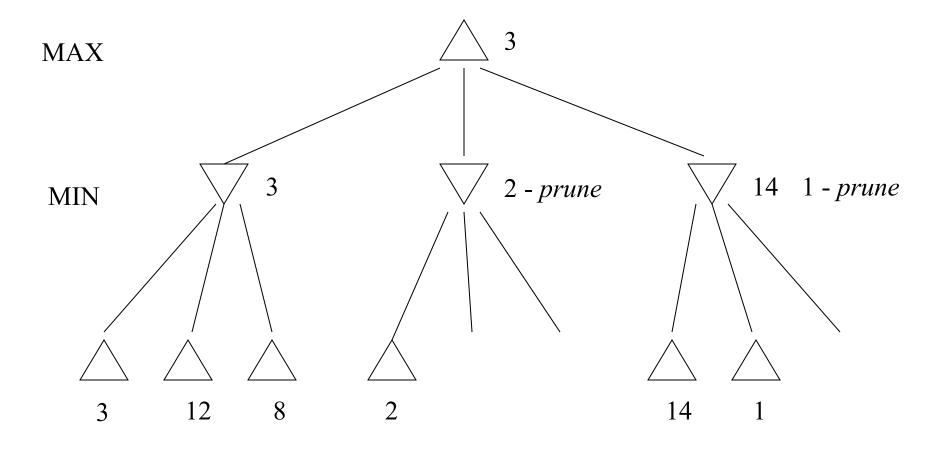




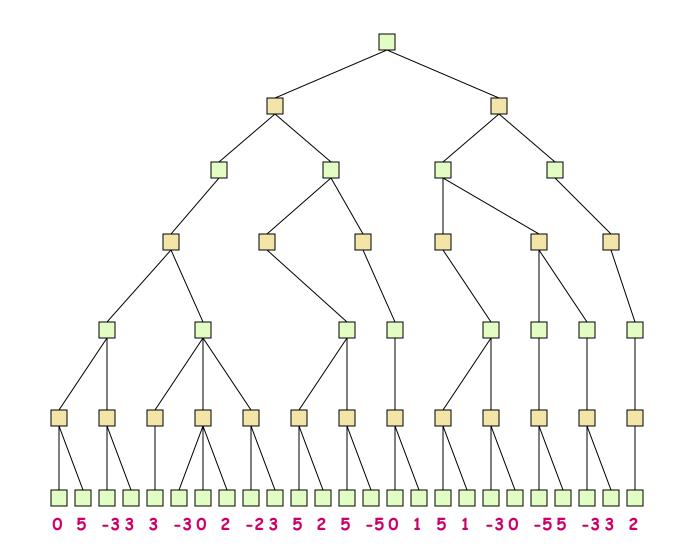


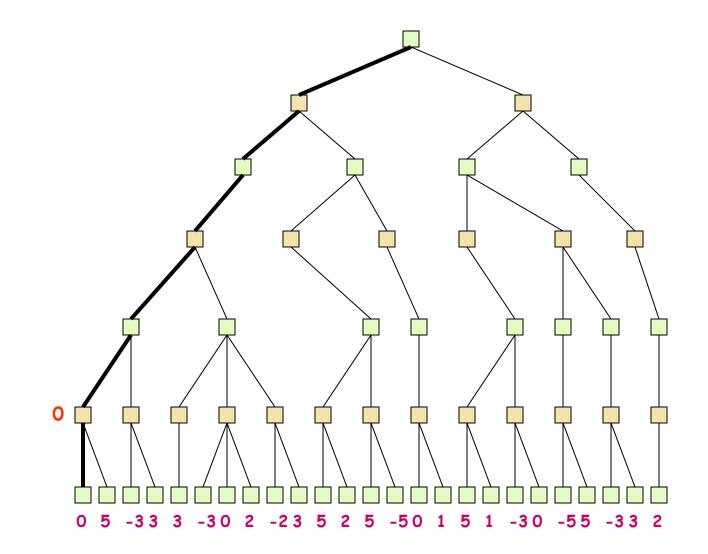


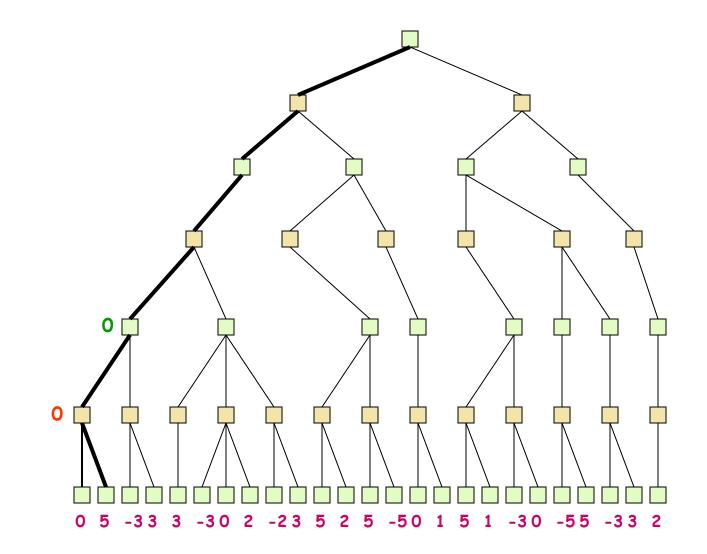
Alpha-beta general example

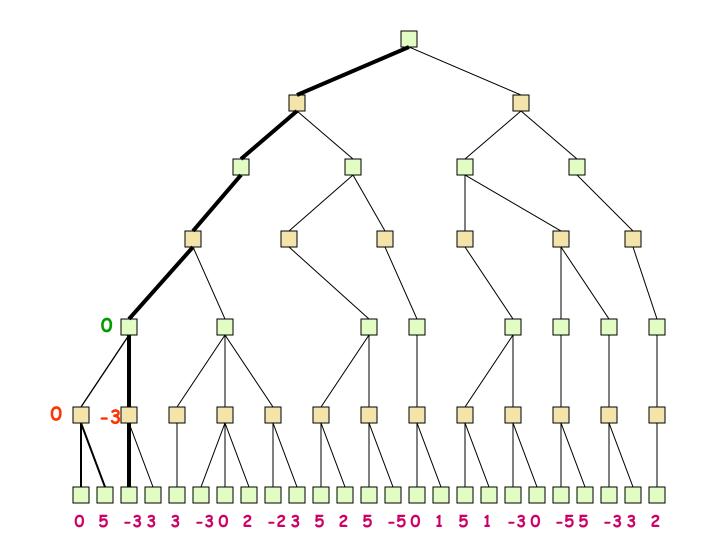


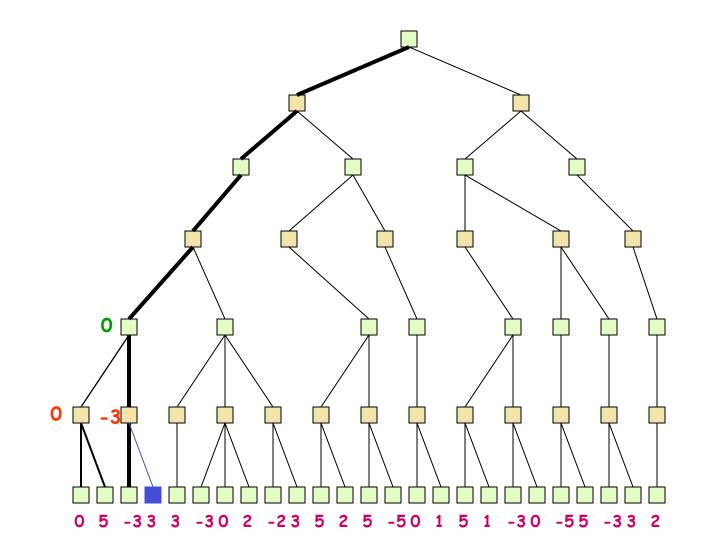
Alpha-Beta Tic-Tac-Toe Example 2

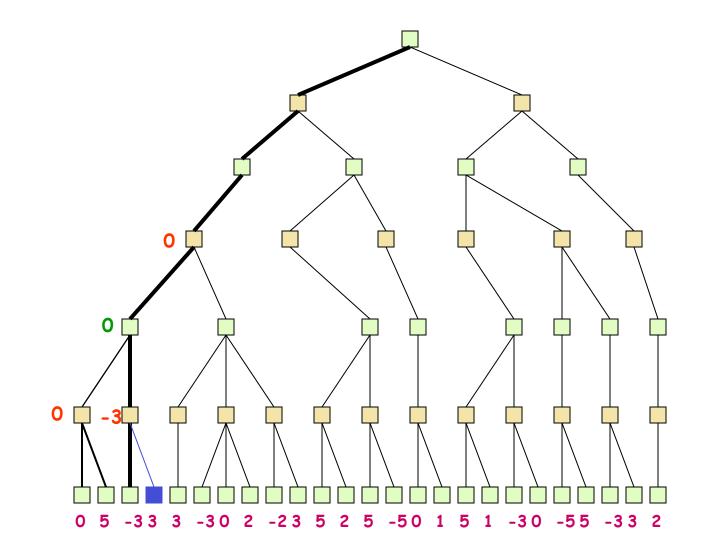


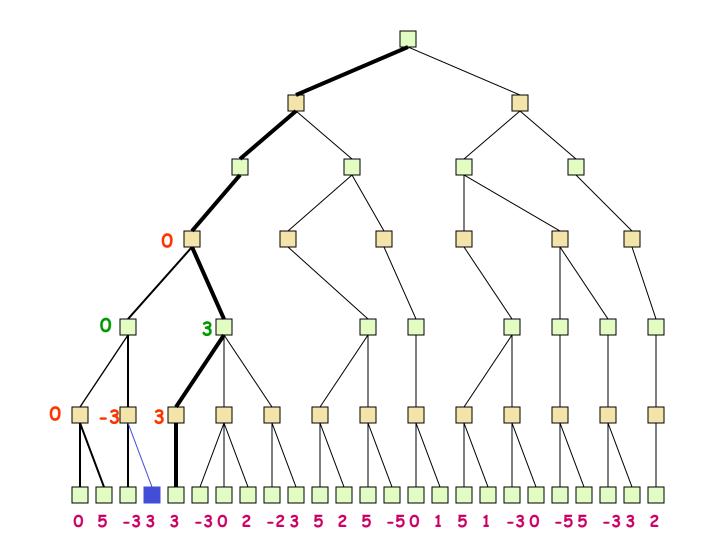


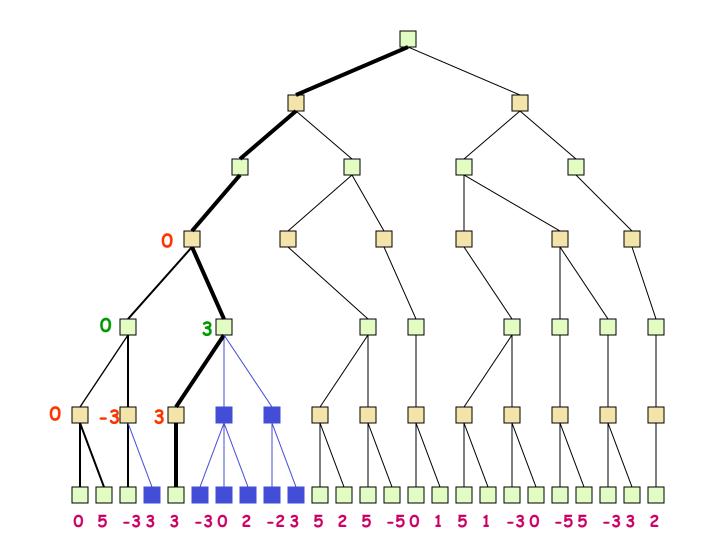


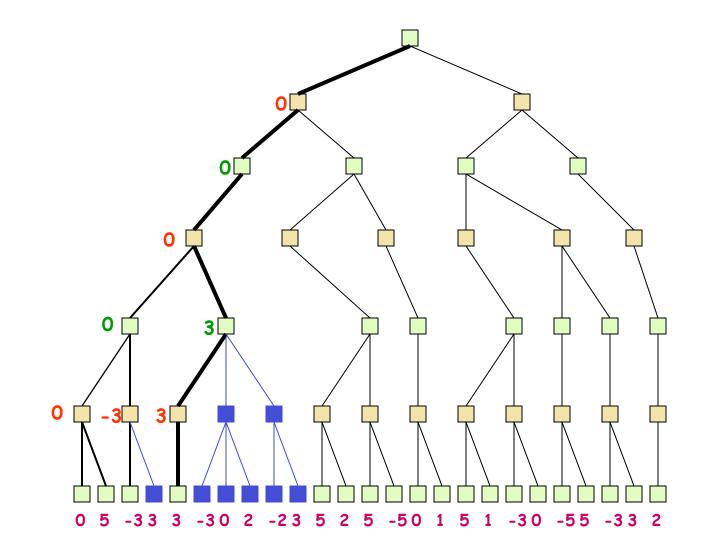


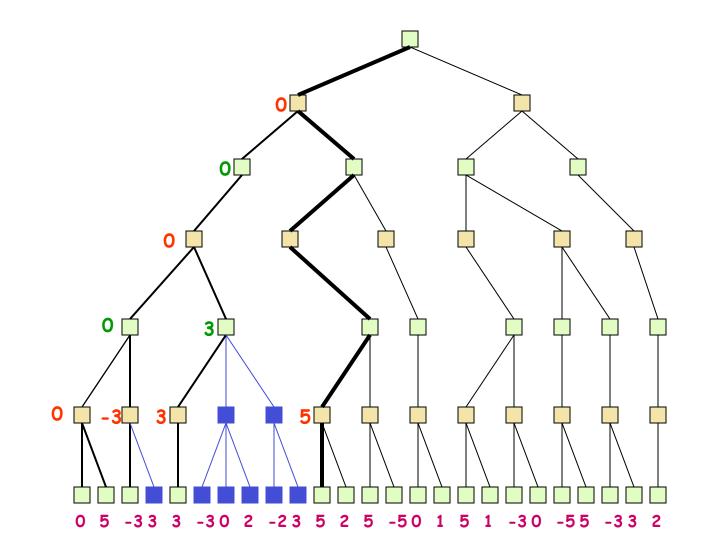


