## CMSC 671 Artificial Intelligence - Fall 2013 Homework Assignment 3 Due at the start of class on October $2^{\text {nd }}$

From the Wikipedia Sudoku page:
"The objective is to fill a 9 x 9 grid with digits so that each column, each row, and each of the nine $3 x 3$ sub-grids that compose the grid (also called "boxes", "blocks", "regions", or "sub-squares") contains all of the digits from 1 to 9 . The puzzle setter provides a partially completed grid, which typically has a unique solution."

Below is an example of an easy Sudoku:

|  | 9 |  | 6 |  |  |  | 8 | 1 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
|  | 8 |  | 2 | 4 |  |  | 7 |  |
| 3 |  | 1 |  |  |  | 2 |  |  |
| 8 | 1 |  |  |  |  | 5 |  |  |
| 4 |  | 6 |  |  |  | 1 |  | 7 |
|  |  | 7 |  |  |  |  | 3 | 6 |
|  |  | 3 |  |  |  | 7 |  | 9 |
|  | 5 |  |  | 3 | 9 |  | 1 |  |
| 9 | 7 |  |  |  | 6 |  | 4 |  |

- Formulate solving a Sudoku puzzle as constraint satisfaction. Submit answers to the questions below. (20 points)
- What are the variables?
- What are their domains?
- What are the constraints formulated as binary constraints?
- Does the requirement that each digit has to occur in each row, column, and block have to be directly specified? Why or why not?
- Write a Sudoku solver that does not represent the requirement that each digit has to occur in each row, column, and block directly. Your solver must use the AC 3 algorithm. ( 50 points)
- The input to your algorithm should be a 9 x 9 grid of characters that are either digits or ${ }^{*}{ }^{*}$, if the digit for that location is unspecified. It's output should be in the same form. If no solution can be found then simply output "no solution possible".
- Submit your code and the result of running your program on the Sudoku above.
- Modify your solver to explicitly represent the the requirement that each digit has to occur in each row, column, and block directly. (30 points)
- Submit your code and the result of running your program on the Sudoku above. Also run your algorithm on the two Sudoku below and report the results (either a solution, the fact that no solution is possible, or the fact that your code never terminated).

| 5 |  |  | 8 |  | 2 |  |  | 7 |
| :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- | :--- |
| 4 |  | 9 | 5 | 1 | 3 |  |  |  |
|  | 8 |  |  |  |  |  |  |  |
| 9 |  |  |  |  | 1 | 7 |  |  |
| 3 | 6 |  |  | 9 |  |  | 2 | 1 |
|  |  | 5 | 2 |  |  |  |  | 4 |
|  |  |  |  |  |  |  | 7 |  |
|  |  |  | 9 | 3 | 7 | 2 |  | 8 |
| 8 |  |  | 1 |  | 4 |  |  | 6 |


|  |  |  |  |  |  |  | 7 |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | 9 |  | 5 |  | 4 |  |  | 3 |
|  |  |  |  |  | 2 | 5 | 6 |  |
|  |  | 3 |  |  |  | 8 | 1 |  |
|  |  | 1 | 7 | 3 | 9 | 4 |  |  |
|  | 5 | 9 |  |  |  | 6 |  |  |
|  | 8 | 7 | 2 |  |  |  |  |  |
| 9 |  |  | 8 |  | 3 |  | 5 |  |
|  | 2 |  |  |  |  |  |  |  |