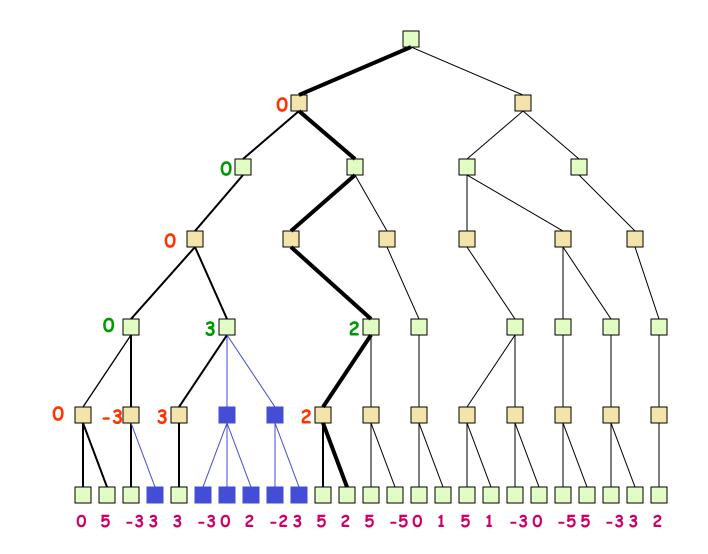


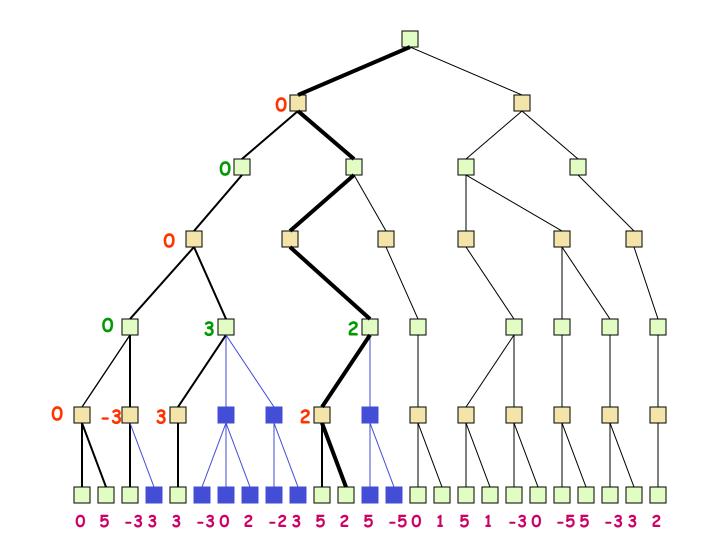


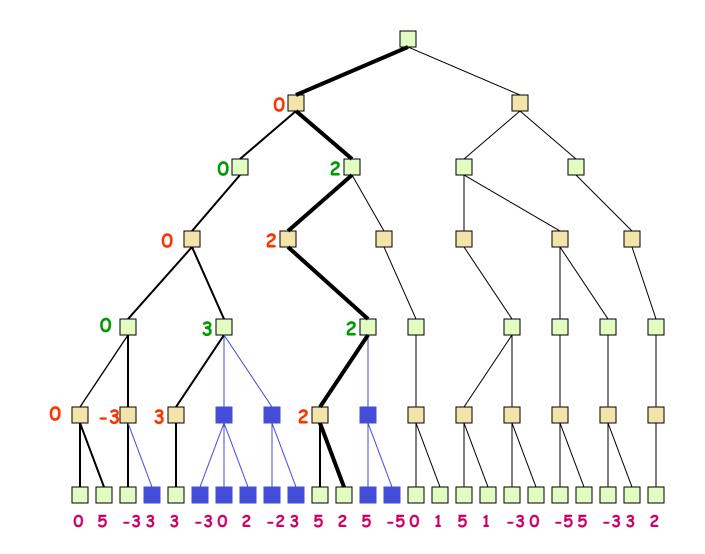


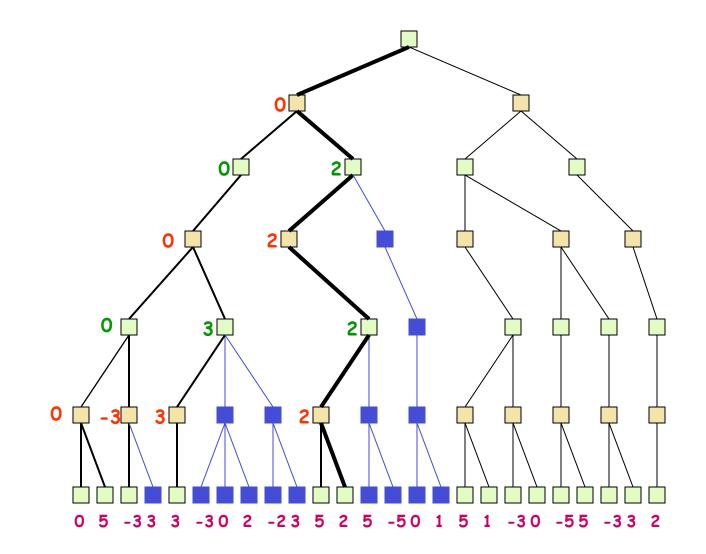


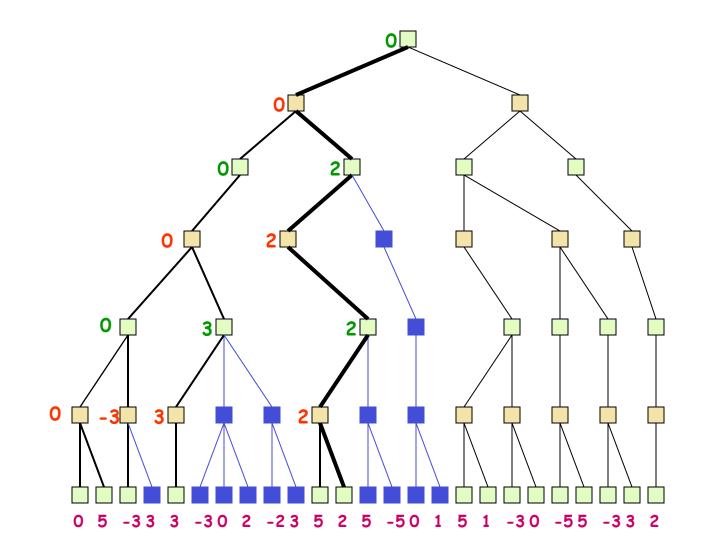


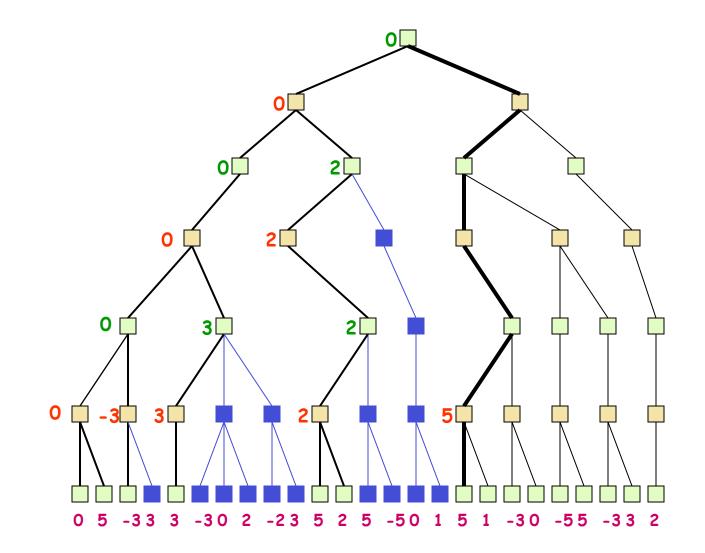


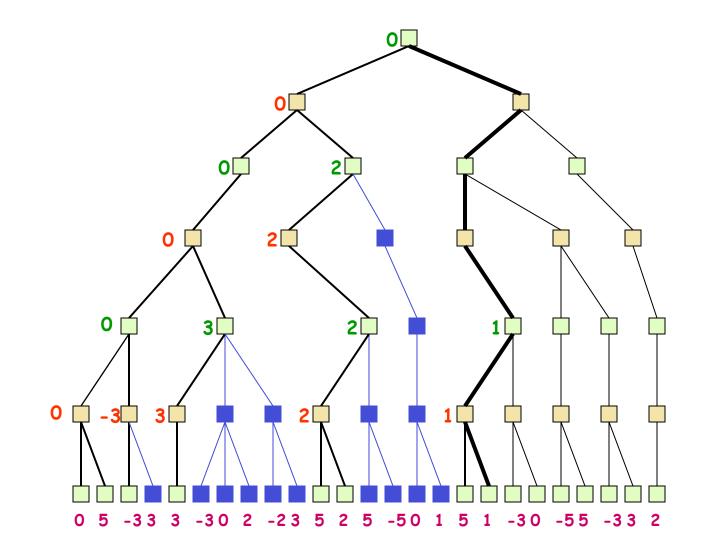


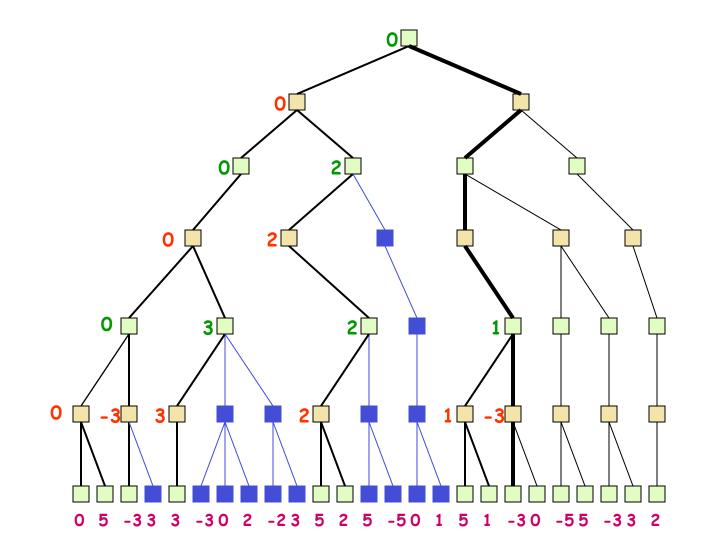


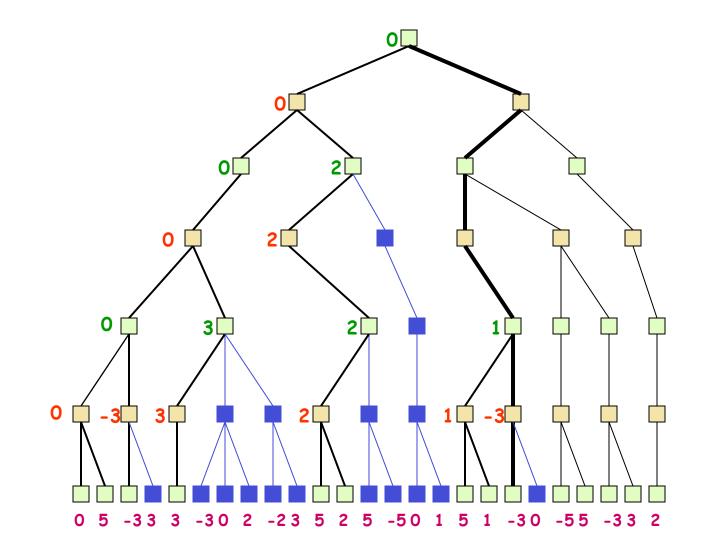


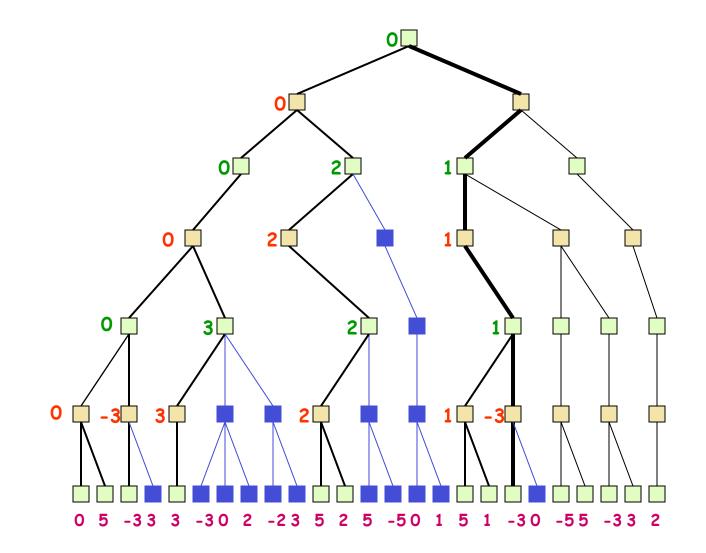


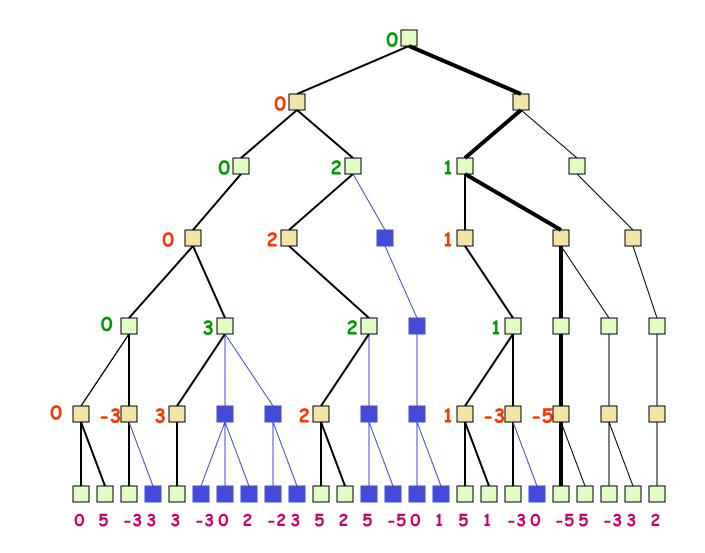


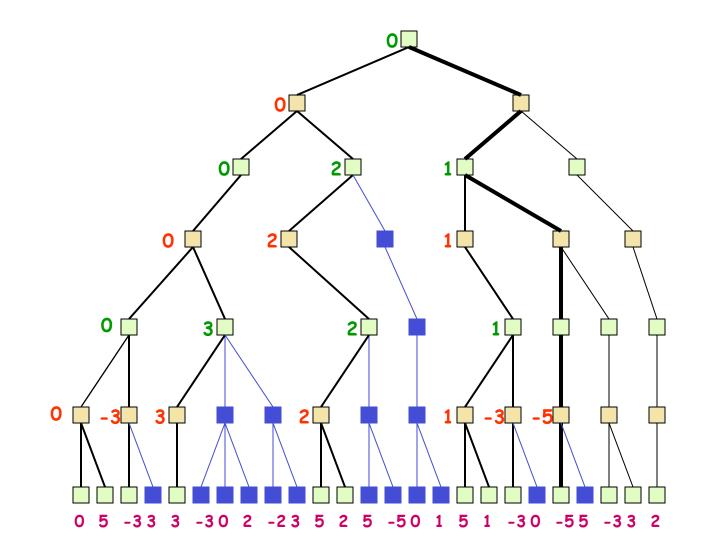


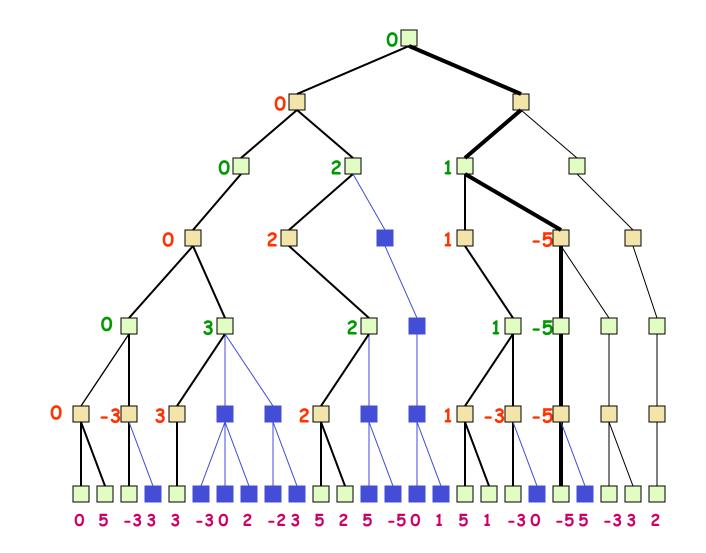


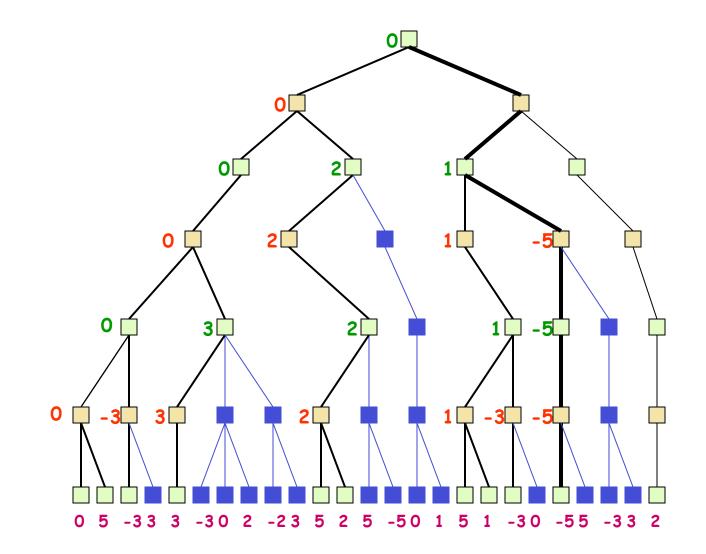


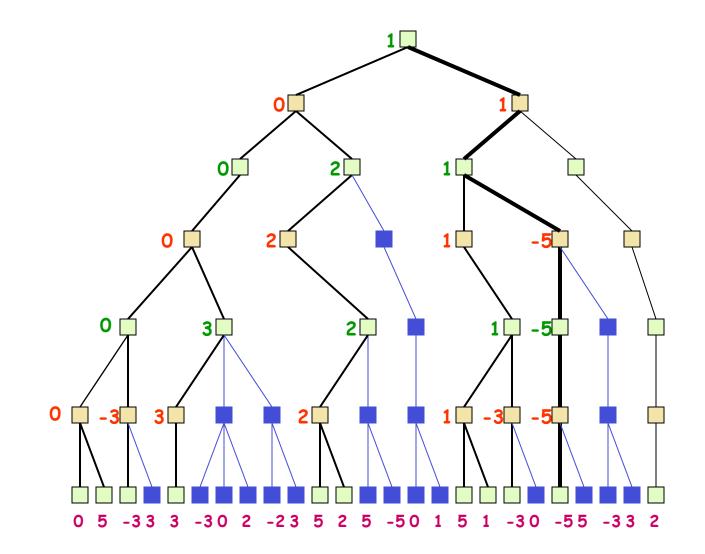


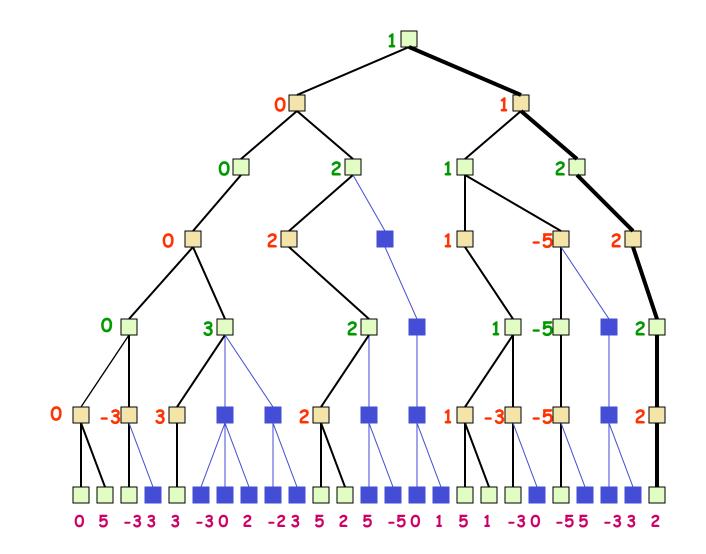


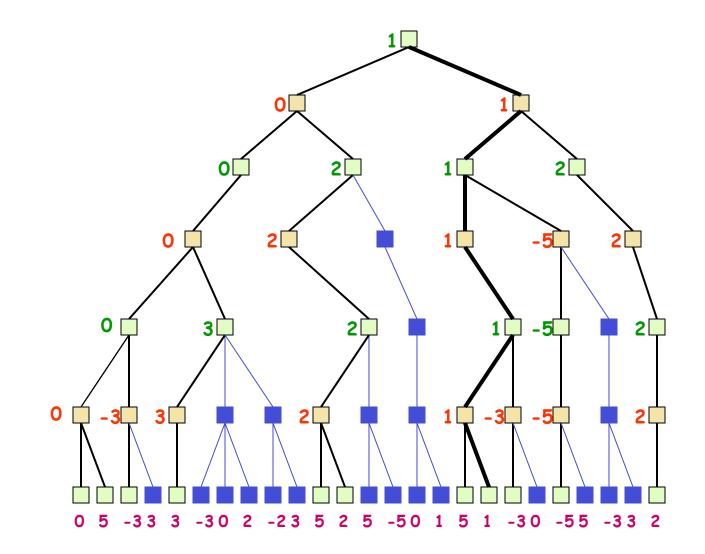












Alpha-beta algorithm

```
function MAX-VALUE (state, \alpha, \beta)
    ;; \alpha = best MAX so far; \beta = best MIN
if TERMINAL-TEST (state) then return UTILITY(state)
v := -\infty
for each s in SUCCESSORS (state) do
    v := MAX (v, MIN-VALUE (s, \alpha, \beta))
    if v \geq \beta then return v
    \alpha := MAX (\alpha, v)
end
return v
function MIN-VALUE (state, \alpha, \beta)
if TERMINAL-TEST (state) then return UTILITY(state)
v := ∞
for each s in SUCCESSORS (state) do
    v := MIN (v, MAX-VALUE (s, \alpha, \beta))
    if v \leq \alpha then return v
    \beta := MIN (\beta, v)
end
return v
```

Effectiveness of alpha-beta

- Alpha-beta is guaranteed to compute the same value for the root node as computed by minimax, with less or equal computation
- Worst case: no pruning, examining b^d leaf nodes, where each node has b children and a d-ply search is performed
- Best case: examine only $(2b)^{d/2}$ leaf nodes.
 - Result is you can search twice as deep as minimax!
- **Best case** is when each player's best move is the first alternative generated
- In Deep Blue, they found empirically that alpha-beta pruning meant that the average branching factor at each node was about 6 instead of about 35!

Other Improvements

- Adaptive horizon + iterative deepening
- Extended search: Retain k>1 best paths (not just one) extend the tree at greater depth below their leaf nodes to help dealing with the "horizon effect"
- **Singular extension**: If a move is obviously better than the others in a node at horizon h, then expand it
- Use **transposition tables** to deal with repeated states
- Null-move search: assume player forfeits move; do a shallow analysis of tree; result must surely be worse than if player had moved. Can be used to recognize moves that should be explored fully.

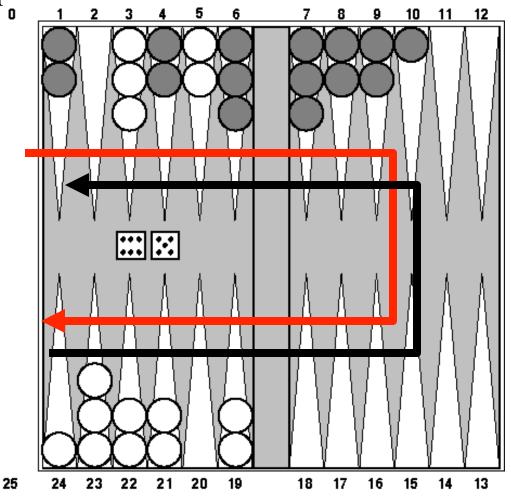
Stochastic Games



- In real life, unpredictable external events can put us into unforeseen situations
- Many games introduce unpredictability through a random element, such as the throwing of dice
- These offer simple scenarios for problem solving with adversaries and uncertainty

Example: Backgammon

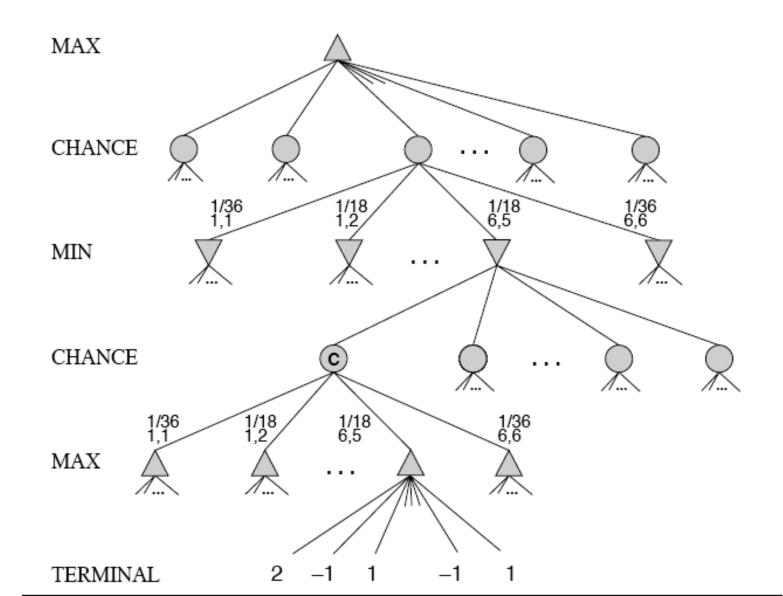
- Backgammon is a two-player game with **uncertainty**.
- •Players roll dice to determine what moves to make.
- •White has just rolled 5 and 6 and has four legal moves:
 - 5-10, 5-11
 - 5-11, 19-24
 - 5-10, 10-16
 - 5-11, 11-16
- •Such games are good for exploring decision making in adversarial problems involving skill and luck



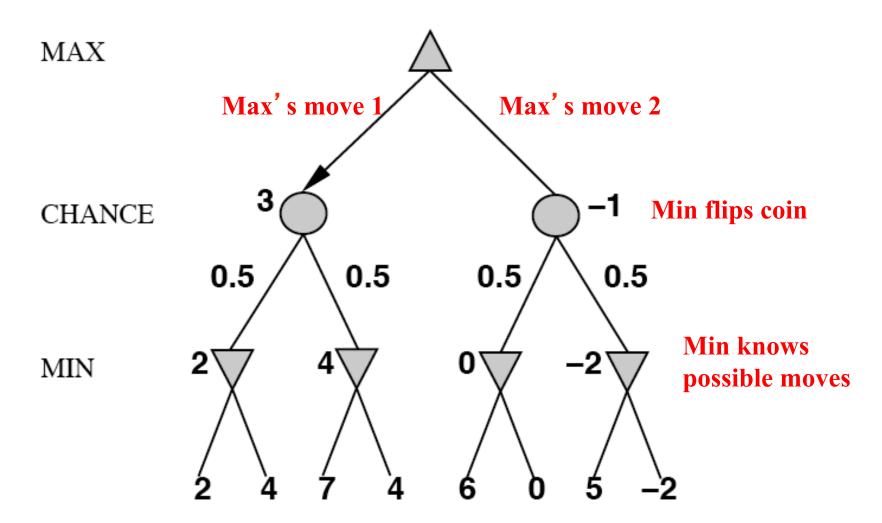
Why can't we use MiniMax?

- Before a player chooses her move, she rolls dice and then knows exactly what they are
- And the immediate outcome of each move is also known
- But she does not know what moves her opponent will have available to choose from
- We need to adapt MiniMax to handle this

MiniMax trees with Chance Nodes



Understanding the notation



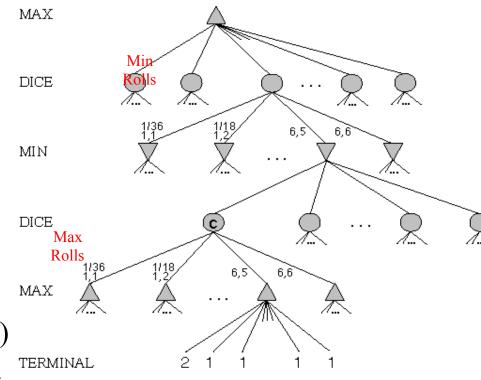
Board state includes the chance outcome determining what moves are available

Game trees with chance nodes

- Chance nodes (shown as circles) represent random events
- For a random event with N outcomes, a chance node has N children; a probability is associated with each
- 2 dice: 21 distinct outcomes
- Use minimax to compute values for MAX and MIN nodes
- Use **expected values** for chance nodes
- For chance nodes over a max node:

expectimax(C) = $\sum_{i} (P(d_i) * maxvalue(i))$

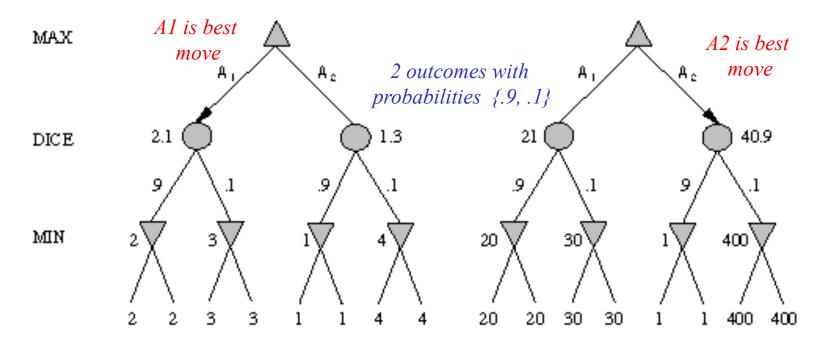
• For chance nodes over a min node: expectimin(C) = $\sum_{i} (P(d_i) * minvalue(i))$



Impact on Lookahead

- Dice rolls increase branching factor
 - -21 possible rolls with 2 dice
- Backgammon has ~20 legal moves for a given roll ~6K with 1-1 roll
- At depth 4 there are 20 * (21 * 20)**3 \approx 1.2B boards
- As depth increases, probability of reaching a given node shrinks
 - value of lookahead is diminished
 - alpha-beta pruning is much less effective
- <u>TDGammon</u> used depth-2 search + very good static evaluator to achieve world-champion level

Meaning of the evaluation function



- With probabilities and expected values we must be careful about the "meaning" of values returned by static evaluator
- A "relative-order preserving" change of the values doesn't change decision of minimax, but could with chance nodes
- Linear transformations are OK

Games of imperfect information

- Example: card games, where opponent's initial cards are unknown
 - We can calculate a probability for each possible deal
 - Like having one big dice roll at the beginning of the game
- Possible approach: compute minimax value of each action in each deal, then choose the action with highest expected value over all deals
- Special case: if action is optimal for all deals, it's optimal
- GIB, a top bridge program, approximates this idea by
 1) generating 100 deals consistent with bidding information
 2) picking the action that wins most tricks on average

High-Performance Game Programs

- Many game programs are based on alpha-beta + iterative deepening + extended/singular search + transposition tables + huge databases + ...
- For instance, <u>Chinook</u> searched all checkers configurations with 8 pieces or less and created an endgame database of 444 billion board configurations
- The methods are general, but their implementation is dramatically improved by many specifically tuned-up enhancements (e.g., the evaluation functions) like an F1 racing car

Other Issues

- Multi-player games
 - E.g., many card games like Hearts
- Multiplayer games with alliances
 - E.g., Risk
 - More on this when we discuss "game theory"
 - Good model for a social animal like humans, where we are always balancing cooperation and competition

AI and Games II

- AI is also of interest to the video game industry
- Many games include 'agents' controlled by the game program that could be

-Adversaries, e.g. in a *first person shooter* game

- -Collaborators, e.g., in a virtual reality game
- Some game environments are used as AI challenges
 - -2009 Mario AI Competition
 - -<u>Unreal Tournament bots</u>

Perspective on Games: Con and Pro

"Chess is the Drosophila of artificial intelligence. However, computer chess has developed much as genetics might have if the geneticists had concentrated their efforts starting in 1910 on breeding racing Drosophila. We would have some science, but mainly we would have very fast fruit flies."

John McCarthy, Stanford

"Saying Deep Blue doesn't really think about chess is like saying an airplane doesn't really fly because it doesn't flap its wings."

Drew McDermott, Yale

General Game Playing

- <u>General Game Playing</u> is an idea developed by Professor Michael Genesereth of Stanford
- See his <u>site</u> for more information
- Goal: don't develop specialized systems to play specific games (e.g., Checkers) very well
- Goal: design AI programs to be able to play more than one game successfully
- Work from a description of a novel game



General Game Playing

- Stanford's GGP is a Web-based system
- Complete, logical specification of many different games in terms of:
 - relational descriptions of states
 - legal moves and their effects
 - goal relations and their payoffs
- Management of matches between automated players and of competitions involving many players and games

GGP

- Input: logical description of a game in a custom game description language
- Game bots must
 - Learn how to play legally from description
 - Play well using general problem solving strategies
 - Improve using general machine learning techniques
- Yearly completions since 2005, \$10K prize
- Java <u>General Game Playing Base Package</u>

GGP Peg Jumping Game

; <u>http://games.stanford.edu/gamemaster/games-debug/peg.kif</u> (init (hole a c3 peg)) (init (hole a c4 peg))

```
(init (hole d c4 empty))
```

```
(<= (next (pegs ?x)) (does jumper (jump ?sr ?sc ?dr ?dc)) (true (pegs ?y))
  (succ ?x ?y)) (<= (next (hole ?sr ?sc empty)) (does jumper (jump ?sr ?sc ?dr ?dc)))</pre>
```

- (<= (legal jumper (jump ?sr ?sc ?dr ?dc)) (true (hole ?sr ?sc peg))
 (true (hole ?dr ?dc empty)) (middle ?sr ?sc ?or ?oc ?dr ?dc) (true (hole ?or ?oc peg)))</pre>
- (<= (goal jumper 100) (true (hole a c3 empty)) (true (hole a c4 empty)) (true (hole a c5 empty))

```
(succ s1 s2)
(succ s2 s3)
```

. . .

Tic-Tac-Toe in GDL

(role xplayer)
(role oplayer)
;; Initial State
(init (cell 1 1 b))
(init (cell 1 2 b))

(init (control xplayer))
;; Dynamic Components
(<= (next (cell ?m ?n x))
 (does xplayer (mark ?m ?n))
 (true (cell ?m ?n b)))</pre>

(<= (next (cell ?m ?n o))
 (does oplayer (mark ?m ?n))
 (true (cell ?m ?n b)))</pre>

(<= (next (control xplayer)))
 (true (control oplayer)))
(<= (legal ?w (mark ?x ?y))
 (true (cell ?x ?y b))
 (true (control ?w)))
(<= (legal xplayer noop)
 (true (control oplayer)))
(<= (legal oplayer noop)
 (true (control xplayer)))</pre>

(<= (goal xplayer 100) (line x))
...
(<= (goal oplayer 0) (line x))</pre>

See ggp-base repository: <u>http://bit.ly/RB49q5</u>

A example of General Intelligence

- "<u>Artificial General Intelligence</u> describes research that aims to create machines capable of general intelligent action"
- Harkens back to early visions of AI, like McCarthy's <u>Advise Taker</u>

-See Programs with Common Sense (1959)

• A response to frustration with narrow specialists, often seen as "hacks"

-See <u>On Chomsky and the Two Cultures</u> of Statistical Learning